Density Regime of Complete Detachment and Operational Density Limit in LHD

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Abstract. The highest central density in net current free helical plasmas of $5 \times 10^{20}$ m$^{-3}$ has been demonstrated in the recent Large Helical Device (LHD) experiment. The volume-averaged electron density reaches $3 \times 10^{20}$ m$^{-3}$, in spite of a small power density of less than 0.5 MW/m$^3$ and a magnetic field strength of less than 3 T. These are attained in the plasmas with strongly peaked density profiles generated by pellet injection. In the case of gas-fueled plasmas, complete detachment takes place when the hot plasma boundary shrinks below the last-closed-flux-surface (LCFS), or in other words, the edge temperature decreases to a critical value. The edge density that results in this shrinking corresponds to the maximum edge density achievable under the attached condition. At detachment, the ionization front moves from the ergodic region to inside of the LCFS and the particle confinement effectively improves. Under an appropriate recycling condition, complete detachment is self-sustained, which is called the Serpens mode. The discharge is finally terminated by radiating collapse, unless gas fueling is stopped. Radiating collapse is triggered even at a small radiation loss fraction of about 0.3, while it ranges from 0.3 to 1 at complete detachment. It is therefore difficult to determine a threshold radiation loss fraction that determines the operational density limit. Both of the critical densities for complete detachment and radiating collapse are dependent on the square root of the heating power, as is predicted by the conventional Sudo density limit scaling. This is explained by the edge temperature property that is a function of the square root of the heating power divided by the density, i.e. the density that results in a critical temperature increases with the square root of the heating power. Even though the Sudo fraction, which is the ratio of the volume-averaged density to the Sudo scaling, reaches as high as 3.5 in pellet-fueled plasmas, the edge density in these cases are similar to those in gas-fueled plasmas of which the Sudo fraction is ~0.8 at attachment. Indeed, the Sudo fraction is proportional to the peaking factor defined by the ratio of the volume-averaged density to the edge density, which exceeds 3 in pellet-fueled plasmas. In detached plasmas, edge densities are roughly twice as large as those in attached plasmas, reflecting the improved particle confinement.

1. Introduction

The operational density range in future magnetically confined deuterium-tritium fusion reactors will be of the order $10^{20}$ m$^{-3}$ [1, 2]. Higher density is more favorable as long as the confinement property is maintained, since the fusion reaction rate increases with the density squared. Furthermore, high-density operation is effective to achieve detachment [3], which reduces the divertor heat load to permissible value for realistic materials, since the edge plasma temperature decreases due to dilution cooling together with enhanced radiation and charge-exchange losses at high-density.

High-density operation of the order $10^{20}$ m$^{-3}$ has been carried out mainly in small or medium size devices, such as the Alcator C-Mod tokamak (C-Mod) [4], the Frascati Tokamak Upgrade (FTU) [5], and the Wendelstein 7-AS stellarator (W7-AS) [6]. Small plasma volume and resultant high heating power density in these small devices, and especially the high magnetic field strength up to 8 T in C-Mod and FTU are apparently helpful for high-density operation. In the case of W7-AS, high-density up to $4 \times 10^{20}$ m$^{-3}$ was attained with divertor...
detachment, in spite of a low magnetic field strength of 2.5 T [6]. The heating power density was \( \leq 4 \text{ MW/m}^3 \) in W7-AS. In the Large Helical Device (LHD), on the other hand, the heating power density is less than 0.5 MW/m\(^3\) and the magnetic field strength is less than 3 T, to date. To discuss a possibility of high-density operation in a future fusion reactor, it is necessary to construct a reliable operational density limit scaling that at least explains the experimental results of various existing devices.

The so-called Sudo density limit scaling [7] has been often used to discuss the operational density limit of helical plasmas. The Sudo scaling is defined by; \( n_e^{\text{Sudo}} (10^{20} \text{ m}^{-3}) = 0.25 (PB/(a^2R))^{0.5} \), where \( P \) (MW), \( B \) (T), \( a \) (m) and \( R \) (m) are the total heating power \( (P_{\text{tot}}) \), the magnetic field strength on the magnetic axis, the minor radius and the major radius, respectively [7]. It should be noted that strongly peaked density profiles are not in the scope of Sudo scaling. This scaling is based on the power balance between the heating power and the radiation loss that is proportional to \( n_e^2 \), where \( n_e \) is the electron density. In LHD, radiating collapse is triggered even at a small radiation loss fraction of \( \sim 30 \% \) [8]. Sustainable complete detachment, named the Serpens mode, has been found in LHD [9]. The radiation loss fraction ranges from 30 to 100 \% at complete detachment [10]. It is therefore difficult to determine a threshold radiation loss fraction that triggers radiating collapse. The temperature dependence of the thermal diffusivity changes from strong \( (\chi_{\text{eff}} \propto T_e^{1.5}) \), gyro-Bohm type to weak \( (\chi_{\text{eff}} \propto T_e^{0.5}) \) at a density much less than the operational density limit [11], where \( T_e \) and \( \chi_{\text{eff}} \) denote the electron temperature and the effective thermal diffusivity, respectively. The plasma stored energy is proportional to \( <P_{\text{dep}}^{2/3} > n_e^{1/2} \) in the latter case (HD scaling [11]), where \( <P_{\text{dep}} > \) is the volume-average of the integrated heat deposition profile. It is necessary to use \( <P_{\text{dep}} > \sim P_{\text{tot}} \times \exp(-<n_e>/12) \), for plasmas with a flat density profile at \( <n_e> > 3 \times 10^{19} \text{ m}^{-3} \) [9], to take into account the shallow penetration of the heating beams in high-density plasmas.

In this study, we experimentally investigate the operational density limit in LHD. Recent results of high-density experiments performed in LHD are given in Section 2. Density regimes for complete detachment and the operational density limit are also given. In Section 3, edge plasma parameters are highlighted to discuss plasma behavior in the vicinity of the operational density limit. A summary is given in Section 4.

2. High-density plasmas in LHD

2.1. Pellet-fueled plasmas

The highest volume-averaged density, \( <n_e> \), in LHD has reached \( 3 \times 10^{20} \text{ m}^{-3} \), in the latest experimental campaign. Waveforms of the highest \( <n_e> \) discharge are depicted in FIG. 1. This was obtained at an inward-shifted configuration, where the magnetic axis, \( R_{\text{ax}} = 3.65 \text{ m} \) and the magnetic field strength on the magnetic axis, \( B_0 = 2.71 \text{ T} \). Eight hydrogen ice pellets are injected from \( t = 0.7 \) to 1 s. Both the line-averaged electron density measured by a CO\(_2\) laser interferometer, of which the line-of-sight passes through the core region of \( \rho = 0.06 \) (\( \rho \) is the normalized minor radius), and \( <n_e> \) measured by Thomson scattering reach \( 3 \times 10^{20} \text{ m}^{-3} \) at \( t \sim 1 \text{ s} \). Since the absolute sensitivity of each channel of Thomson scattering has not yet been calibrated, all Thomson density signals are multiplied by a single calibration factor to match \( <n_e> \) with that estimated from the Abel inversion of far-infrared (FIR) multi-chord interferometer signals. The electron density profile at the peak timing is shown in FIG. 2, together with the electron temperature and pressure profiles. The temperature profile becomes hollow transiently, just after the pellet injection that strongly peaks the density profile. The resultant pressure profile is flat in the core region of \( \rho < 0.7 \).
The highest central density, \( n_{e0} \), of \( 5 \times 10^{20} \) m\(^{-3} \), as shown in FIGs 3 and 4, was achieved at an outward-shifted configuration, where \( R_{\text{ax}} = 3.75 \) m and \( B_0 = 2.64 \) T. This is the world record in helical plasmas including heliotrons and stellarators. Hydrogen ice pellet injection was also used in this case. After the pellet injection, the electron density decreases and the electron temperature increases. The diamagnetic stored energy, \( W_p^{\text{dia}} \), increases in this phase, as is known as reheat. In this case, the superdense core (SDC) [12] is formed after \( t \sim 1.2 \) s. Central plasma pressure reaches 100 kPa (the ion temperature, \( T_i \), and the ion density, \( n_i \), are assumed to be equal to \( T_e \) and \( n_e \), respectively). This is also the world record in helical plasmas. A large Shafranov shift from 3.75 m to 4 m is observed at the SDC phase. Although SDC has been first found in the Local Island Divertor (LID) configuration [12], where \( n_{e0} \sim 5 \times 10^{20} \) m\(^{-3} \) has also been attained, it is possible to form SDC in the usual helical divertor configuration, as in the case of FIGs 3 and 4.
2.2. Gas-fueled plasmas

Detachment in LHD proceeds as in FIG. 5, where the density is increased by strong hydrogen gas puffing at a constant flow rate of $\Phi_{\text{puff}} \sim 200 \text{ Pa m}^3/\text{s}$ ($R_{\text{ax}} = 3.65 \text{ m}$ and $B_0 = 2.71 \text{ T}$, $P_{\text{tot}} = 8.3 \text{ MW}$). Then, the ion saturation current measured on the divertor tiles in the gas puff port, $I_{\text{sat}}$, decreases while it continues to increase with the density at the opposite side of the torus ($I_{\text{sat}}$). We refer to this as transient partial detachment. The hot plasma boundary, $\rho_{100eV}$, given as the normalized minor radius where $T_e = 100 \pm 50 \text{ eV}$, gradually decreases during the transient partial detachment phase. The reason why $\rho_{100eV}$ is highlighted as the hot plasma boundary will be explained in Section 3. When $\rho_{100eV}$ decreases to 1, complete detachment takes place and $I_{\text{sat}}$ begins to decrease at all the measured divertor tiles. In contrast to tokamaks, but similar to W7-AS, there are no clear indications of high recycling prior to detachment. The penetration of the heating beam becomes shallow and both $<P_{\text{dep}}>$ and $W_p^{\text{dia}}$ decrease as $<n_e>$ increases. Nevertheless, $W_p^{\text{dia}}$ is well reproduced by the HD scaling even at complete detachment [9]. As the edge $T_e$ decreases, hydrogen volume recombination takes place [10] and the ionization front moves from the ergodic region to inside the last-closed-flux-surface (LCFS). The effective fueling efficiency for neutral particles is improved at complete detachment. This reflects the better particle confinement inside the LCFS, where particle diffusion perpendicular to the flux surfaces is important, compared with that in the ergodic region, where parallel particle transport through the open field lines dominates. Indeed, the density ramp up rate increases at $t \sim 1.15 \text{ s}$ in FIG. 5, even though $\Phi_{\text{puff}}$ is unchanged. To avoid an excess of density increase that leads to radiating collapse, it is necessary to decrease the fueling rate. Therefore, the density that results in $\rho_{100eV} = 1$ corresponds to the maximum density achievable under the attached condition. It is possible to increase the density further...
beyond this critical density, under the completely detached condition. The Serpens mode begins when $\rho_{100eV}$ decreases to ~0.9, and fluctuations due to a rotating helical radiation belt, named the serpent, appear in $I_{\text{sat}}$. In contrast to the Marfe observed in W7-AS, the serpent follows the magnetic field lines and is continuously propagating in both the poloidal and toroidal directions. In the Serpens mode phase, $I_{\text{sat}}$ normalized by the main plasma density decreases to 10% of the attached phase [9].

### 2.3. Density regimes of complete detachment and radiating collapse

Pellet injection is indeed effective to achieve a high-density. As is shown in FIG. 6, pellet-fueled plasmas are characterized by a strongly peaked density profile. In gas-fueled plasmas including detached and Serpens mode plasmas, the density profile is hollow or flat. However, even in pellet-fueled plasmas, edge densities are similar to those in gas-fueled plasmas. In FIG. 7, $<n_e>$ and the edge electron density, $n_e^{100eV}$, given by the electron density at $\rho_{100eV}$, are plotted against $P_{\text{tot}}$, for the case of $R_{\text{ax}} = 3.65$ m and $B_0 = 2.71$ T. Shaded regions denote the density regimes for complete detachment. The $n_e^{\text{Sudo}}$ plotted in FIG. 7 is calculated using the fixed parameters of $a = a_0 = 0.64$ m, $R = R_{\text{ax}} = 3.65$ m, and $B = B_0 = 2.71$ T. High-density reaching $2.2 n_e^{\text{Sudo}}$ is sustainable in the Serpens mode plasmas. Higher densities as high as $3.5 n_e^{\text{Sudo}}$ are achieved by applying pellet injection, although these are transient. Even in these pellet-fueled plasmas, however, $n_e^{100eV}$ are similar to those obtained in gas-fueled plasmas.

The high $<n_e>$ achieved in pellet-fueled plasmas are the result of the strongly peaked density profiles, as shown in FIG. 8, where Sudo fraction defined by $<n_e>/n_e^{\text{Sudo}}$ is plotted against a peaking factor defined by $<n_e>/n_e^{100eV}$. In this case, $n_e^{\text{Sudo}}$ is calculated using $a = a_0 \rho_{100eV}$, to take into account the shrinking minor radius, while $R = 3.65$ m, and $B = 2.71$ T are fixed. The Sudo fraction linearly increases with the peaking factor, which exceeds 3 in pellet-fueled plasmas. In detached plasmas of which $\rho_{100eV} < 1$, $n_e^{100eV}$ are larger than in the attached plasmas of which $\rho_{100eV} \sim 1$.
3. Critical edge density

3.1. Electron temperature dependence on total heating power and density

As was mentioned in the introduction, the Sudo scaling is based on the power balance between $P_{\text{tot}}$ and $P_{\text{rad}}$ that is proportional to $n_e^2$, i.e. it is assumed that radiating collapse takes place at a critical radiation loss fraction of $P_{\text{rad}} / P_{\text{tot}} \propto n_e^2 / P_{\text{tot}}$, and therefore, the critical density is proportional to $P_{\text{tot}}^{-0.5}$. However, a large scatter of radiation loss fraction that ranges from 30 to 100% at detachment suggests that this scenario is not sufficient to explain the density limit in LHD. Nevertheless, the threshold edge density for complete detachment does increase with $P_{\text{tot}}^{-0.5}$ (see FIG. 7), as in the Sudo scaling. For a better understanding on this, the dependence of temperature on heating power and density is investigated.

The results of linear regression analysis of $T_e$ for attached plasmas ($\rho_{100eV} > 1$) are summarized in FIG. 9, where the heating power and the density are scanned while the magnetic configuration is fixed to $R_{ax} = 3.65$ m and $B_0 = 2.71$ T. At each $\rho$, the local electron temperature, $T_e(\rho)$, is fitted by $n_e(\rho)^{0.5} P_{\text{tot}}^{0.5}$, or $n_e(\rho)^{1} P_{\text{dep}}(\rho)^{0.5}$, where $P_{\text{dep}}(\rho)$ is the total heating power deposited inside $\rho$, i.e. $P_{\text{dep}}(1.0) = P_{\text{tot}}$. Use of $P_{\text{dep}}$ is effective to take into account shallow penetration of heating beams in high-density plasmas [11]. Since $P_{\text{dep}}(\rho) < P_{\text{tot}}$ inside the LCFS ($\rho < 1$), $P_{\text{tot}}$ and $P_{\text{dep}}(\rho)$ give upper and lower estimation of the heating power, respectively. Note that $P_{\text{dep}}(\rho)$ is similar to $P_{\text{tot}}$ in the very edge region of $\rho > 0.9$, and therefore both fitting results coincide in this region. The ratio of $-\alpha P_{0} / \alpha n_{0}$ (or, $-\alpha P_{1} / \alpha n_{1}$) is $\sim 0.5$ in the edge region and $\sim 1$ in the core region. This means that $T_e$ can be expressed by a function of $(P_{\text{tot}}^{0.5}/n_e)$ in the edge region, while $T_e$ in the core region is expressed by another function of $(P_{\text{tot}}/n_e)$. For example, $T_e$ at $\rho = 1$ is well fitted by $(P_{\text{tot}}^{0.5}/n_e)^{2/3}$, as is shown in FIG. 10. This fitting fails, however, at $T_e < 100$ eV, suggesting that the heating power is lost by enhanced radiation in the low temperature regime, and/or the transport property changes. Although the reason why this occurs at $T_e \sim 100$ eV is not known and remains for future studies, the critical temperature scarcely depends on $P_{\text{tot}}$ [8], at least under fixed conditions of the magnetic configuration, working gas, and wall conditioning.

Since the edge temperature is a function of $(P_{\text{tot}}^{0.5}/n_e)$, the critical density that results in a critical temperature should be dependent on $P_{\text{tot}}^{0.5}$, as seen in FIG. 7 and in the Sudo scaling. In this explanation, the power balance between $P_{\text{tot}}$ and $P_{\text{rad}}$ is not mentioned explicitly. Nevertheless, this power balance might be playing an important role in determining the critical temperature.

![FIG. 9. Summary of regression analysis of the electron temperature in attached plasmas. See text for definition of fitting parameters.](image)

![FIG. 10. Electron temperature dependence on the square root of heating power divided by the local electron density, at the LCFS.](image)
3.2. Evolution of the edge density

At complete detachment, \( n_e^{100\text{eV}} \) begins to increase rapidly reflecting improvement of the effective fueling efficiency (see FIG. 5 in Section 2) and continues to increase toward radiating collapse, unless gas fueling is decreased. However, this increase of the edge density is only observed inside \( \rho_{100\text{eV}} \). Outside of the hot plasma boundary (\( \rho > \rho_{100\text{eV}} \)), the density decreases as the plasma column shrinks, even though gas fueling is continued. In FIG. 11, shown are \( n_e(\rho) / P_{\text{tot}}^{0.5} \) at the fixed positions of \( \rho = 0.8, 0.9, \) and 1.0, in shrinking plasmas where \( \rho_{100\text{eV}} \) decreases from > 1 to zero (from right to left in FIG. 11). The local density at each \( \rho \) increases with decreasing \( \rho_{100\text{eV}} \), as long as \( \rho_{100\text{eV}} > \rho \), and begins to decrease with \( \rho_{100\text{eV}} \), after \( \rho_{100\text{eV}} \) passes through the \( \rho \). As a result, for example, the maximum density at \( \rho = 0.9 \) is obtained when \( \rho_{100\text{eV}} \sim 0.9 \), i.e. the maximum of \( n_e(0.9) \) is roughly equal to \( n_e^{100\text{eV}} \) at \( \rho_{100\text{eV}} = 0.9 \). Therefore, \( n_e^{100\text{eV}} \) is a good representative of the maximum of \( n_e(\rho) \) at each \( \rho \). Now, the meaning of \( \rho_{100\text{eV}} \) as the hot plasma boundary can be redefined as below; \( \rho_{100\text{eV}} \) is the radial position inside which one can increase the electron density by fueling.

3.3. Maximum edge densities achievable in attached and detached conditions

Since \( n_e^{100\text{eV}} \) represents the maximum local density and increases with \( P_{\text{tot}}^{0.5} \), a plot of \( n_e^{100\text{eV}} / P_{\text{tot}}^{0.5} \) versus \( \rho_{100\text{eV}} \), as in FIG. 12, gives a radial profile of maximum edge densities in attached and detached plasmas. The maximum edge density increases as the plasma column shrinks and \( \rho_{100\text{eV}} \) decreases. In the attached condition (\( \rho_{100\text{eV}} \geq 1 \)), therefore, the maximum is reached at \( \rho_{100\text{eV}} = 1 \), which roughly corresponds to 0.8 \( n_c^{\text{Sudo}} \) on average. As \( \rho_{100\text{eV}} \) decreases,
the maximum edge density increases further and then saturates to \( \sim 1.5 \ n_{c_{\text{Sudo}}} \) at \( \rho_{100eV} \leq 0.95 \). Even in the pellet-fueled plasmas (crosses in FIG. 12), the maximum edge density follows the same tendency as in gas-fueled plasmas (open circles). Note that this maximum edge density is not necessarily sustainable. To avoid further shrinking that leads to radiating collapse, one should decrease the fueling. Serpens mode appears in such a situation (closed circles). In the Serpens mode phase, \( \rho_{100eV} \) fluctuates within 0.8 to 0.95, and correspondingly, the maximum edge density also fluctuates within \( 1.5 \ n_{c_{\text{Sudo}}} \) to \( 0.8 \ n_{c_{\text{Sudo}}} \). Even if the edge density decreases to \( 0.8 \ n_{c_{\text{Sudo}}} \), which is the threshold density for complete detachment, the Serpens plasma keeps the detachment condition of \( \rho_{100eV} < 1 \). In some cases, however, the plasma does reattach after the Serpens mode phase.

In FIG. 13, shown are the neutral pressure, \( p_0 \), normalized by \( P_{\text{tot}}^{0.5} \), versus \( \rho_{100eV} \) as in FIG. 12. Generally, \( p_0 \) increases with the density in attached plasmas. At detachment, \( p_0 \) decreases even though gas puffing is continued and the edge density increases. In the Serpens mode phase after the gas puff is turned off, \( p_0 \) decreases to as small as \( \sim 1/3 \) of that during gas puffing. With low recycling conditions, \( p_0 \) decreases further and reattachment occurs. On the contrary, if recycling is too high and \( p_0 \) does not decrease enough even after the gas puff is turned off, then \( \rho_{100eV} \) continues shrinking toward radiating collapse.

4. Summary

The highest central density in net current free helical plasmas, including heliotrons and stellarators, of \( 5 \times 10^{20} \ m^{-3} \) has been demonstrated in LHD. The volume-averaged density reaches \( 3 \times 10^{20} \ m^{-3} \). These are attained in plasmas with strongly peaked density profiles generated by hydrogen ice pellet injection. Even in these pellet-fueled plasmas, edge densities are similar to those in gas-fueled plasmas with flat or hollow density profiles. Complete detachment takes place when the edge temperature at the LCFS decreases to a critical value of \( \sim 100 \) eV. In the edge region, the electron temperature is a function of the square root of the heating power divided by the electron density. Consequently, the critical edge density that results in complete detachment is proportional to the square root of the heating power, as is expressed in the Sudo scaling. The critical edge density roughly corresponds to 0.8 times the Sudo scaling. High volume-averaged densities reaching \( \sim 2.2 \) times the Sudo scaling are sustainable in the Serpens mode plasmas, where the edge density is limited to \( \sim 1.5 \) times the Sudo scaling. Fueling and recycling control is necessary to reproduce the Serpens mode, because an excess (a shortage) of neutral pressure leads to radiating collapse (reattachment).

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References