

PLASMA TURBULENCE IMAGING VIA BEAM EMISSION SPECTROSCOPY IN THE CORE OF THE DIII-D TOKAMAK

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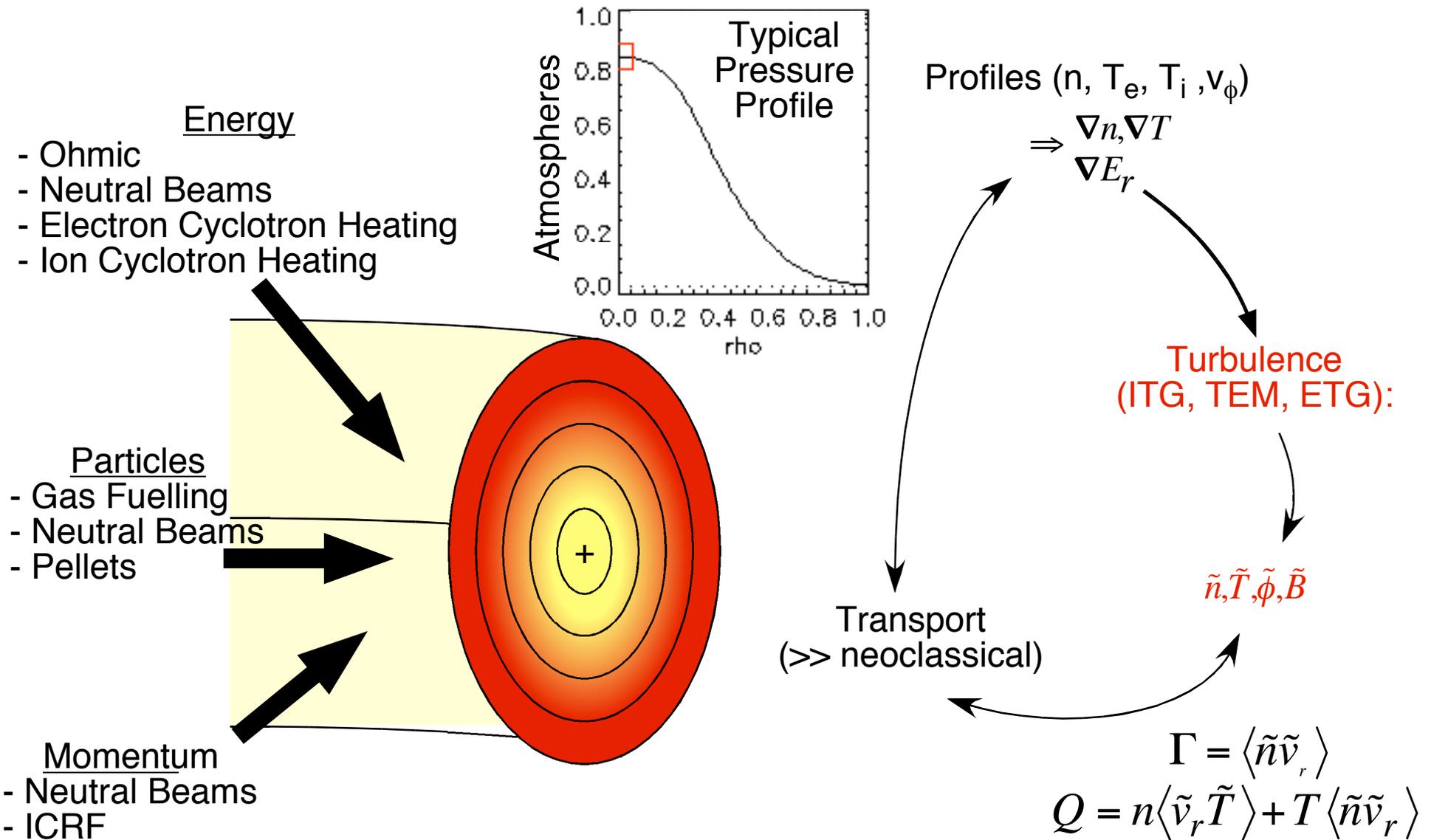
THE UNIVERSITY
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WISCONSIN
MADISON



OUTLINE

- **Role of Turbulence in Magnetically-Confined Plasmas**
- **Motivation to Design, Build and Implement a Higher Sensitivity BES**
- **Overview of Beam Emission Spectroscopy Diagnostic for 2D Density Fluctuation Measurements**
- **Design concepts employed for upgraded BES**
 - *Optics*
 - *Configuration*
 - *Filters*
 - *Detectors*
 - *Data Acquisition*
- **Noise Considerations & Measurements**
- **Example density fluctuation measurements with upgraded BES system**
- **Visualizations of core turbulence**
- **Applications: Time-Resolved Velocimetry Analysis**
- **Summary & Future directions**

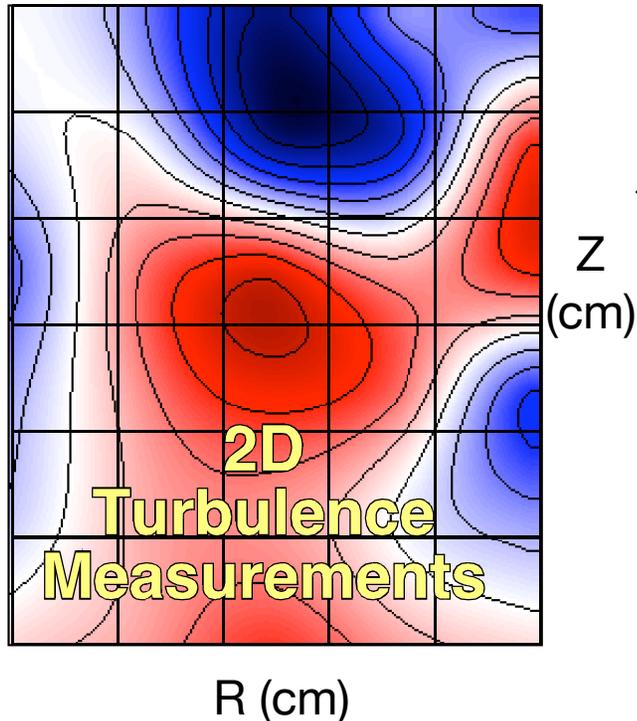
TURBULENCE DRIVES CROSS-FIELD TRANSPORT OF PARTICLES, ENERGY AND MOMENTUM IN A MAGNETICALLY-CONFINED PLASMA



Complex, Highly Nonlinear, Self-Regulating System

WHY MEASURE 2D DENSITY FLUCTUATION CHARACTERISTICS?

Strong Physics Need for Higher Sensitivity 2D Fluctuation Measurements ($k_{\parallel} \ll k_{\perp}$)



Physics Topics

Turbulence Imaging

- Eddy visualization
- Velocity field turbulence

Nonlinear Physics:

- Energy cascade
- Growth rate
- Reynolds Stress

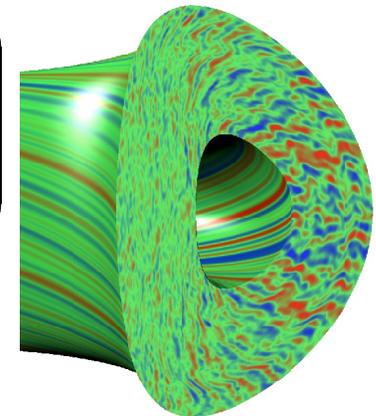
Zonal Flows:

- Core Zonal Flow Identification
- Geodesic Acoustic Mode
- Generation & Interaction

Validation of Nonlinear 3D Simulations (e.g., GYRO)

Turbulent Particle Flux

$$\Gamma = \langle \tilde{n} \tilde{v}_r \rangle$$



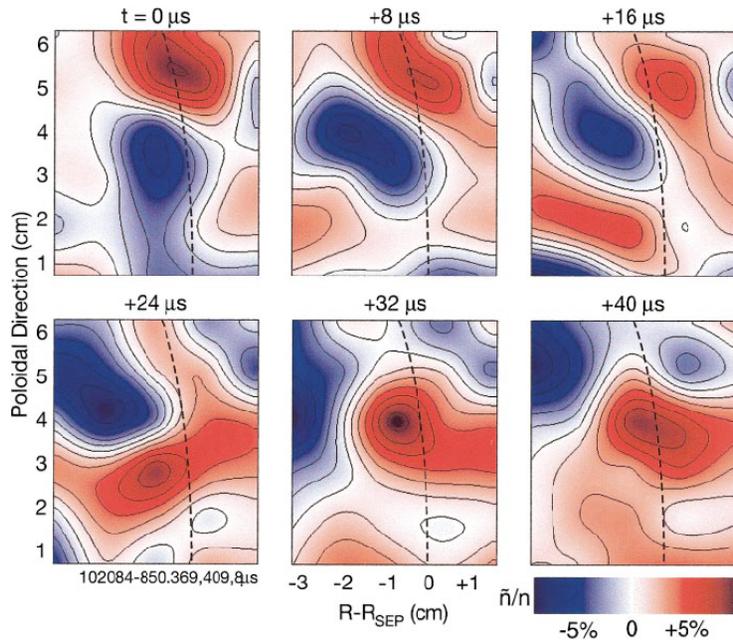
Upgraded BES provides:

$$\tilde{n}(r, Z, t), \tilde{v}(r, Z, t)$$

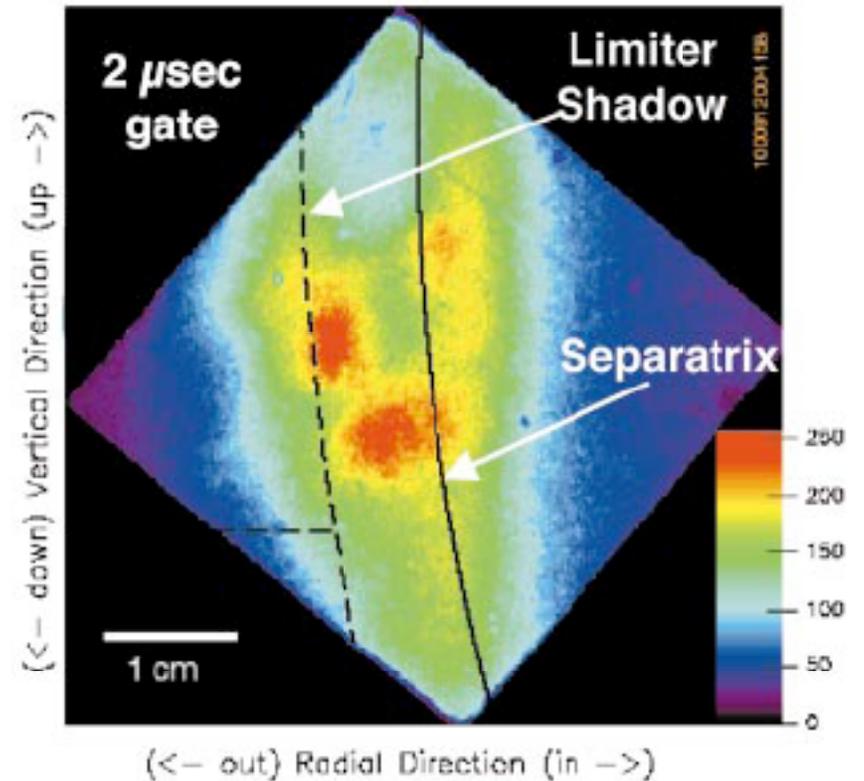
at high sensitivity in core regions of high performance discharges

SEVERAL APPROACHES TO 2D TURBULENCE DIAGNOSTICS HAVE BEEN SUCCESSFULLY DEPLOYED ON PLASMA EXPERIMENTS

BES@DIII-D



Gas Puff Imaging @ NSTX, CMOD



C. Fenzi *et al.*, Rev. Sci. Instrum. **72**, 988 (2001).
G. McKee *et al.*, Rev. Sci. Instrum. **74**, 2014 (2003).

**Imaged edge region due to
signal to noise**

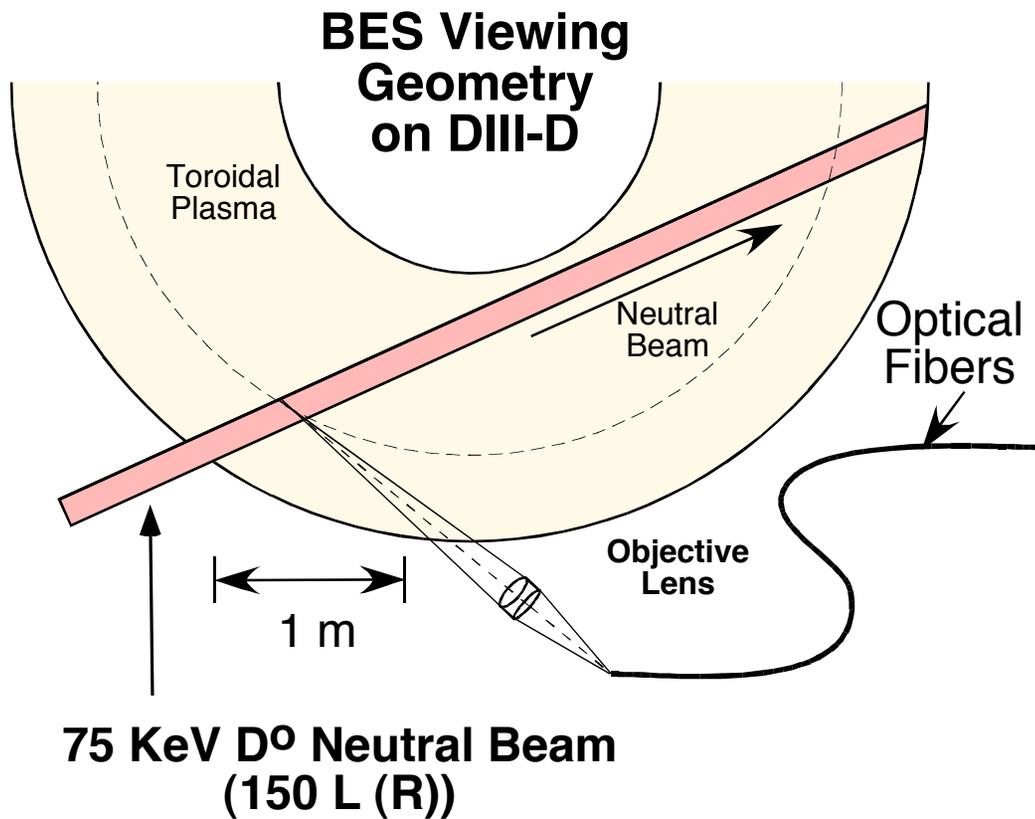
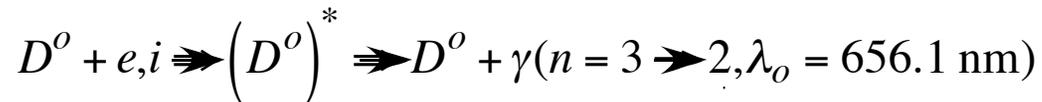
S. Zweben *et al.*, Phys. Plasmas **9**, 1981 (2002).
J. Terry *et al.*, Phys. **10**, 1739 (2003).

Views emission shell near plasma edge

Core Plasma Turbulence Imaging capability is needed!

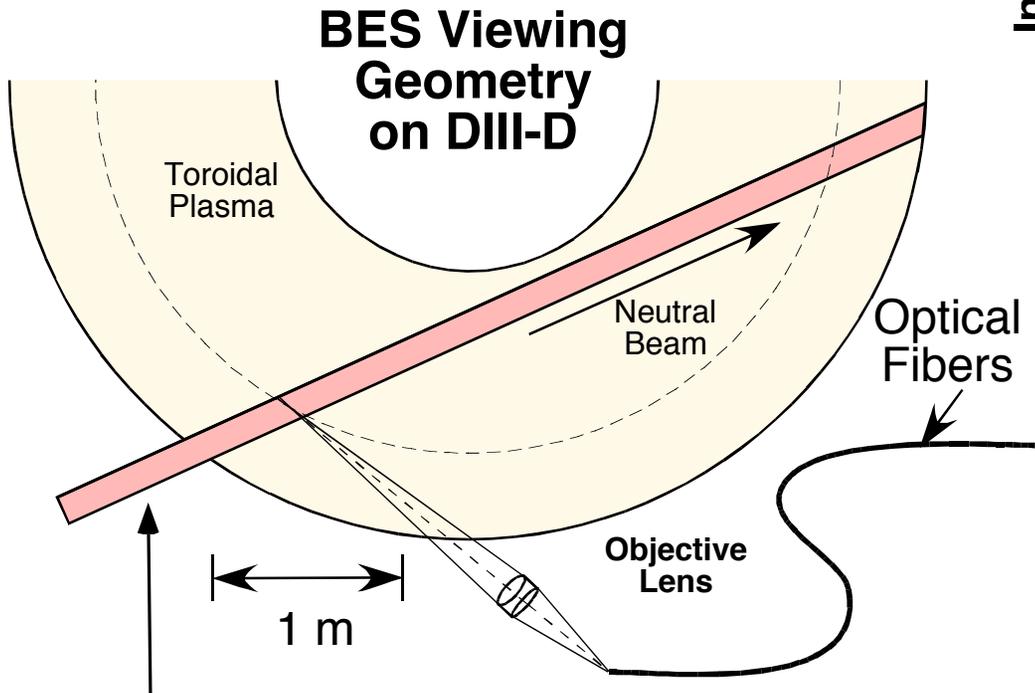
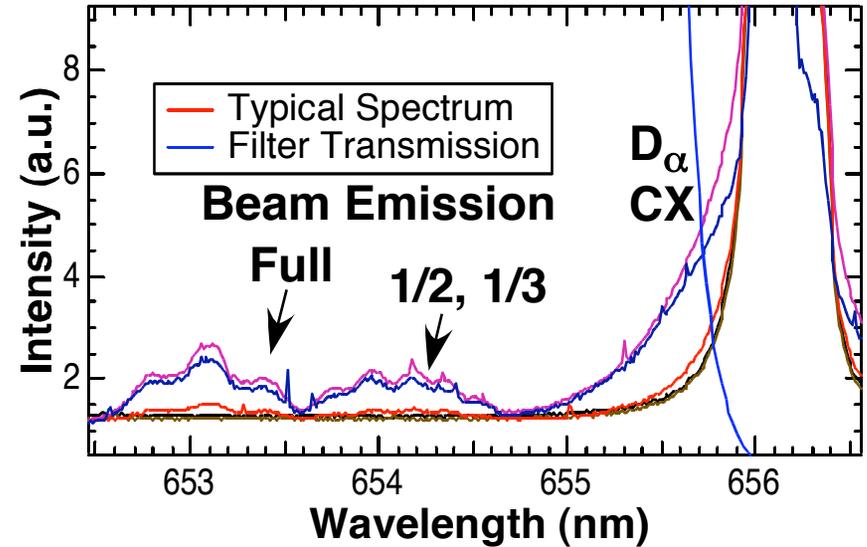
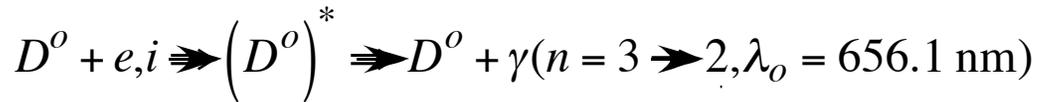
BEAM EMISSION SPECTROSCOPY MEASURES SPATIALLY LOCALIZED, LONG-WAVELENGTH ($k_{\perp}\rho_i < 1$) DENSITY FLUCTUATIONS

Collisionally-excited, Doppler-shifted neutral beam fluorescence



BEAM EMISSION SPECTROSCOPY MEASURES SPATIALLY LOCALIZED, LONG-WAVELENGTH ($k_{\perp}\rho_i < 1$) DENSITY FLUCTUATIONS

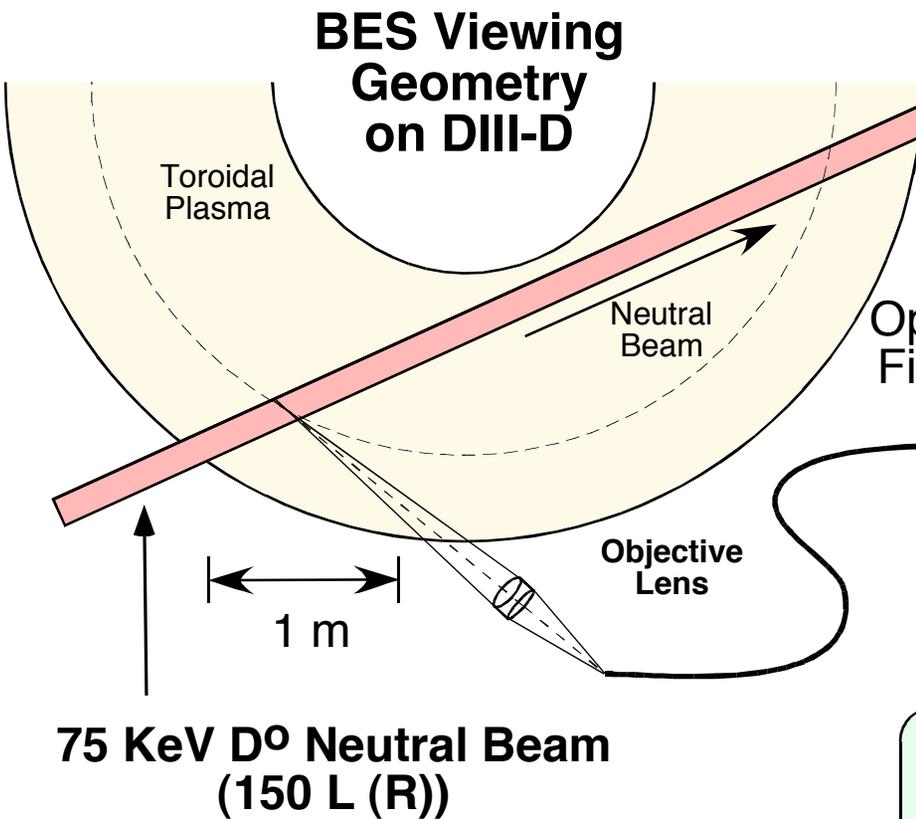
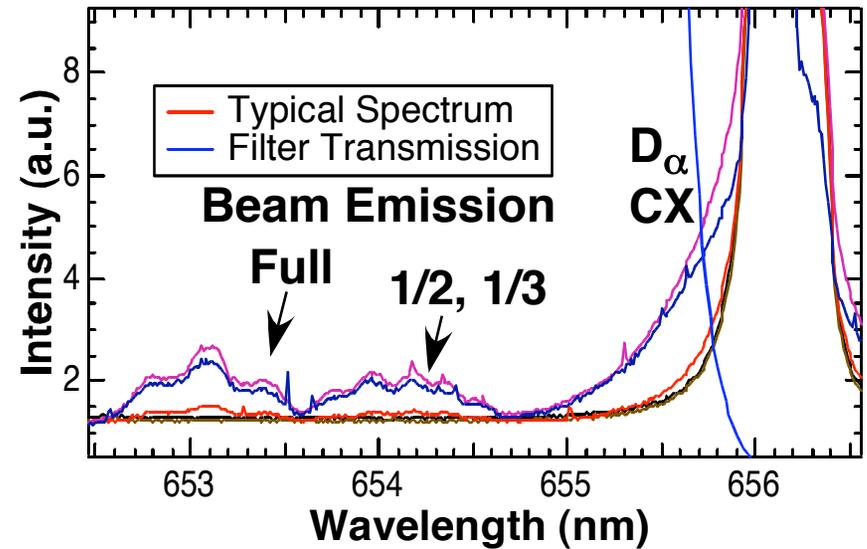
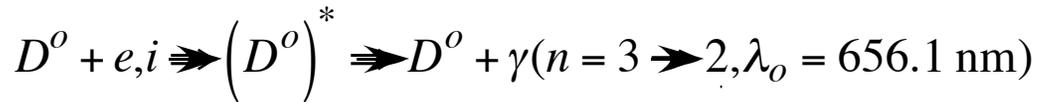
Collisionally-excited, Doppler-shifted neutral beam fluorescence



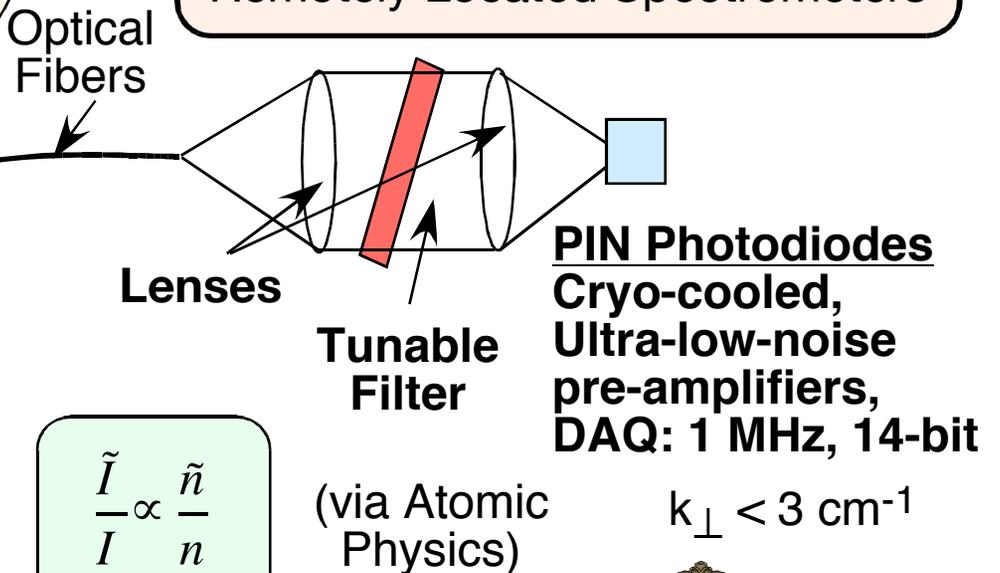
75 KeV D⁰ Neutral Beam
(150 L (R))

BEAM EMISSION SPECTROSCOPY MEASURES SPATIALLY LOCALIZED, LONG-WAVELENGTH ($k_{\perp}\rho_i < 1$) DENSITY FLUCTUATIONS

Collisionally-excited, Doppler-shifted neutral beam fluorescence

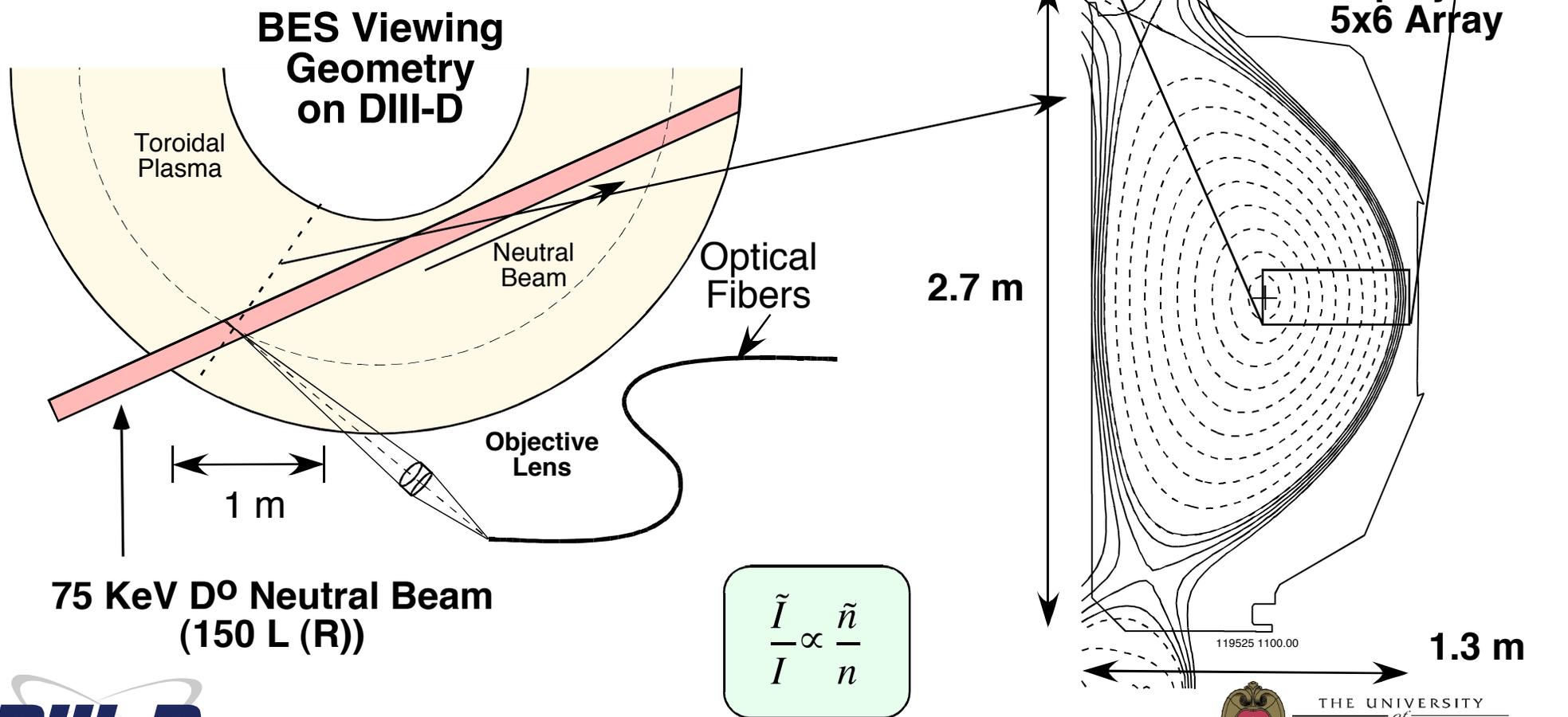
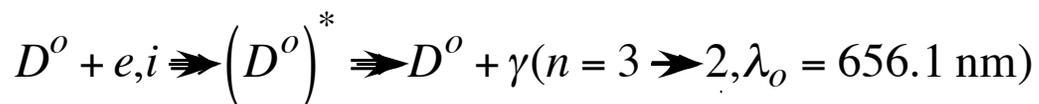


Remotely Located Spectrometers



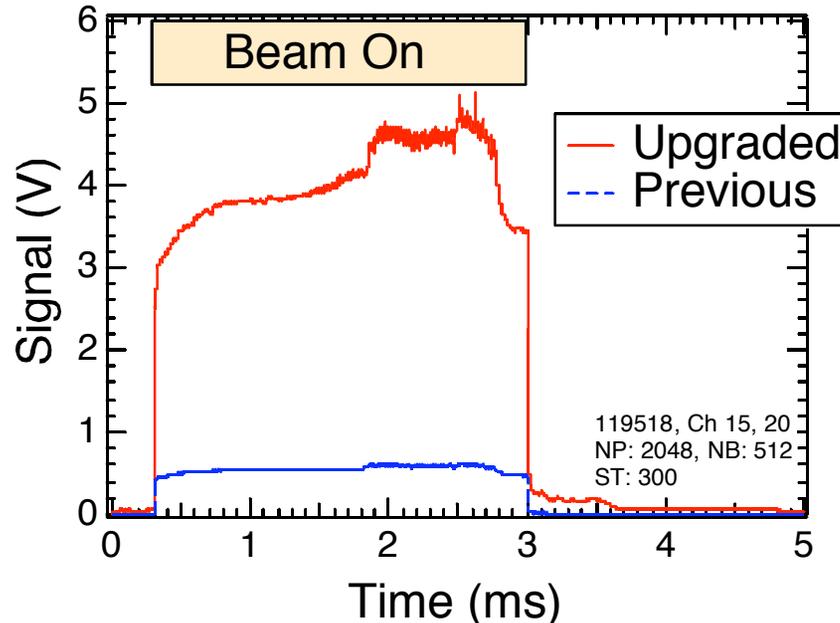
BEAM EMISSION SPECTROSCOPY MEASUREMENT OF LOCALIZED, LONG-WAVELENGTH ($k_{\perp}\rho_i < 1$) DENSITY FLUCTUATIONS

Collisionally-excited, Doppler-shifted neutral beam fluorescence



NUMEROUS DIAGNOSTIC ENHANCEMENTS YIELD SIGNIFICANT GAIN IN MEASURED SIGNAL

Parameter	Previous	Upgraded	Gain
1) Increased light collection:	0.59 mm ² -ster	1.62 mm ² -ster	2.75
2) Increased filter transmission	1.0	1.5 (w/D _α CX)	1.5
3) Larger photodiode detector	0.85 mm ²	2.9 mm ²	1.4
4) Higher reflectivity mirrors	0.94	0.98	1.05
Total 6+			

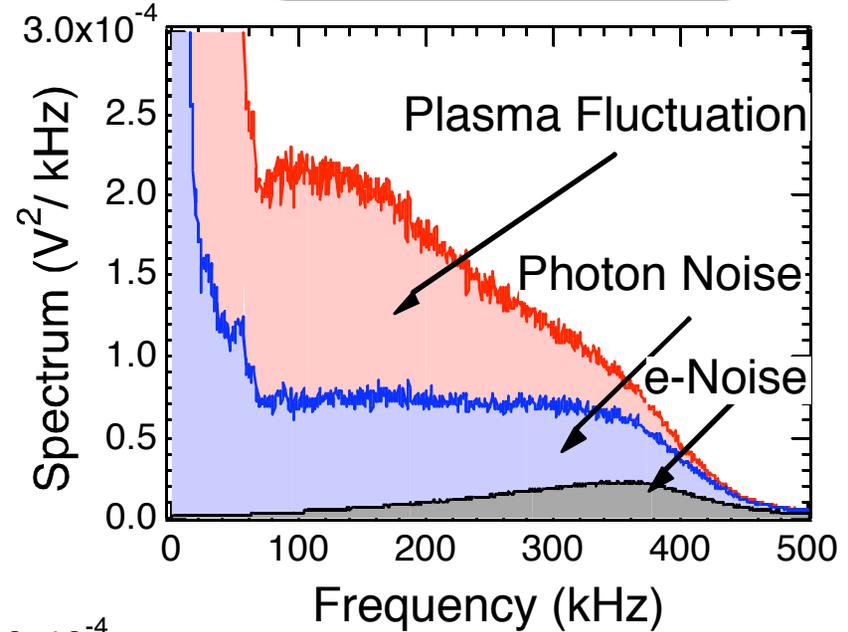
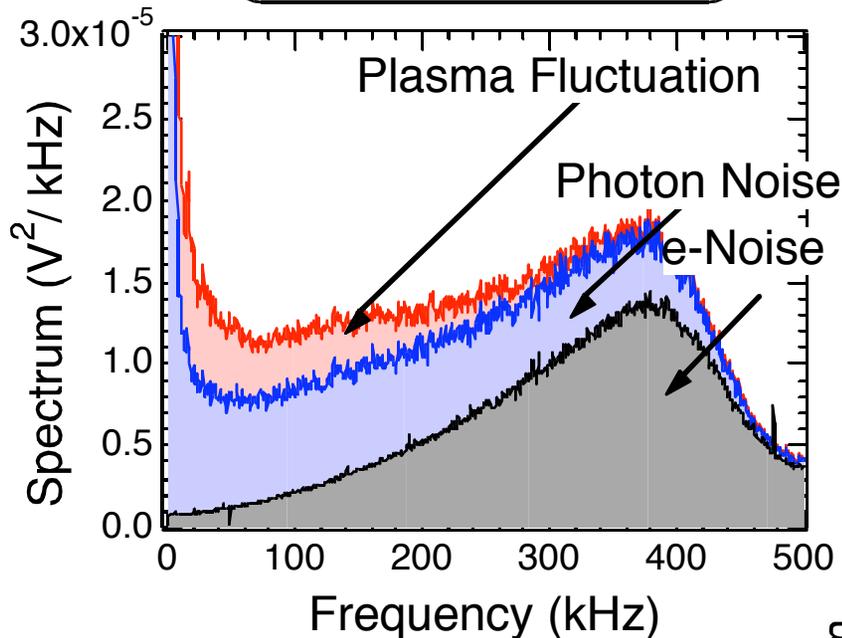


FACTOR OF 30-50 INCREASE IN SENSITIVITY TO PLASMA DENSITY FLUCTUATION POWER WITH UPGRADED BES SYSTEM

Previous BES

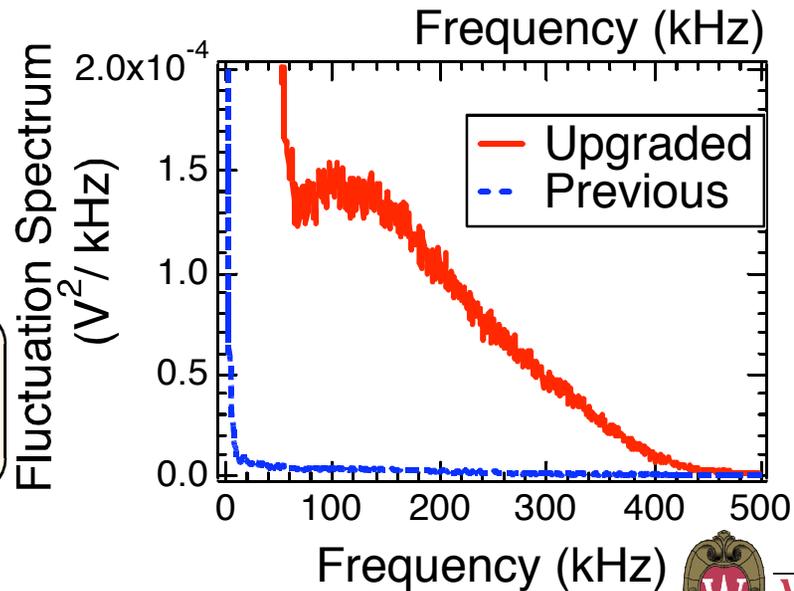
$r/a \sim 0.7$

Upgraded BES

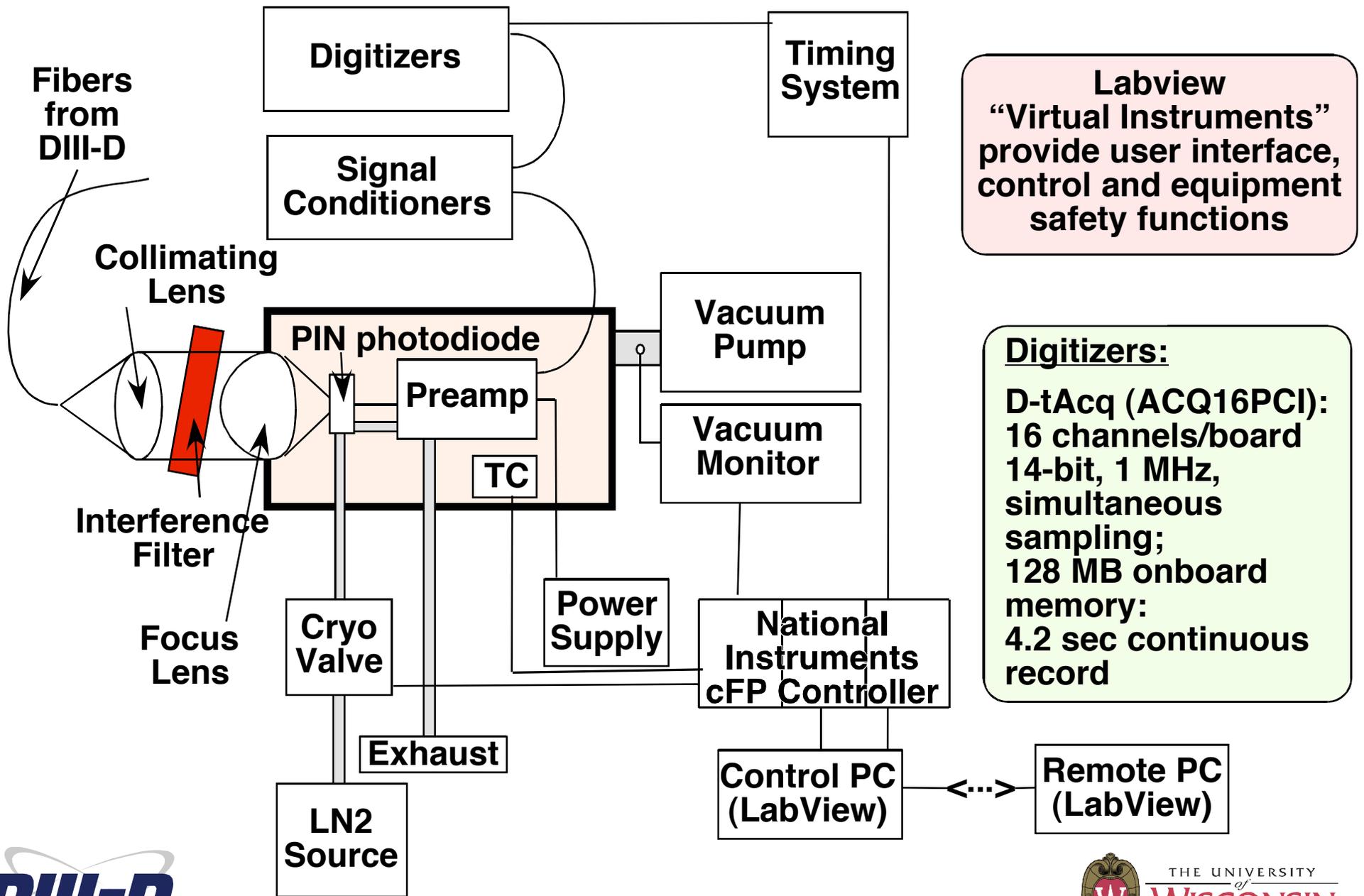


- e-Noise: x 1.7
- Photon Noise: x ~10
- Plasma Fluctuation: x ~40

Huge increase in plasma fluctuation power greatly facilitating studies of small-amplitude density fluctuations



BES DETECTOR AND CONTROL SYSTEM PROVIDES INTEGRATED CONTROL AND FULLY REMOTE OPERATIONS



OVERVIEW OF THE BEAM EMISSION SPECTROSCOPY SYSTEM

Fiber Optics

Cryogenic Lines, Manifold, Transfer Lines

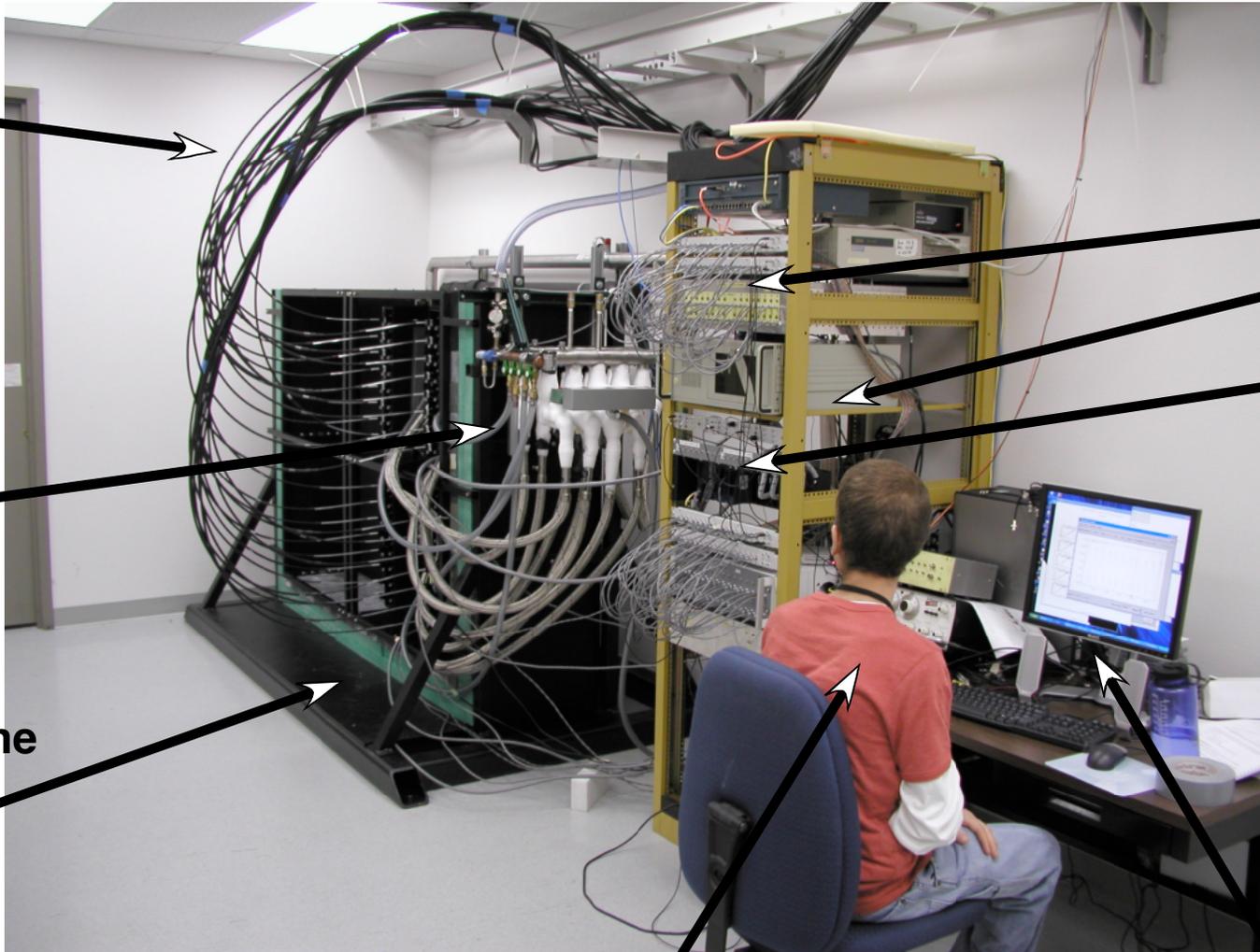
5-ton Pb & Borated Polyethylene Radiation Shield

Signal Conditioning Electronics, Amplifiers, Power Supplies

Digitizer (D-tAcq)

Control System (Regulates Temperature Monitors Vacuum, timing, AC Power National Instruments)

Control PC (Labview)

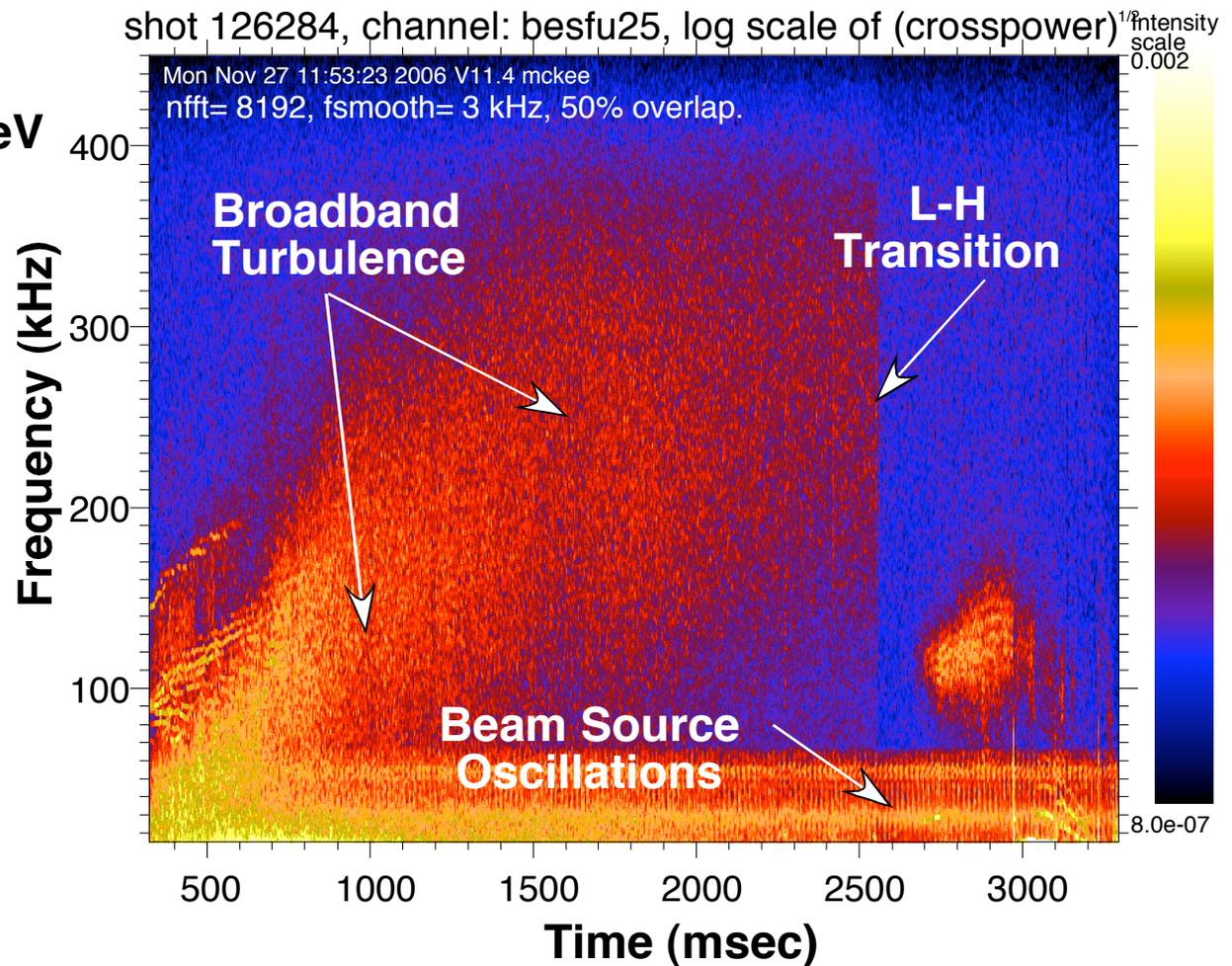


Dave, the Graduate Student

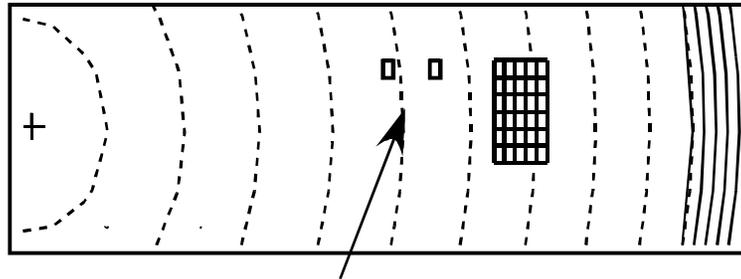
FLUCTUATION SPECTRUM EVOLVES DYNAMICALLY THROUGHOUT DISCHARGE

- Measurements obtained in L-mode Discharges:
 $I_p = 1 \text{ MA}$, $B_T = -2.0 \text{ T}$
 $P_{inj} = 5 \text{ MW}$,
 $n_{e,o} = 3 \times 10^{19} \text{ m}^{-3}$, $T_{e,o} = 2.2 \text{ keV}$
 $T_{i,o} = 2.7 \text{ keV}$
- Beam source oscillations arise from current or voltage noise in neutral beam source, small amplitude:
 $\tilde{n}_{BEAM}/n < 1\%$
- Common-mode rejection procedures can isolate and subtract

Cross-Power Spectrum at $r/a=0.64$ ($\Delta Z=1.2 \text{ cm}$)



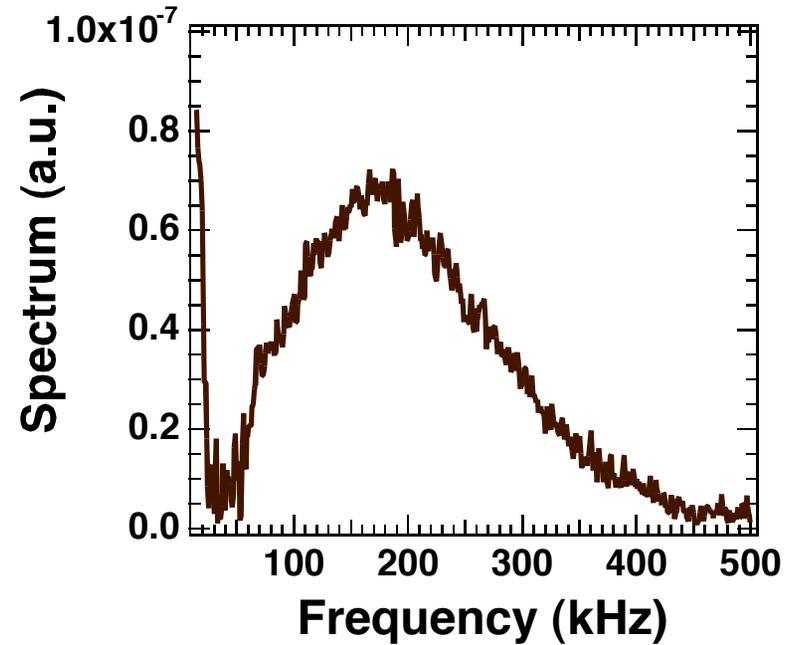
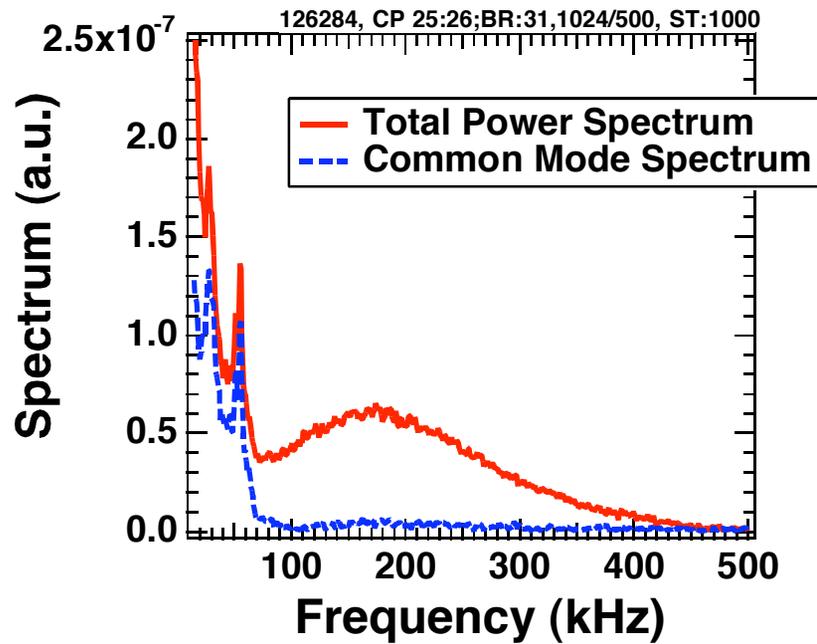
COMMON-MODE FLUCTUATIONS ARE MEASURED AND SUBTRACTED



Common-Mode Channels

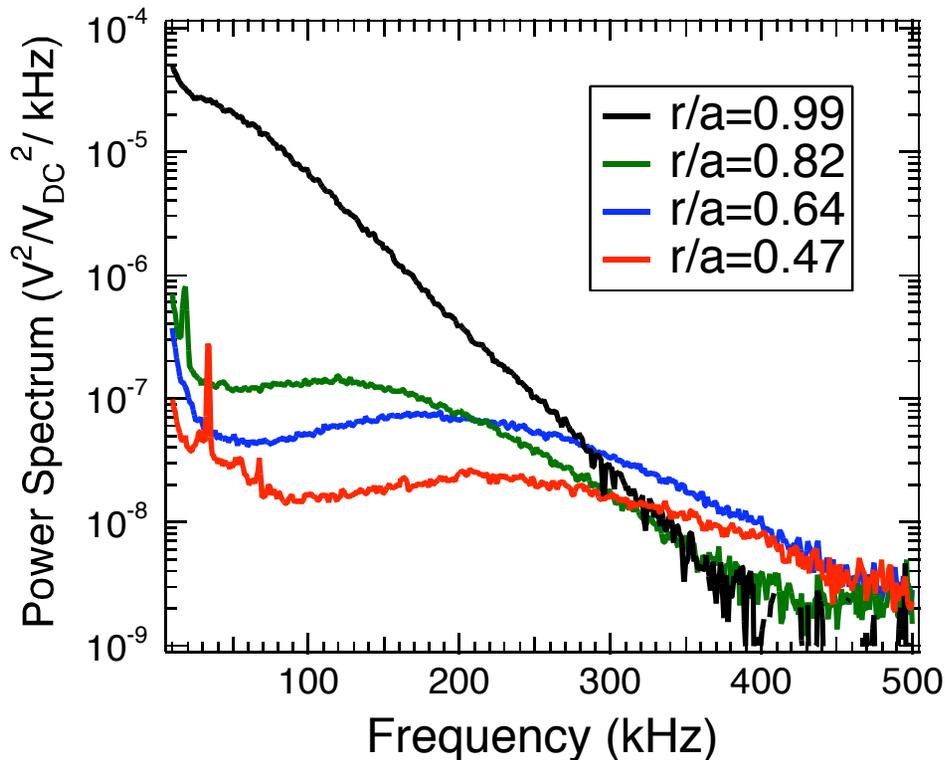
Power Spectrum has both local fluctuations and common-mode components

Local Spectrum after Subtraction of Common-Mode Signal

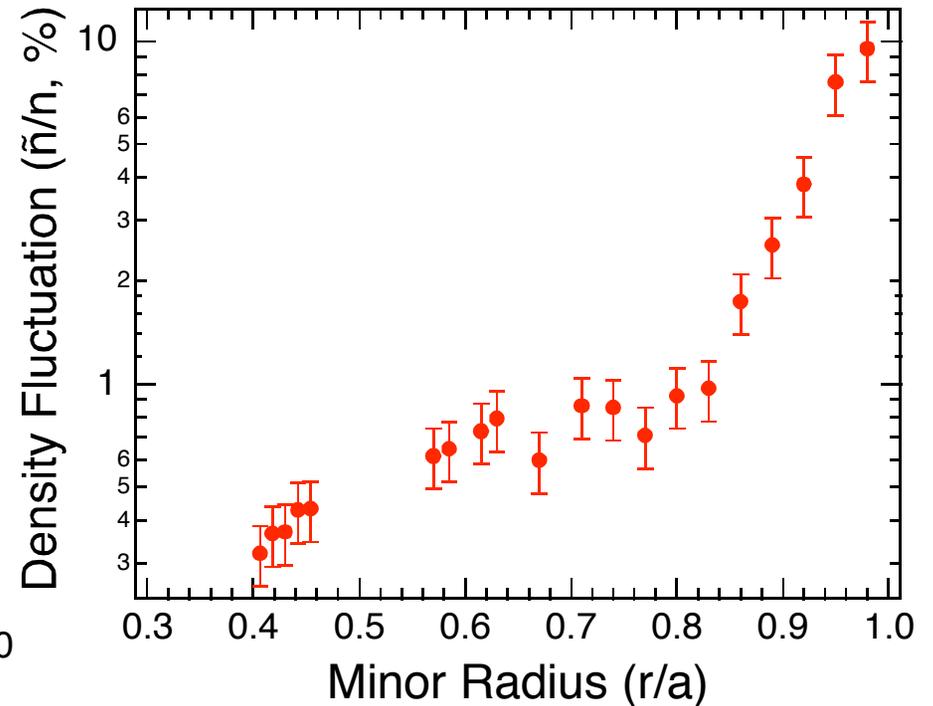


FLUCTUATION SPECTRA AND AMPLITUDE VARY STRONGLY WITH RADIUS

Fluctuation Spectra at Several Radii



Density Fluctuation Amplitude Profile



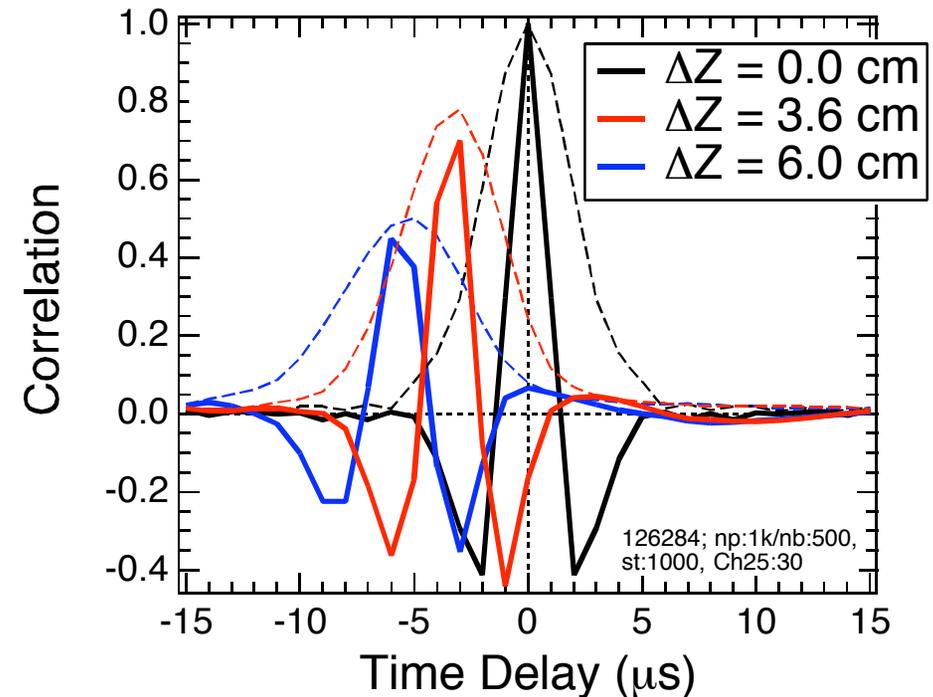
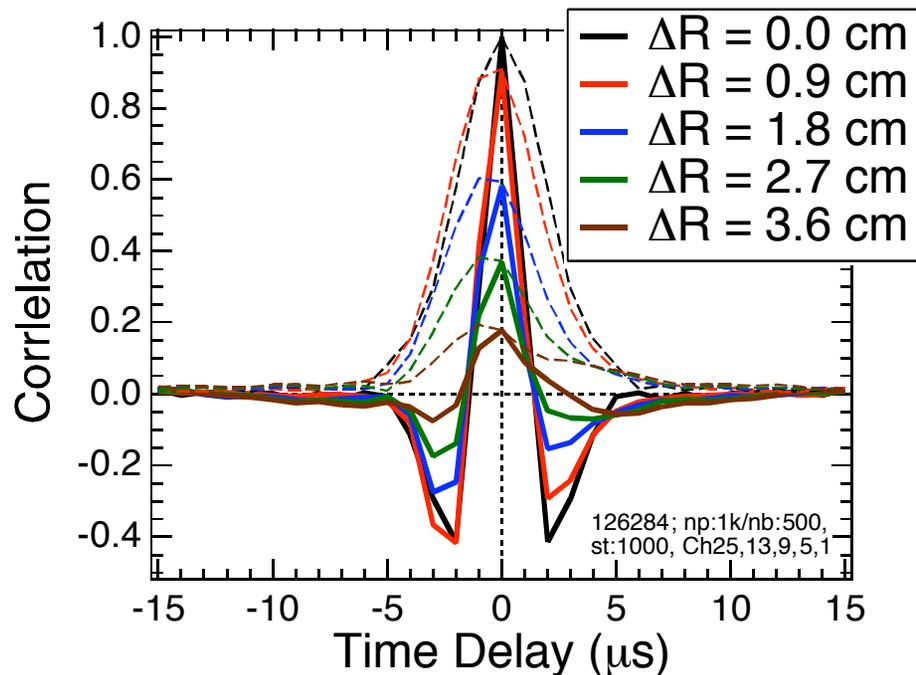
- Density fluctuation amplitude in L-mode discharges shows wide dynamic range across plasma radius
- Spectra strongly Doppler-shifted to higher frequency towards core

TIME-LAG CROSS CORRELATIONS EXHIBIT STRONG SPATIAL ASYMMETRY

Radial Cross Correlation Function

$r/a = 0.64$

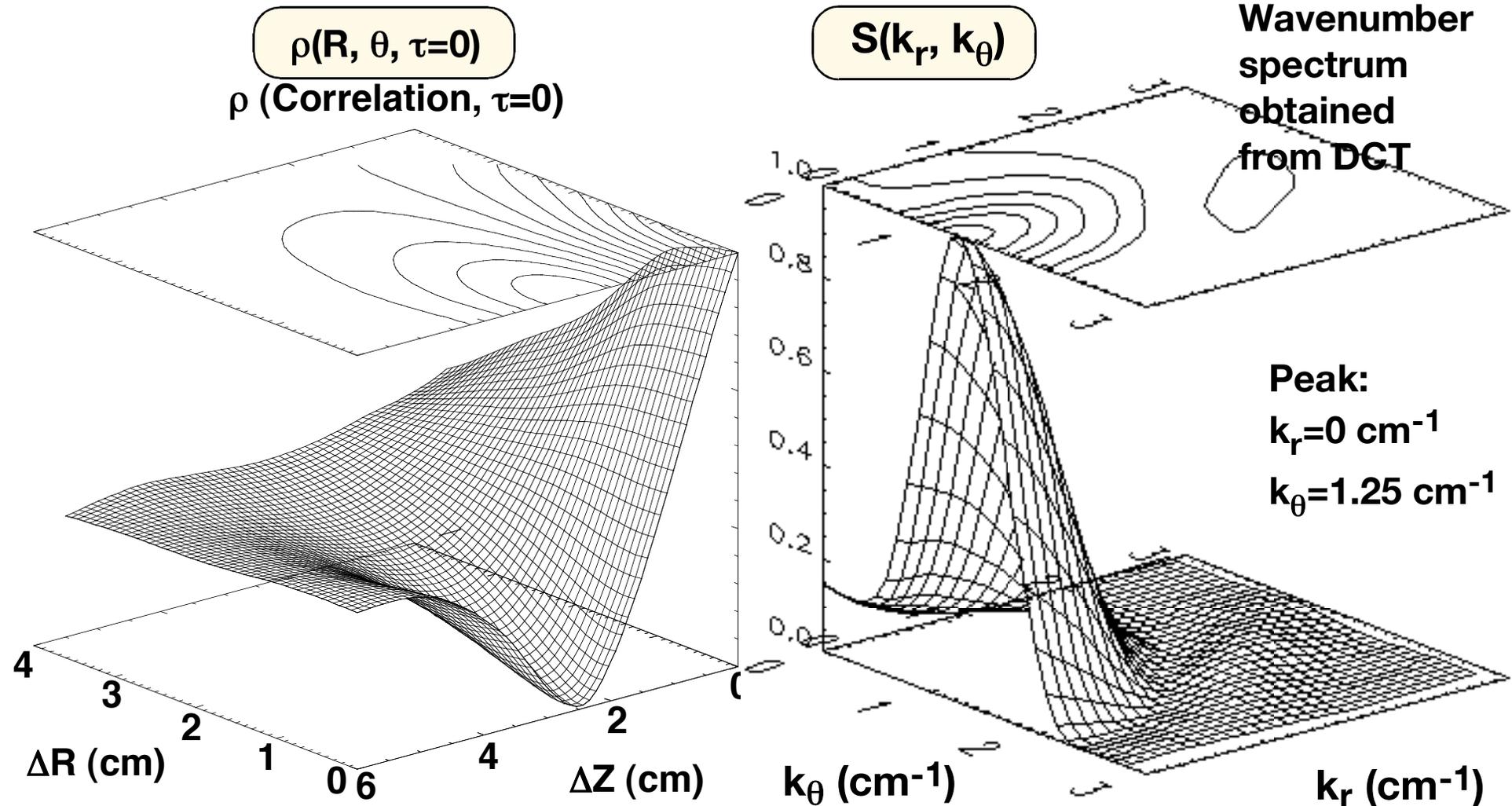
Poloidal Cross Correlation Function



- Turbulence has no time-averaged radial propagation, but strong poloidal propagation
- Poloidal correlation length slightly larger than radial:

$$L_{c,\theta} \approx 3.0 \text{ cm}, L_{c,r} \approx 2.5 \text{ cm}$$

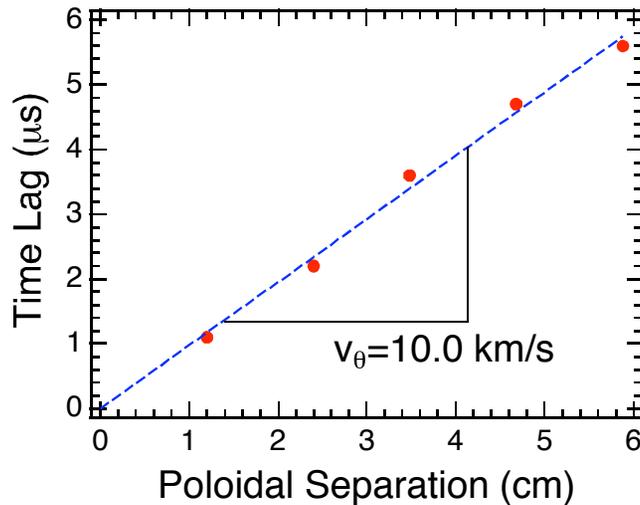
2D CORRELATION AND $S(k_r, k_\theta)$ SPECTRA CONFIRM SPATIAL ASYMMETRY



- Exhibits radially decaying, poloidally wavelike structure, $L_{c,\theta} > L_{c,r}$
- Wavenumber spectra can be compared with turbulence simulations

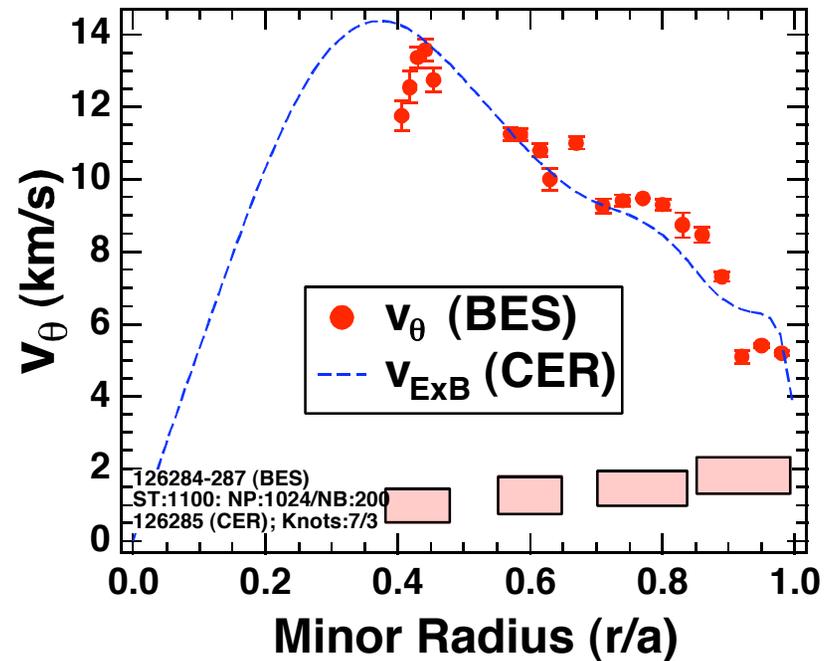
TURBULENCE ADVECTS POLOIDALLY AT LOCAL $E_r \times B_T$ VELOCITY

- Turbulence Velocity determined from poloidal cross-correlation time-lag analysis from BES



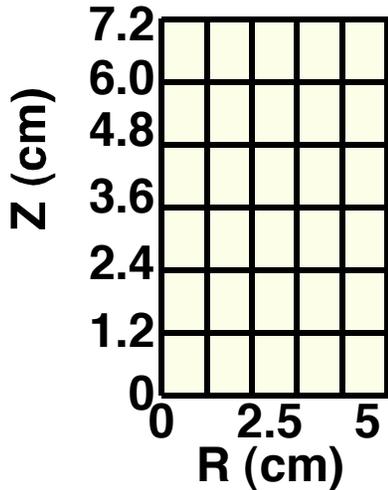
- V_{ExB} determined from ion radial force balance equation and Charge Exchange Recombination Spectroscopy measurements of carbon impurity toroidal and poloidal rotation, temperature and density

Poloidal Velocity from BES compared to V_{ExB} from CER

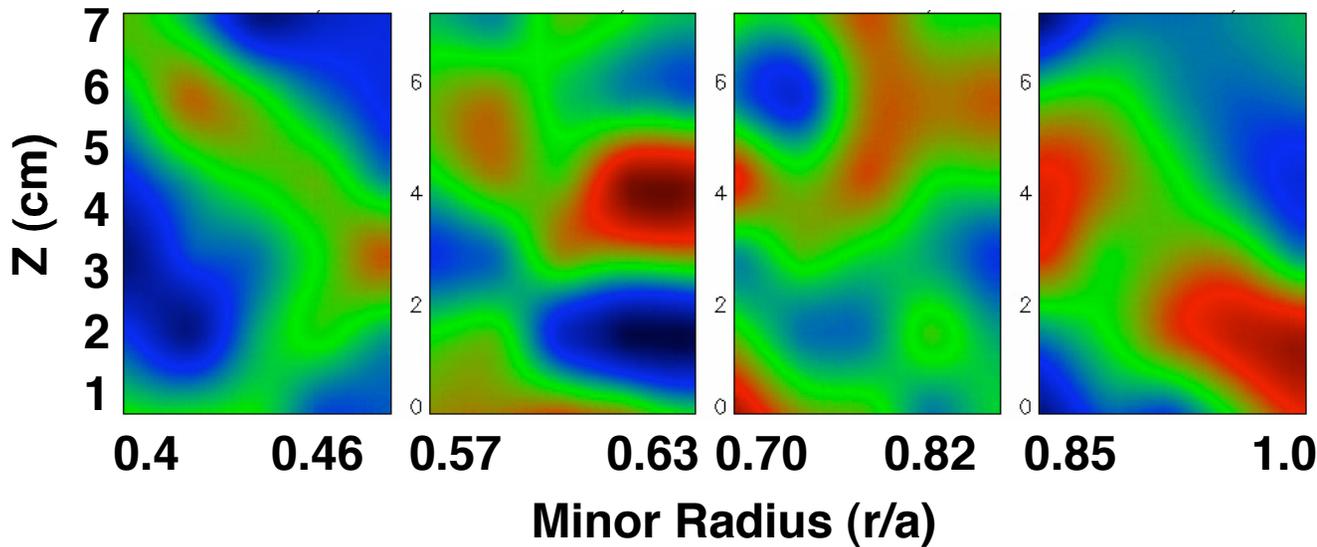


- Excellent agreement between independent measurements confirms that turbulence advection at ExB velocity

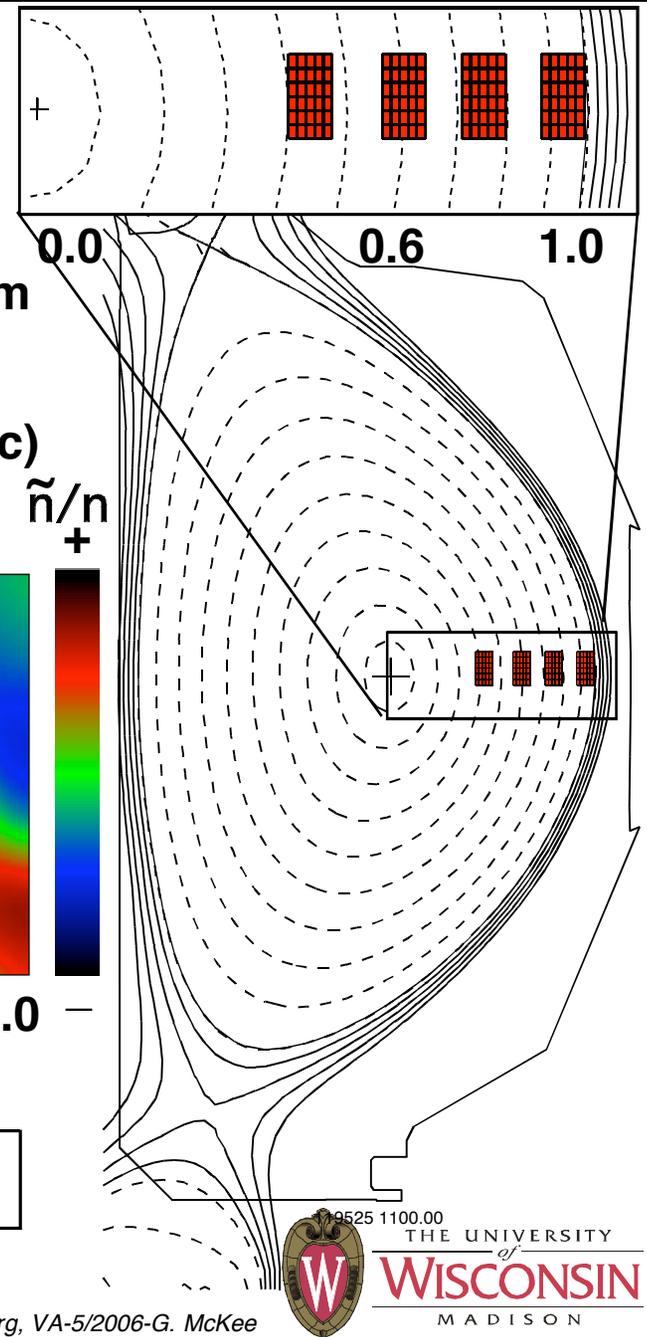
VISUALIZATIONS OF CORE PLASMA TURBULENCE OBTAINED WITH HIGH-SENSITIVITY BES SYSTEM ACROSS MINOR RADIUS



- 1 MHz sampling
- L-mode discharges (1.2 MA, 2.0 T, 5 MW NBI)
- Frequency-filtered per spectrum
- 2D spline
- 2×10^5 time dilation ($5 \mu\text{s} = 1 \text{ sec}$)



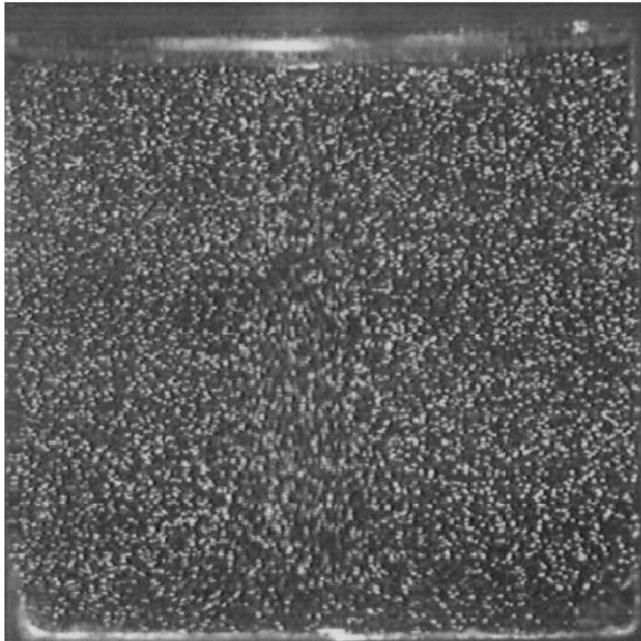
\tilde{n}/n	0.4%	0.7%	0.9%	2-10%
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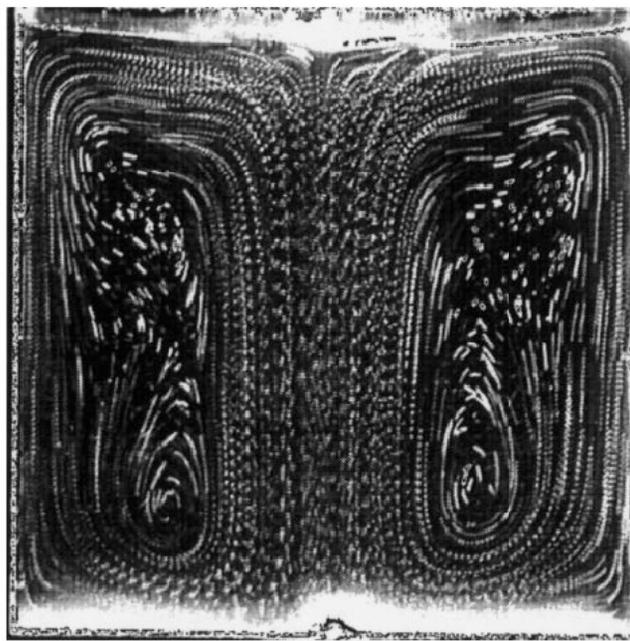
TIME-RESOLVED EDDY VELOCITY FIELD CAN BE DERIVED FROM MULTI-FRAME SPATIOTEMPORAL ANALYSIS

- Adapt technique from in fluid dynamics: *Orthogonal Dynamic Programming*
 - Reduces 2D problem to a set of selected 1D vector-matching problems
 - Utilizes “dynamic programming” to match patterns in related data sets
 - ODP then applies successive 1D matching techniques to full 2D data set, first in one dimension, then the other
 - Various optimization and tuning parameters
- Example output from application to PIV [1]:

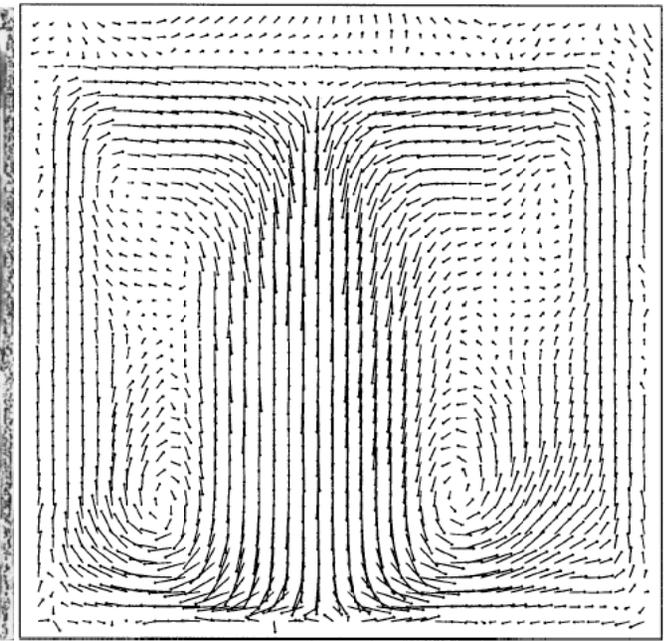
Single Image



Time-averaged Image



Calculated Flow Field



EXAMPLE SEQUENCE OF TIME-RESOLVED 2D TURBULENCE FLOW FIELD

**Analysis
Provides:**

$v_r(R, Z, t)$

- Flux

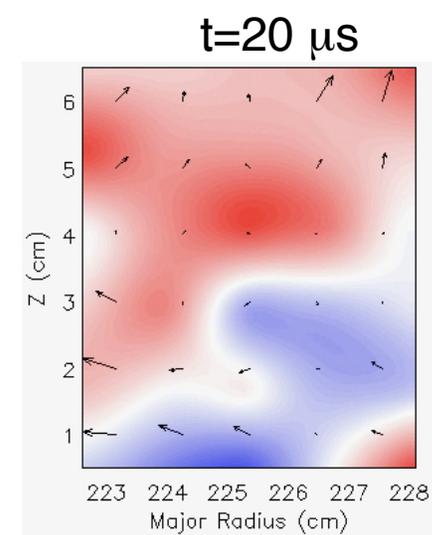
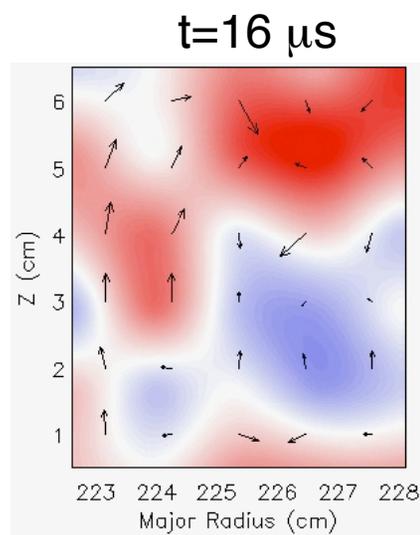
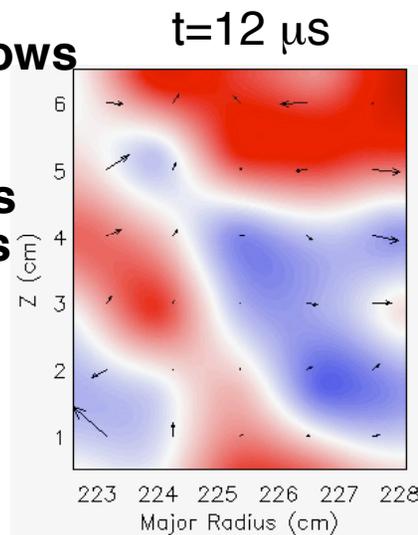
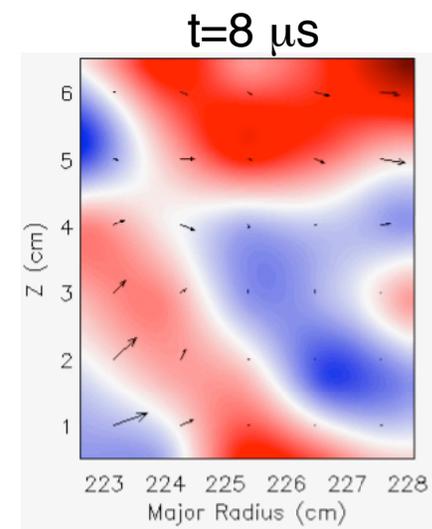
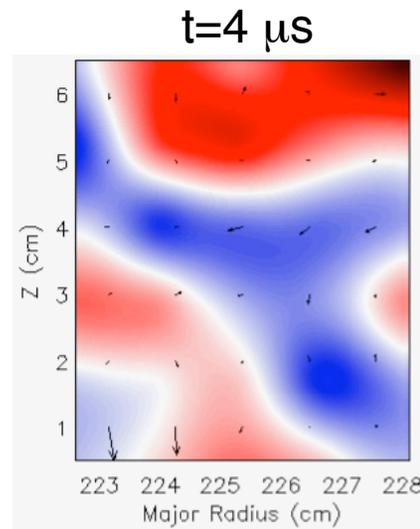
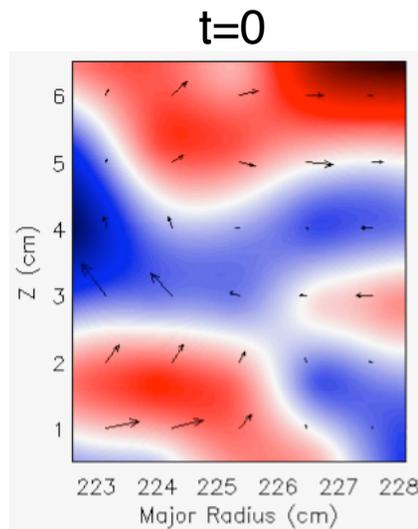
$v_\theta(R, Z, t)$

- Zonal Flows

R - 5 channels

Z - 6 channels

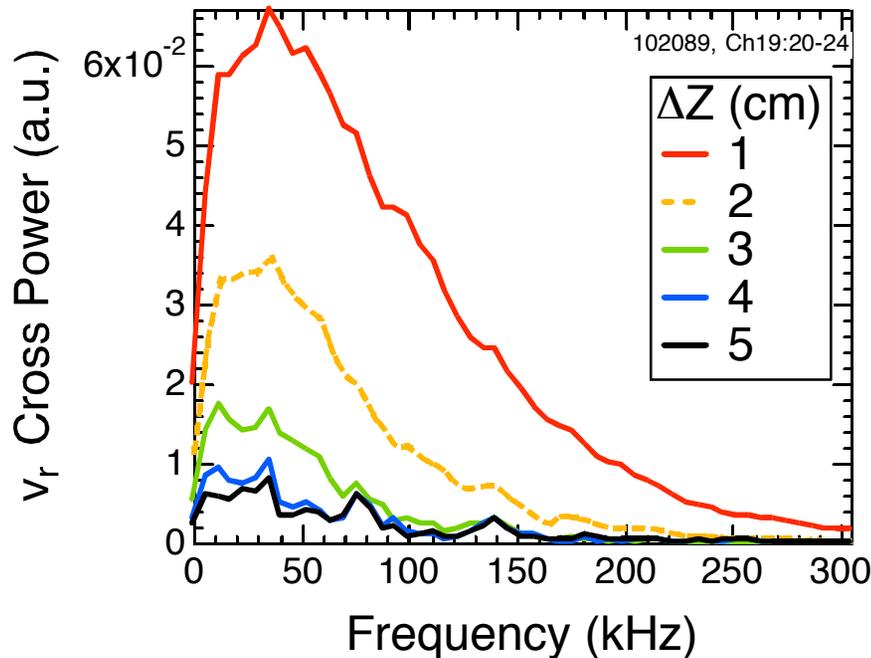
t - 1000 μ s



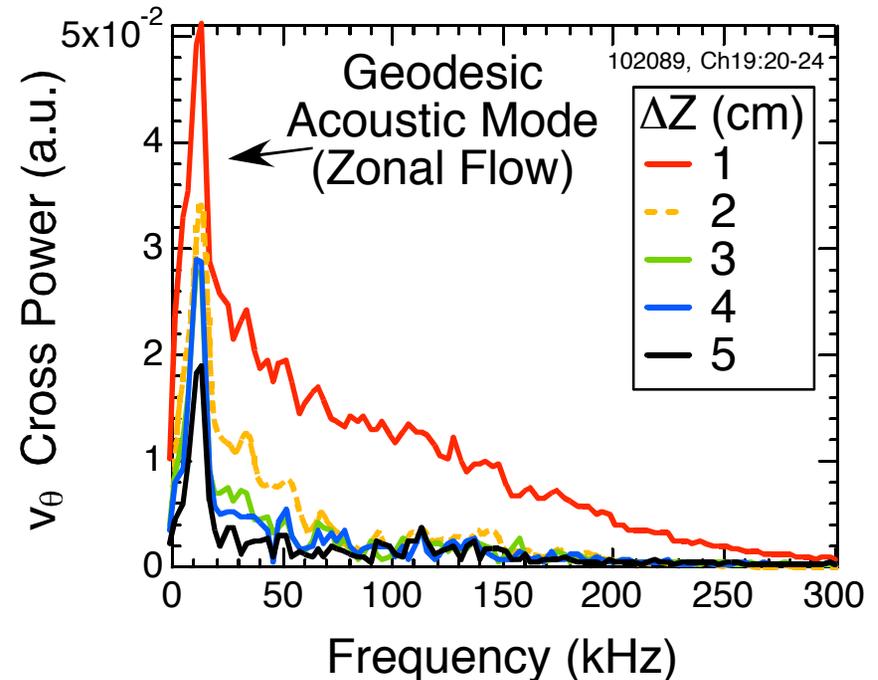
Vectors represent local velocity field (scaled by image)

RADIAL AND POLOIDAL VELOCITY FLUCTUATIONS EXHIBIT DISTINCT BROADBAND SPECTRA

Radial Velocity Spectra



Poloidal Velocity Spectra



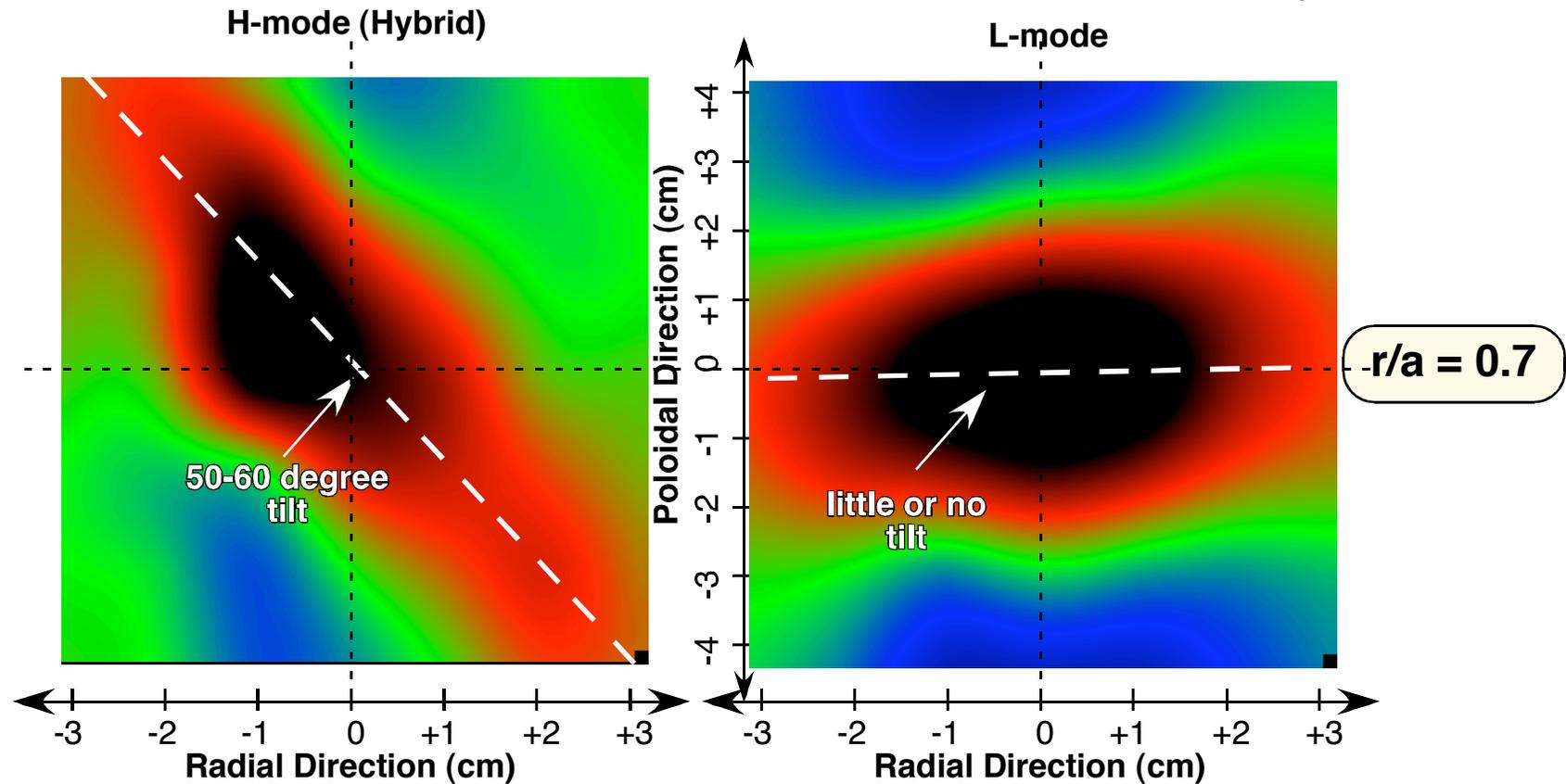
- Decaying spatial coherence indicates velocity fluctuations have few cm correlation length, similar to density fluctuations
- Spatially increasing phase shift suggests poloidal advection (not shown)
- GAM shows clearly in v_θ , not in v_r : zero poloidal phase shift, $2\pi f = c_s/R$

How are \tilde{v} related to $\tilde{\phi}$ (through $\tilde{E} \times B$)?

SPATIOTEMPORAL CROSS-CORRELATIONS REVEAL SIGNIFICANT DIFFERENCES IN L-MODE & H-MODE TURBULENCE STRUCTURES

2D Spatial Correlation Function ($\Delta\tau = 0$)
in (Hybrid) H-mode Discharge

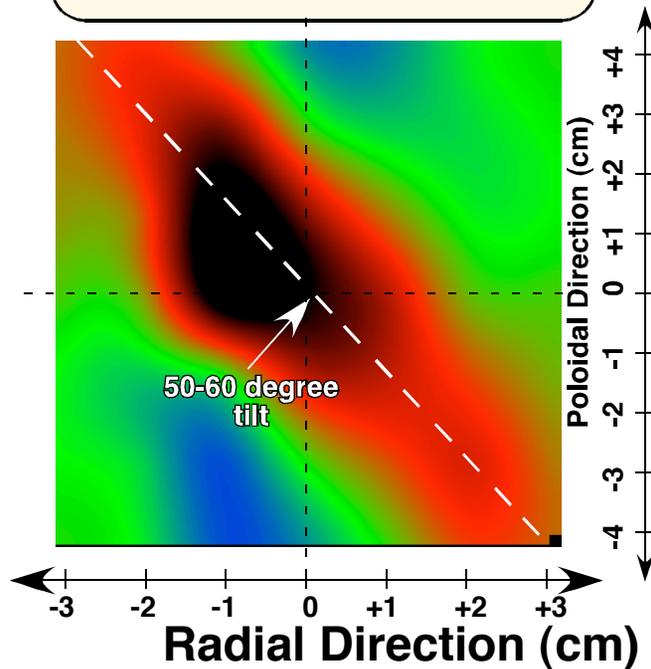
Time-resolved correlation function:
 $\rho(\Delta r, \Delta\theta, \Delta\tau)$



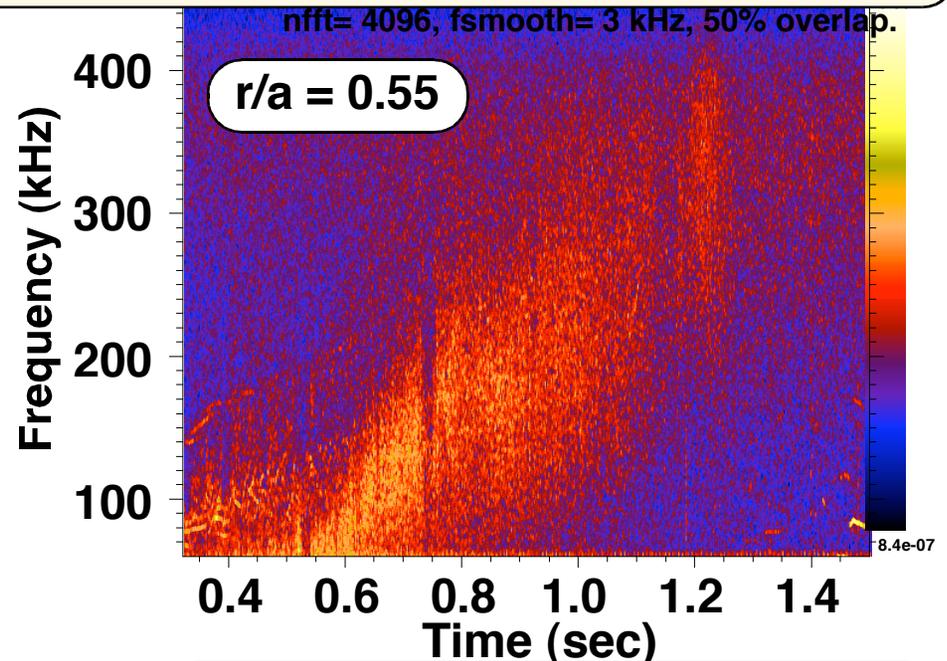
- Suggests core H-mode turbulence subject to stronger flow shear: amplitude is significantly lower (~ 10)

STUDIES OF SMALL-SCALE, LOW-AMPLITUDE PLASMA INSTABILITIES BENEFIT FROM LOCAL, HIGH-SENSITIVITY FLUCTUATION MEASUREMENTS

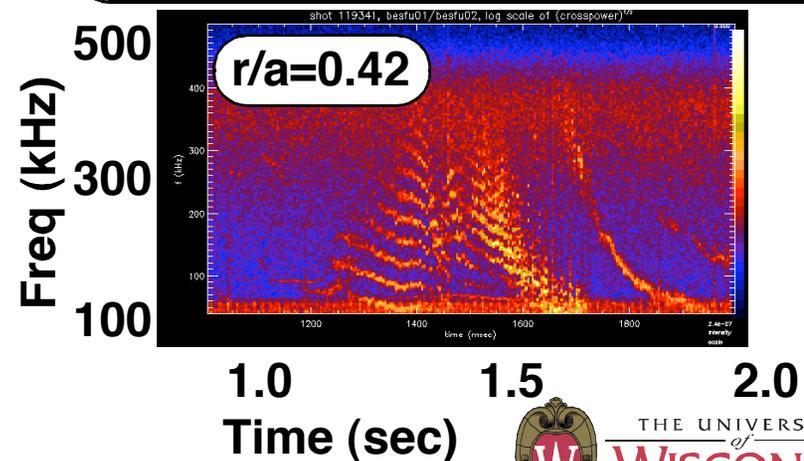
Turbulent Eddy Spatial Correlation in H-mode Plasmas



Turbulence Dynamics During ITB Formation



Energetic Particle-Driven Modes



Example measurements obtained in the core of DIII-D Tokamak Plasmas with the upgraded High-Sensitivity Beam Emission Spectroscopy System



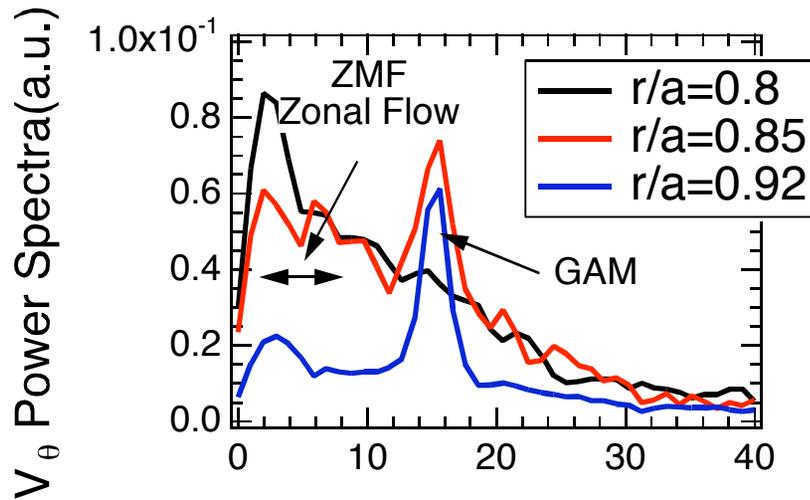
$$\tilde{n}/n < 1\%$$



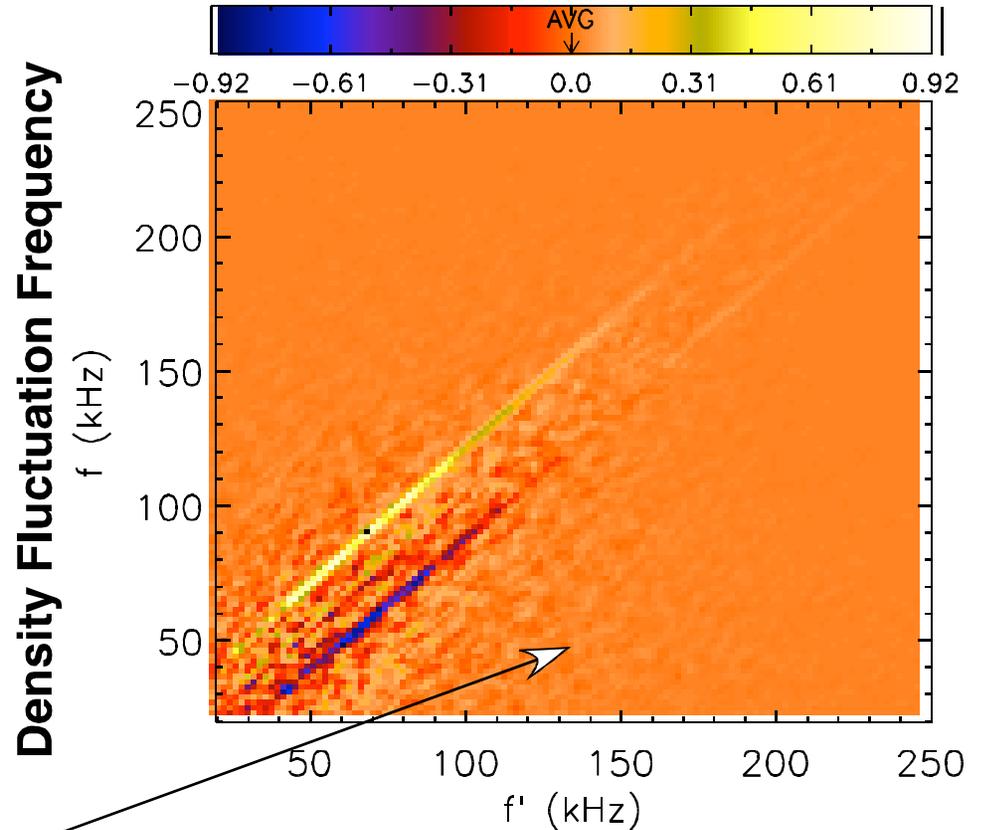
ANALYSIS OF 2D TURBULENCE MEASUREMENTS ALLOWS FOR INVESTIGATION OF COMPLEX AND NONLINEAR DYNAMICS

Zonal Flows, include Geodesic Acoustic Modes are manifest in high frequency poloidal velocity fluctuations, measured via application of “Time-Delay-Estimation” methods to BES data

$$T_n^Y(f', f) = -\text{Re} \left\langle n^*(f) V_y(f - f') \frac{\partial n}{\partial y}(f') \right\rangle$$



GAM mediates nonlinear transfer of energy from low frequencies to high frequencies in tokamak edge plasma



Poloidal Density Gradient Fluctuation Frequency

CONCLUSIONS & FUTURE DIRECTIONS

- **Beam Emission Spectroscopy deployed at DIII-D provides time-resolved visualizations of plasma turbulence in the R-Z plane**
 - *Allowing for detailed characterization of inherently 2D turbulence in magnetically-confined plasmas*
- **Beam Emission Spectroscopy at DIII-D has been redesigned, component-by-component to provide high-sensitivity 2D measurements:**
 - *Increased light collection*
 - *Higher transmission filter*
 - *Larger area photodiode*
 - *Net 5-10* increase in measured signal*
 - *Advanced control system, expanded lab facility*
- **Sensitivity to small-amplitude fluctuation power increased by 30-50**
- **Now provides density fluctuation measurements in the core region ($0.25 < r/a < 1.0$) of L & H modes (L, H-mode, QH, QDB, Hybrid, AT)**
 - *Turbulence and energetic particle-driven modes*
- **High SNR data and advanced analysis enables study of:**
 - *Zonal flow/Geodesic Acoustic Mode (GAM)*
 - *Velocimetry (potential fluctuations, turbulent particle flux)*
 - *Nonlinear: energy transfer, cascades*

