



# Gyrokinetic Turbulence in Tokamaks and Stellarators

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Acknowledgements:

P. Xanthopoulos, F. Merz, T. Görler, M. Pueschel, D. Told;  
A. Boozer, G. Hammett, D. Mikkelsen, M. Zarnstorff,  
H. Sugama, T. Watanabe

18<sup>th</sup> International Toki Conference; December 10, 2008

# Outline

A very brief review of some recent (tokamak) gyrokinetic results – for more details, see, e.g., E.J. Doyle *et al.*, “Progress in the ITER physics basis”, Ch. 2, Nuclear Fusion **47**, S18 (2007)

Some recent gyrokinetic turbulence simulations for:

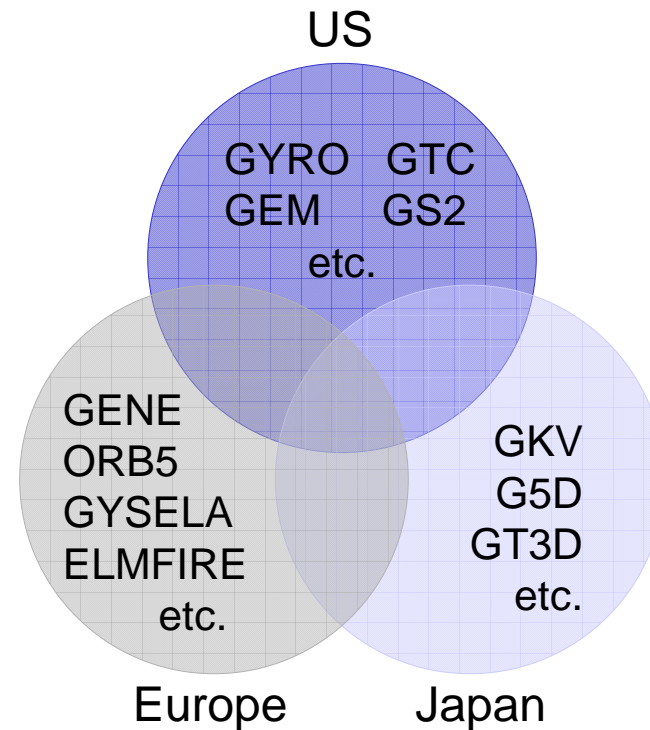
- LHD
- NCSX
- W7-X

Long-term goal: Explore potential for systematic optimization of turbulent transport in stellarators

# State of the art in nonlinear gyrokinetics



- Gyrokinetics has emerged as the standard approach to tokamak core turbulence
- Experimental comparisons are rather promising
- Extensions to tokamak edge and stellarator are underway
- Variety of gyrokinetic codes is being used and (further) developed, differing both in physics and in numerics



# Gyrokinetic stellarator codes in production



GS2 (Mikkelsen, Dorland *et al.*); GOBLIN (Yamagishi *et al.*)

- Comprehensive physics (multispecies, finite beta, collisions etc.)
- Flux tube geometry

GKV (Watanabe, Sugama *et al.*)

- Adiabatic electrons, model geometry
- Flux tube geometry
- Under further development

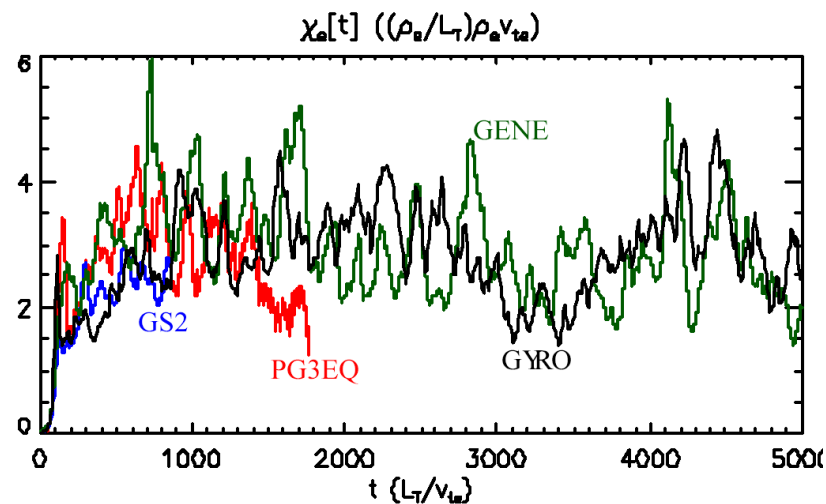
GENE (Jenko, Xanthopoulos, Merz *et al.*)

- Comprehensive physics (multispecies, finite beta, collisions etc.)
- Flux tube or global (tokamak) geometry; includes eigenvalue solver
- Under further development
- Freely available via [www.ipp.mpg.de/~fsj/gene](http://www.ipp.mpg.de/~fsj/gene)

# Code benchmarking efforts

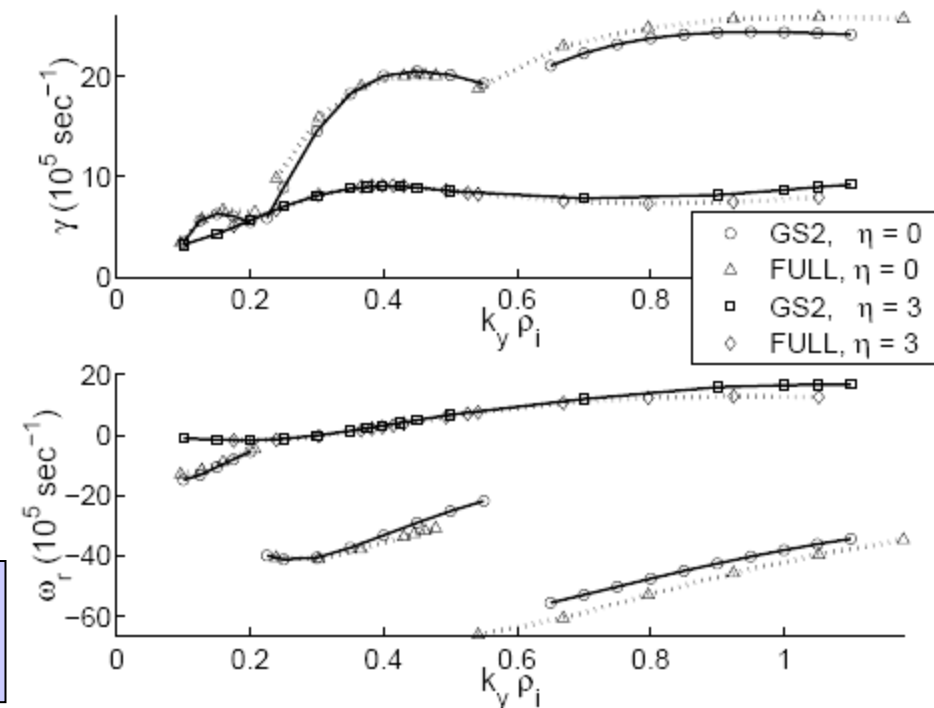
- Are we solving the equations right?
- Such efforts tend to be a bit painful but are necessary
- Examples below: Nevins *et al.*, PoP 2006 & 2007; Belli *et al.*
- Another recent example: Falchetto *et al.*, PPCF 2008

## Nonlinear tokamak ETG case



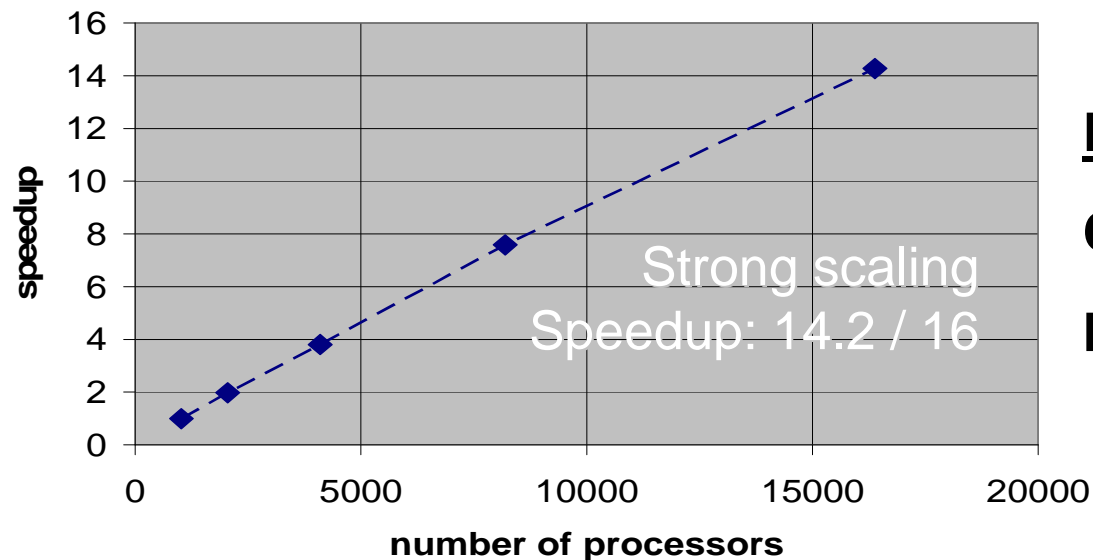
See poster P1-18 by D. Mikkelsen;  
P. Xanthopoulos *et al.*, PoP 12/2008

## Linear stellarator (NCSX) case



# Massive parallelism

- Many codes scale well up to thousands of cores
- Both particle and grid-based codes can deal with massive parallelism
- Assistance by computer experts can be helpful



## Example

**Code: GENE**

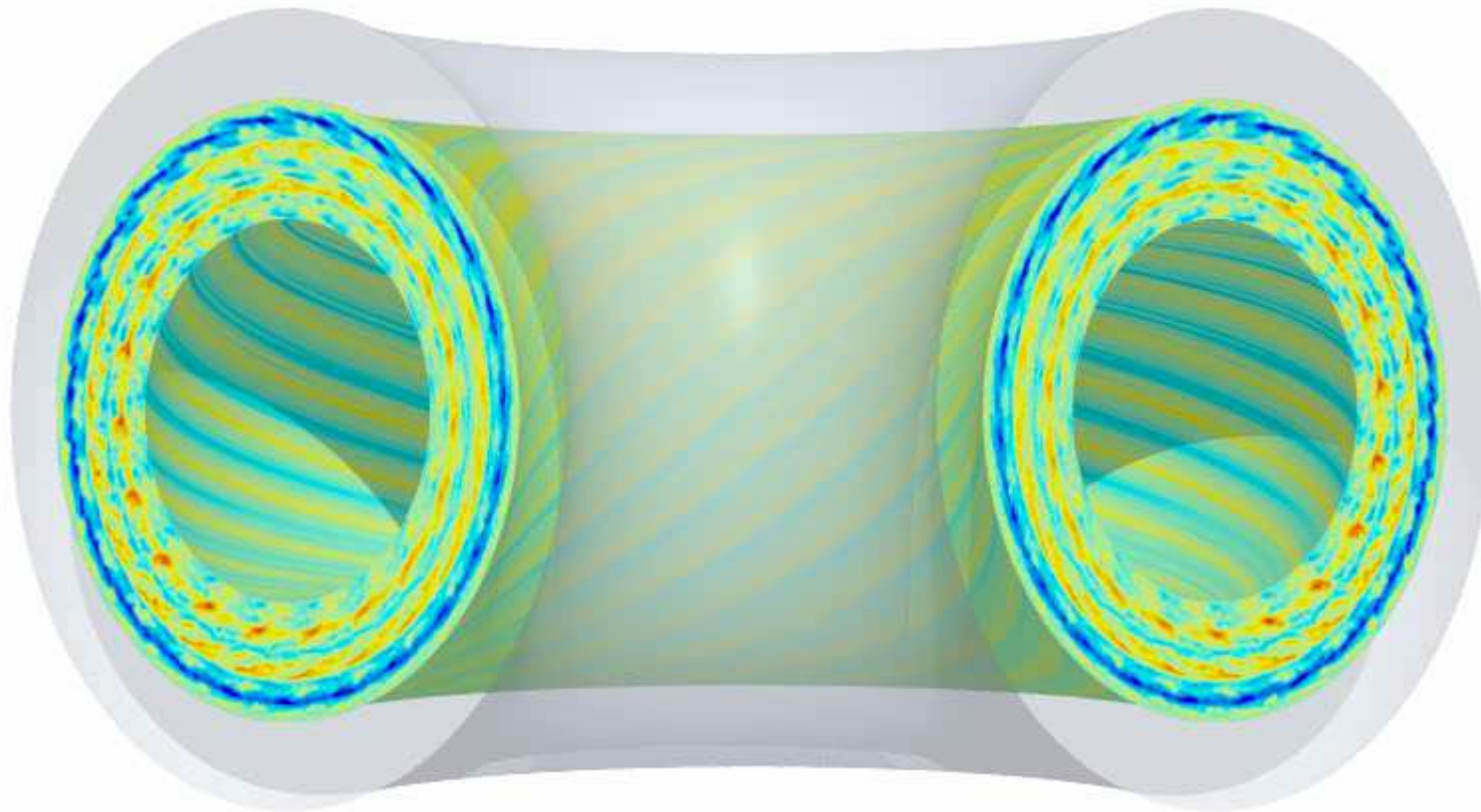
**Machine: BlueGene/L**

The community is prepared for computers with more than 10k cores.  
Further efforts are needed on the way towards PFlop/s computing.



# Tokamak simulations

# Gyrokinetic simulations for tokamaks



gene@ipp.mpg.de

[www.ipp.mpg.de/~fsj/gene](http://www.ipp.mpg.de/~fsj/gene)



# Physics issues



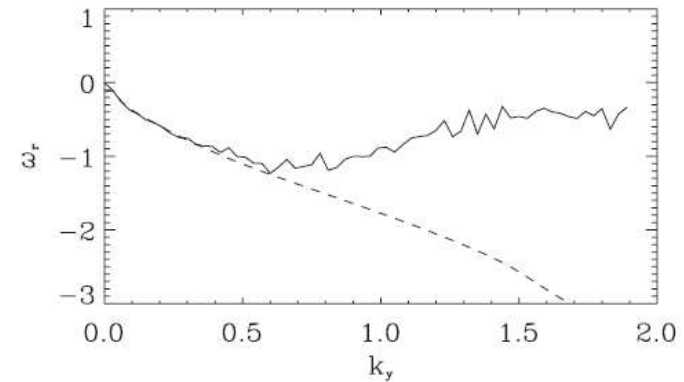
- Our physical understanding of microturbulence is still fragmentary at present
- Open questions (selection):
  1. Nonlinear saturation and mode interference
  2. Validity of quasilinear theory
  3. Impact of finite  $\beta$  effects in (improved) H-modes
  4. Role of sub-ion-gyroradius scales
  5. Interactions between turbulence, neoclassics, MHD
  6. Predictive *ab initio* modeling of core plasmas and transport barriers
- Close interactions between theory, simulation, and experiment are called for

# Nonlinear saturation of TEM turbulence

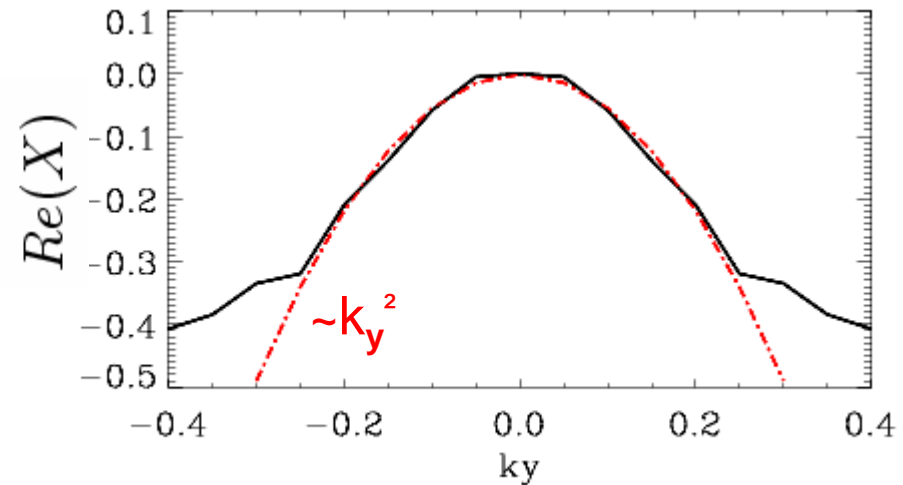
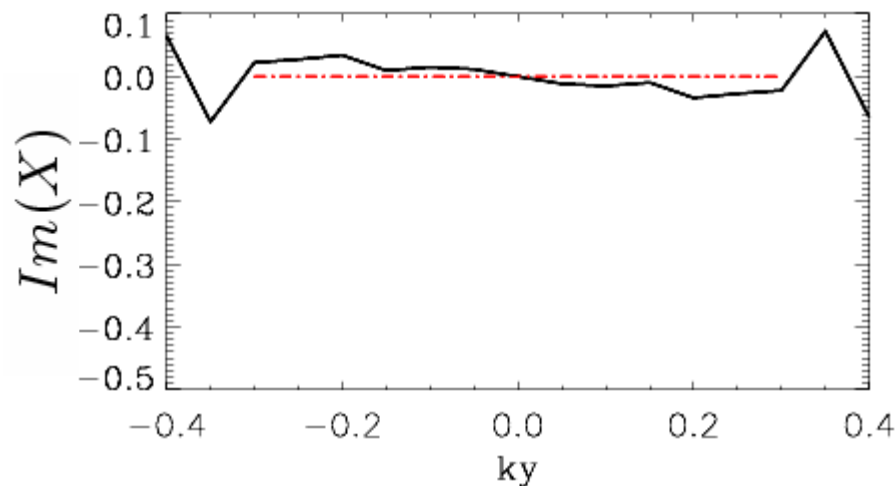
## Statistical analysis of NL GENE runs:

- No significant shift of cross phases and frequencies w.r.t. linear ones
- Low  $k_y$ : nonlinearity  $\sim$  eddy diffusion

**[Merz & Jenko, PRL 2008]**



$$\mathcal{Nl}[g] \simeq D(-k_{\perp}^2)g = D\nabla_{\perp}^2 g$$



This is in line with various theories, including Resonance Broadening Theory (Dupree), MSR formalism (Krommes), Dressed Test Mode Approach (Itoh).

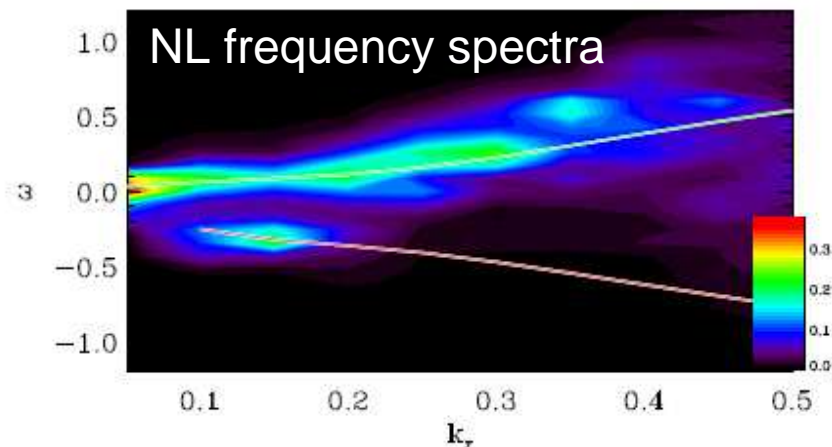
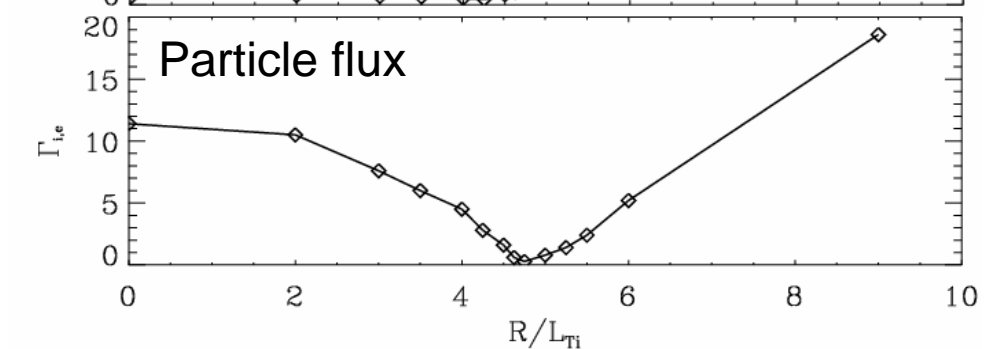
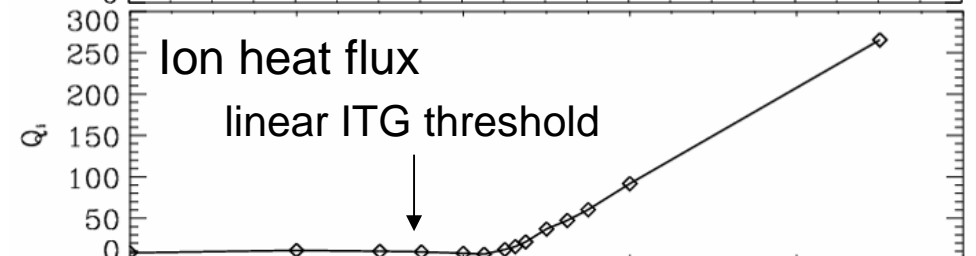
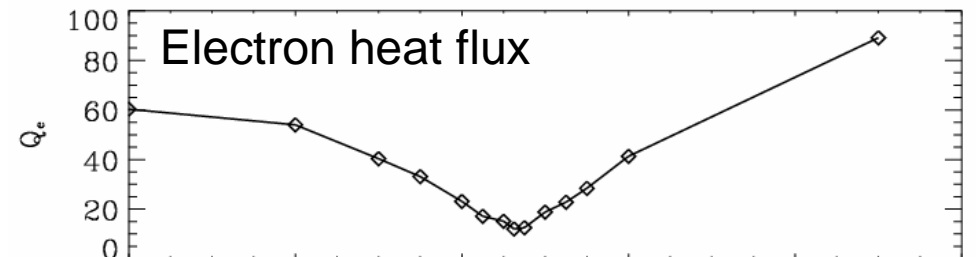
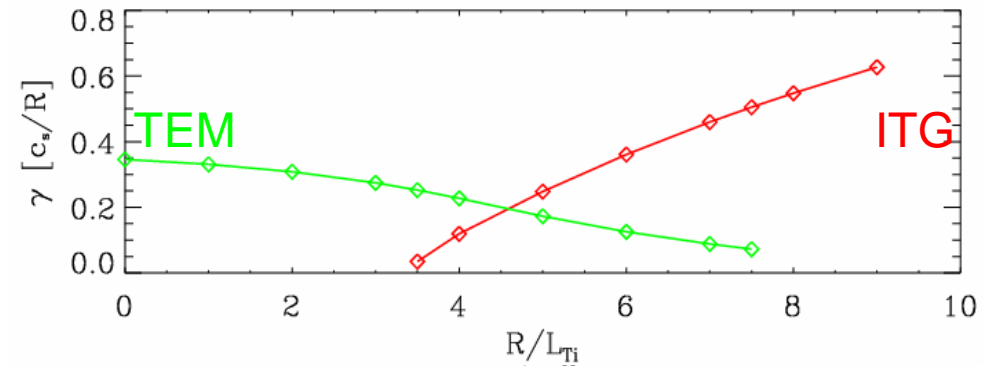
# Destructive ITG/TEM interference



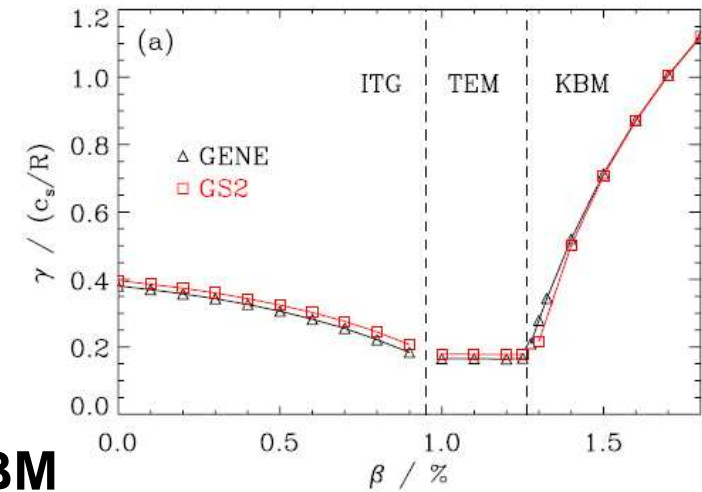
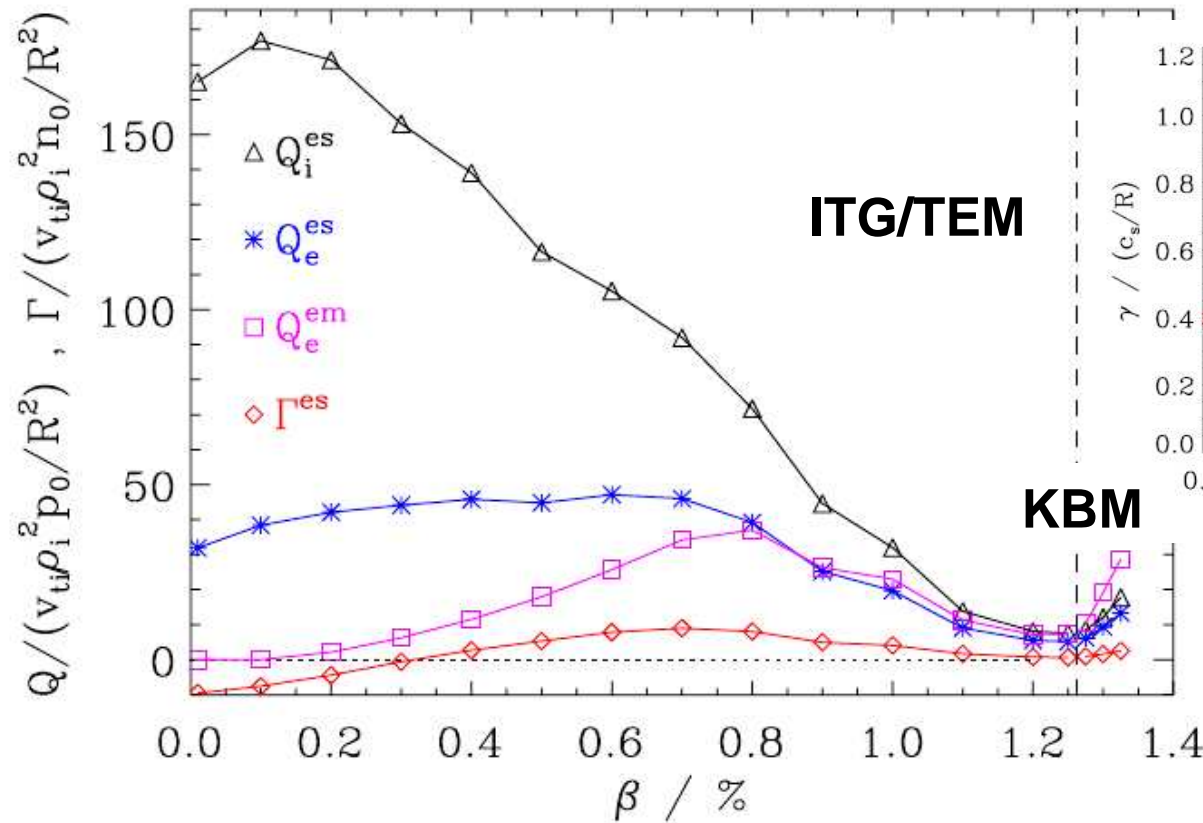
[F. Merz, PhD Thesis 2008]

- Linear growth rates ( $k_y=0.25$ ), using GENE as an EV solver

- TEM regime: Electron heat flux is suppressed, not increased
- ITG regime: Nonlinear upshift of critical  $R/L_{Ti}$
- Nonlinear ITG/TEM coexistence



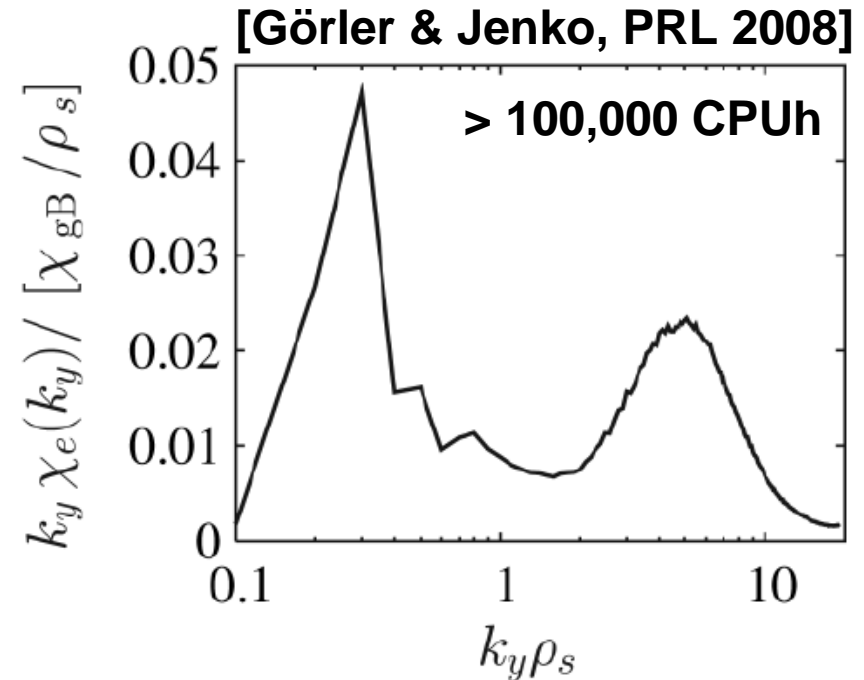
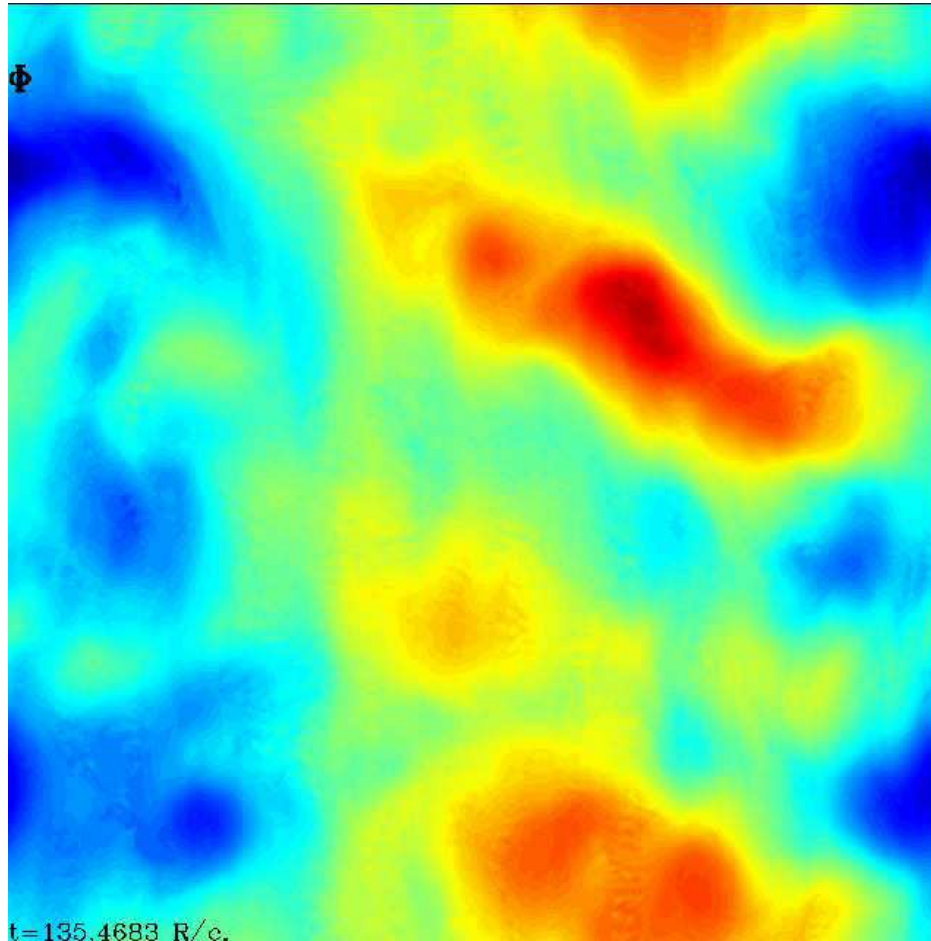
# Gyrokinetic turbulence at high beta



Finite-beta Cyclone  
Base Case simulations  
with the GENE code  
[Pueschel *et al.*, PoP 2008]

Nonlinear drop clearly exceeds (quasi-)linear expectations;  
this is likely to be due to destructive ITG/TEM interference.

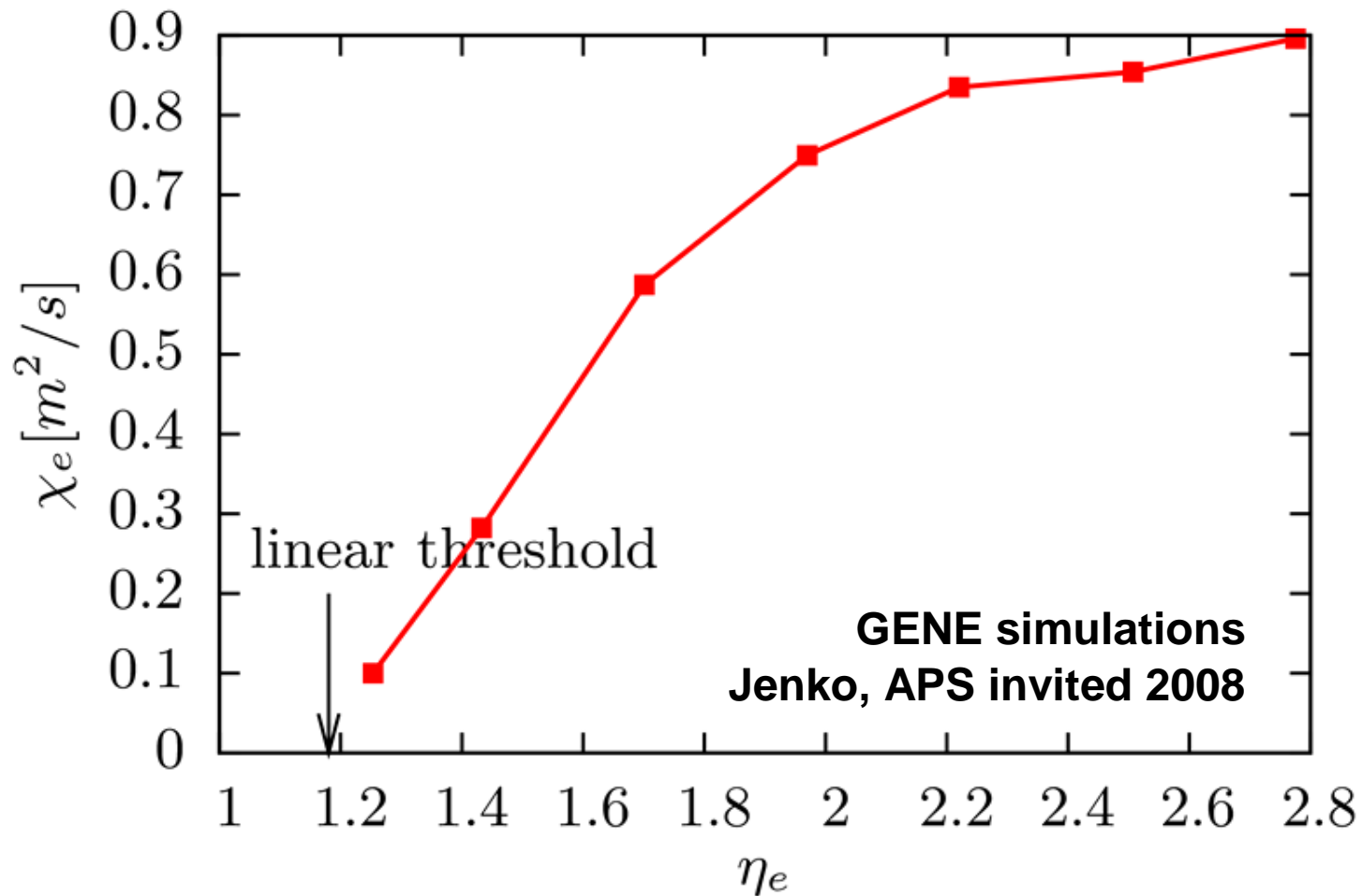
# Role of sub-ion-gyroradius scales



Mazzucato *et al.*, PRL 2008  
Smith / Yuh, APS invited 2008  
Schmitz, APS invited 2008

GENE simulations of ITG/TEM/ETG turbulence: Large fraction of the electron heat transport is carried by the electron scales.

# Electron heat diffusivity from edge ETG

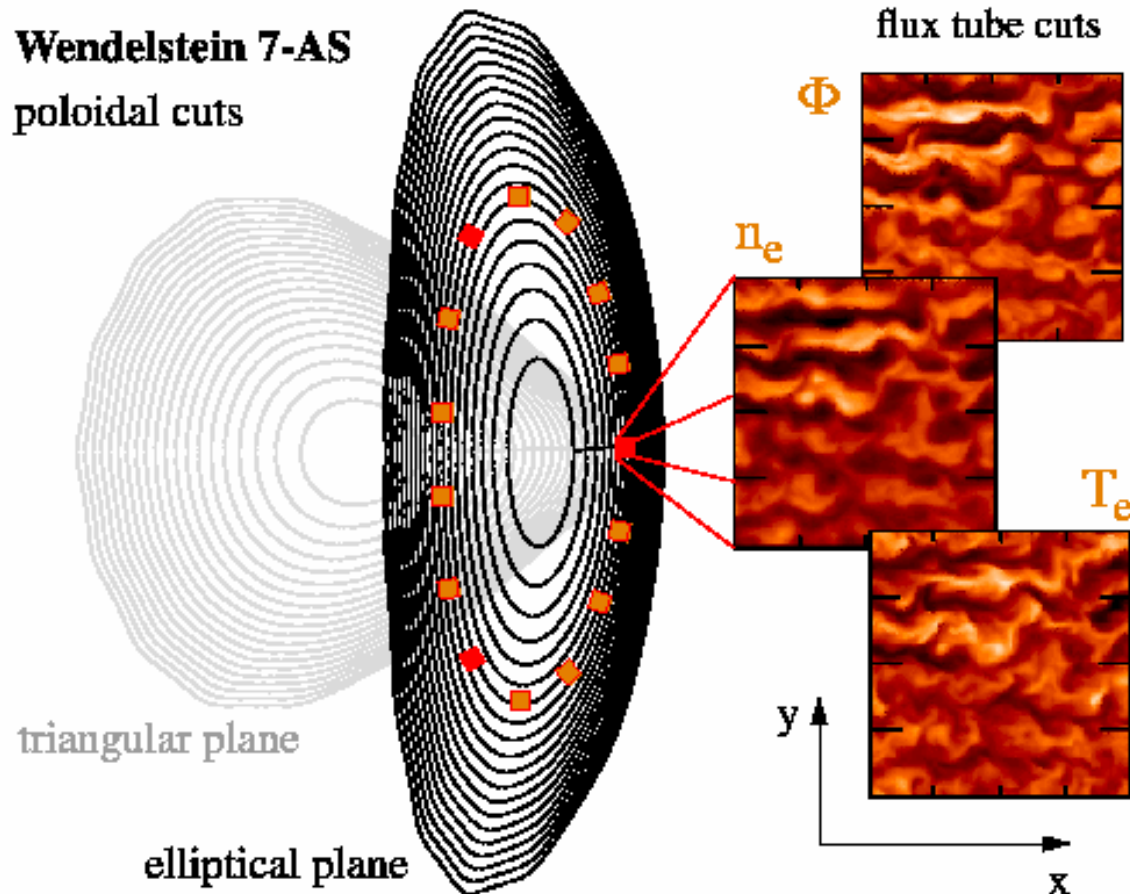


ETG turbulence is able to explain the residual electron heat transport in H-mode edge plasmas.



# Stellarator simulations

# Gyrokinetic simulations for stellarators



Jenko & Kendl, NJP & PoP 2002

## *Linear simulations*

Rewoldt *et al.* 1999  
Kuroda *et al.* 2000  
Kendl 2001 & 2004  
Jenko & Kendl 2002  
Rewoldt *et al.* 2002 & 2005  
Lewandowski 2003  
Kornilov *et al.* 2004 & 2005  
Yamagishi *et al.* 2007  
Xanthopoulos & Jenko 2007

## *Nonlinear simulations*

Jenko & Kendl 2002 & 2002  
Xanthopoulos *et al.* 2007  
Watanabe *et al.* 2007 & 2008



# Stellarator-specific issues



- Fairly (physically) comprehensive flux tube simulations in real 3D MHD equilibria are becoming feasible
- Nonlocal codes to be developed; computational cost will be very substantial, however
- Open questions (selection):
  1. Similarities and differences w.r.t. tokamak turbulence?
  2. Impact of 3D shaping on linear properties of various microinstabilities and their nonlinear saturation mechanisms?
  3. Potential for systematic optimization of turbulent transport in stellarators (long-term goal)?



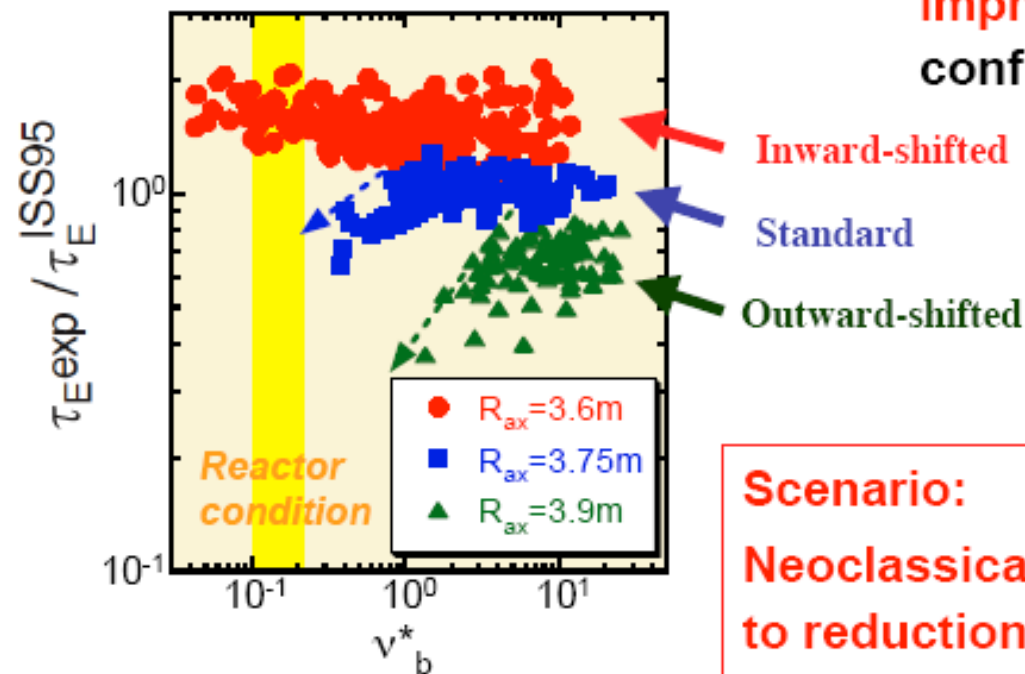
Some recent GKV results on  
LHD core turbulence  
(using non-axisymmetric model equilibria)

Studies by H. Sugama and T. Watanabe

# Results from LHD experiments

For low collisionality, better confinement is observed in the **inward-shifted** magnetic configurations, where **lower neoclassical ripple transport** but **more unfavorable magnetic curvature** driving pressure-gradient instabilities are anticipated.

**Anomalous transport** is also **improved** in the inward shifted configuration.



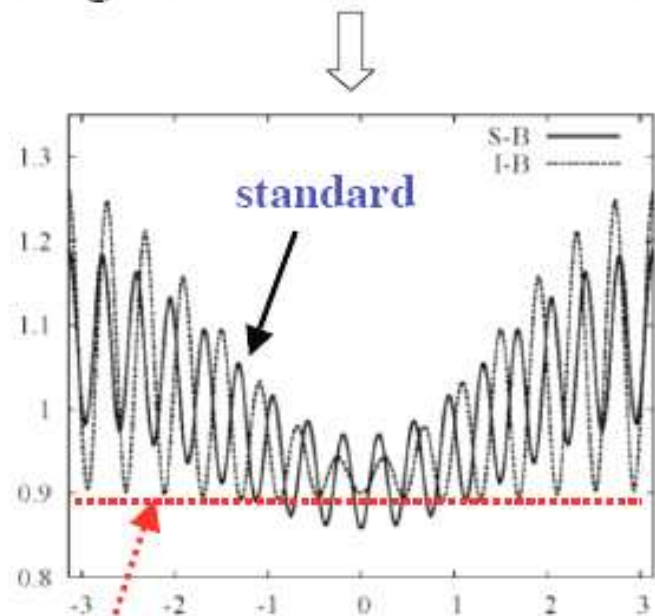
H. Yamada *et al.* (PPCF2001)

## Scenario:

Neoclassical optimization contributes to reduction of anomalous transport by enhancing the zonal-flow level.

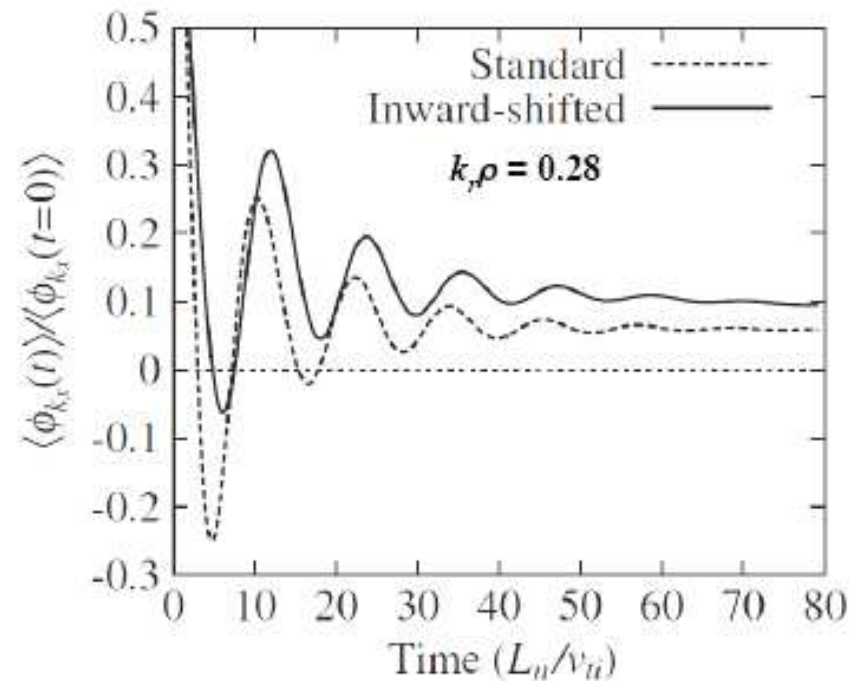
# Standard and inward-shifted configurations

$|B|$  along the fieldline on the magnetic surface at  $r = 0.6 a$



**Inward**  
 $\Rightarrow$  smaller neoclassical transport

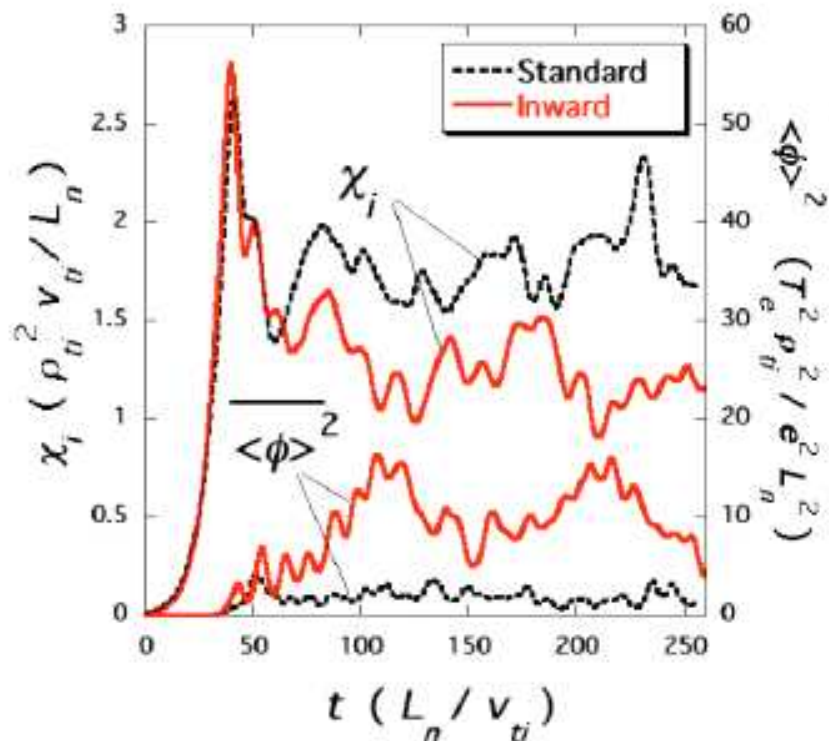
Time evolution of zonal-flow potential



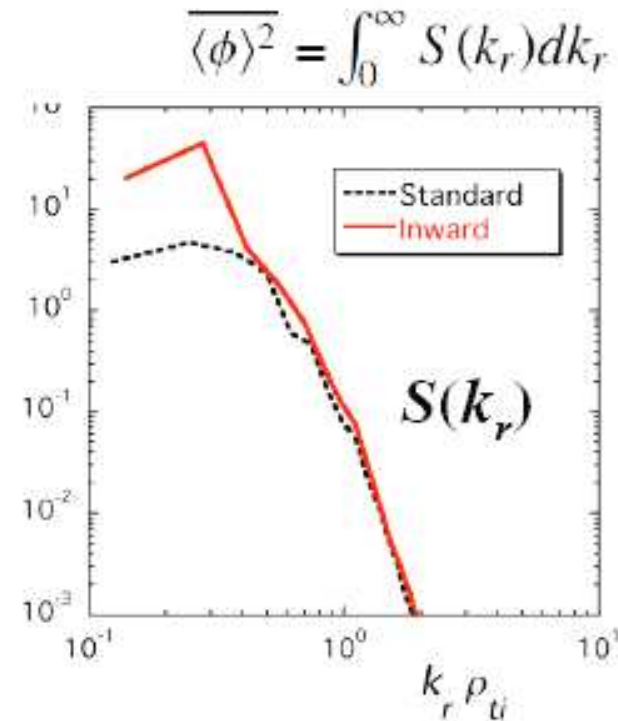
**Larger residual zonal flow is found for the inward-shifted case.**

# Adiabatic ITG turbulence simulations

Smaller  $\chi_i$  and larger zonal flows are found in the saturated turbulent state for the inward-shifted configuration than for the standard one !



Turbulent thermal diffusivity and squared zonal-flow potential

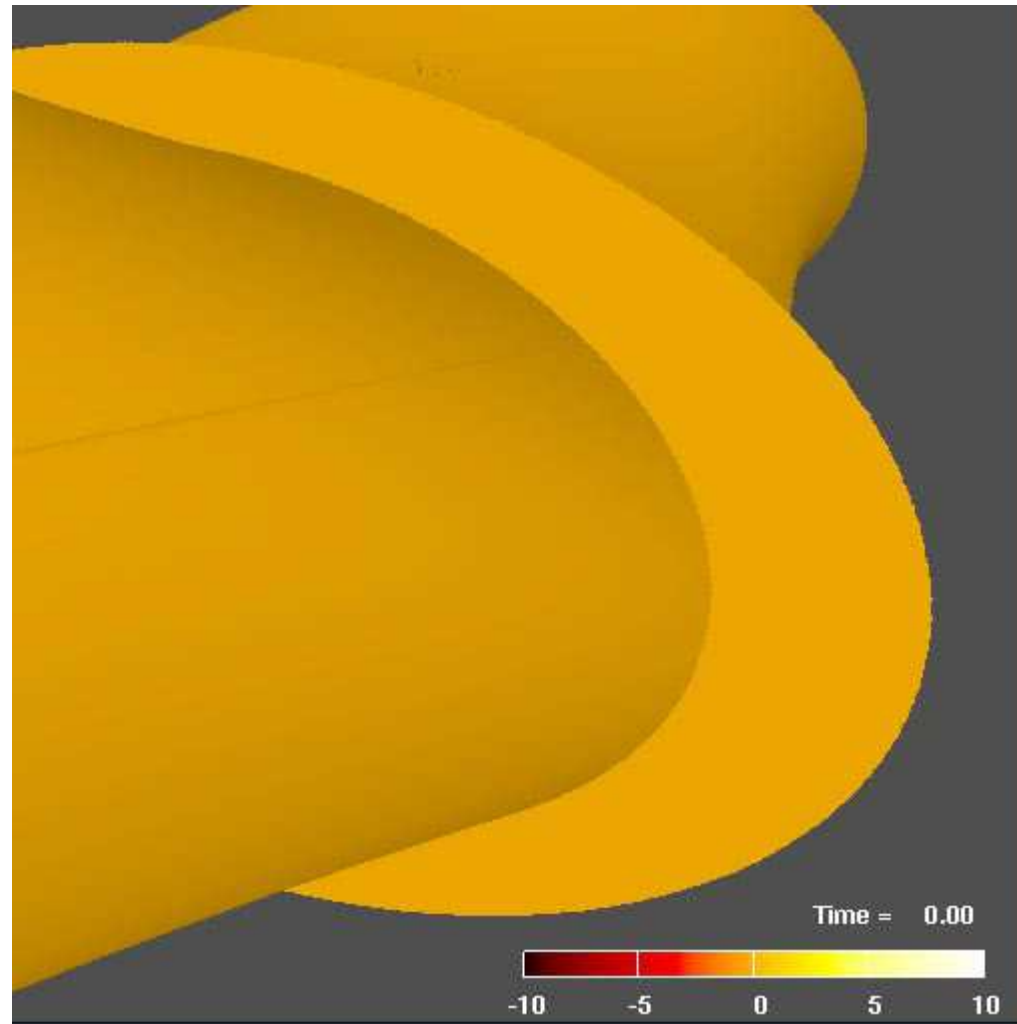


$k_r$  spectrum of zonal-flow potential (averaged over  $60 < t < 250$ )

# Zonal flow dynamics in ITG-ae simulations



Contours of potential fluctuations (Inward-Shifted Case)



Sugama, APS invited 2008

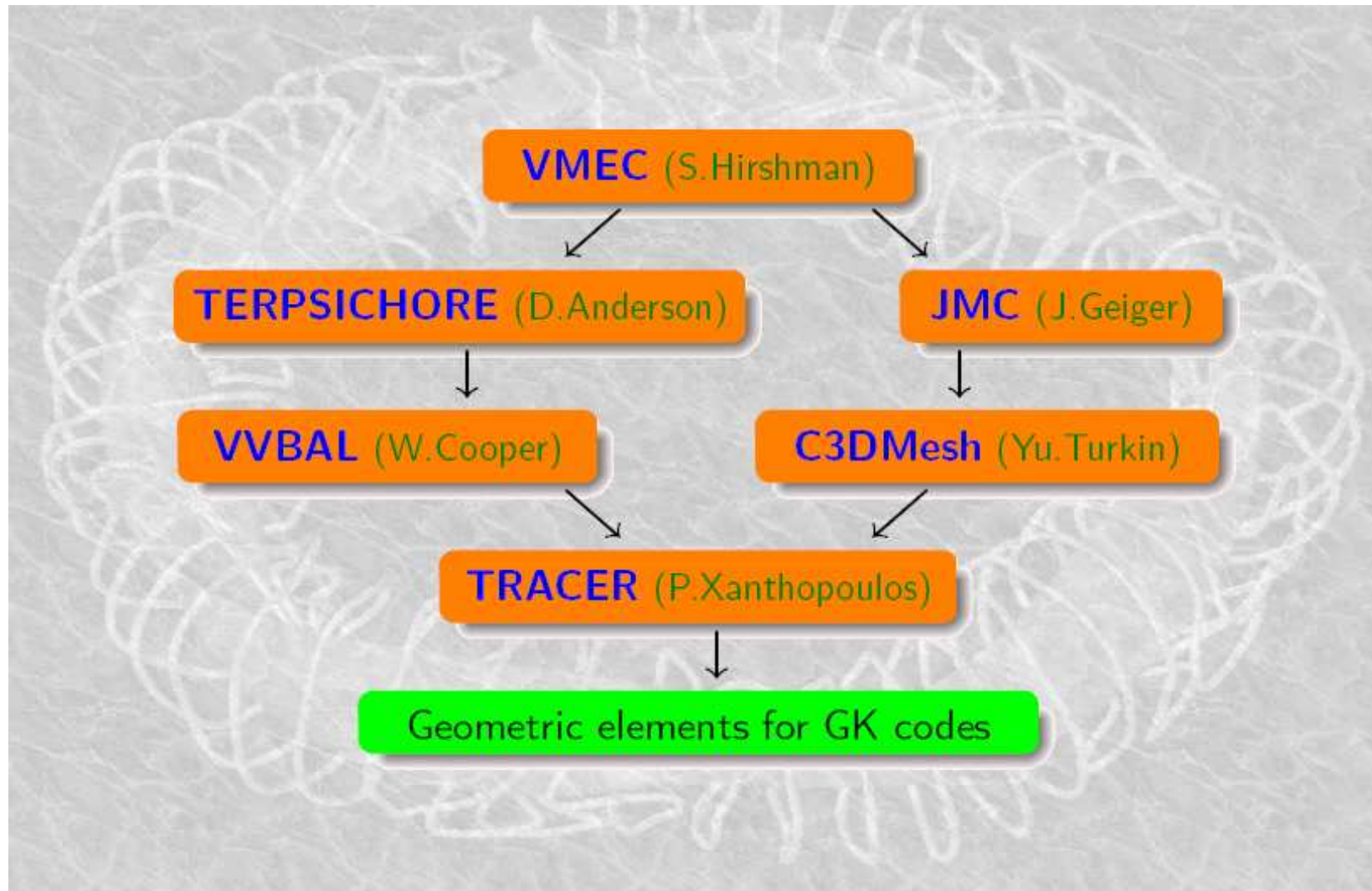
Some recent GENE results on  
NCSX and W7-X core turbulence  
(using real non-axisymmetric equilibria)

# Geometry Interface for Stellarators/Tokamaks



Author: P. Xanthopoulos (thanks to W. A. Cooper)

Goal: Local simulations for non-axisymmetric devices

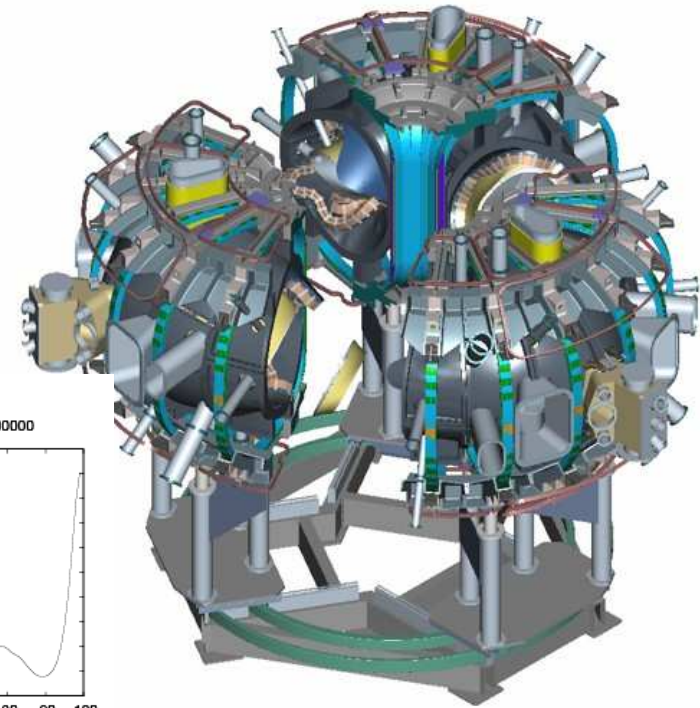




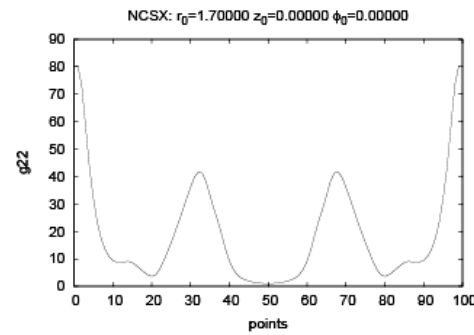
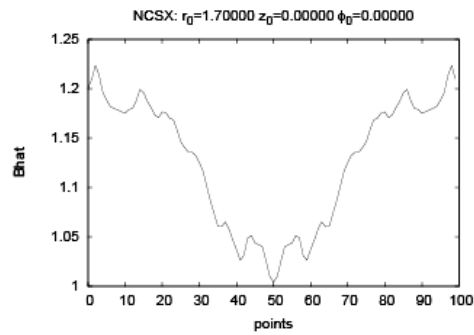
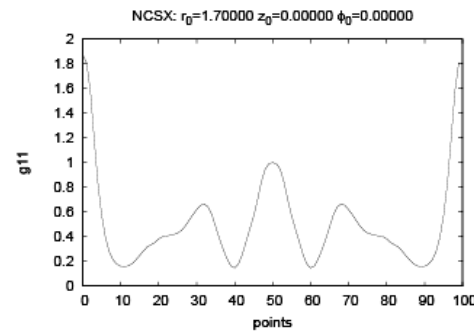
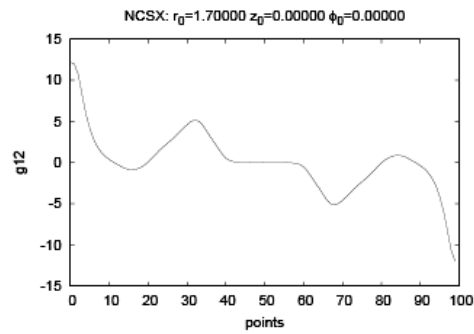


First example:  
NCSX

# Geometric coefficients for NCSX



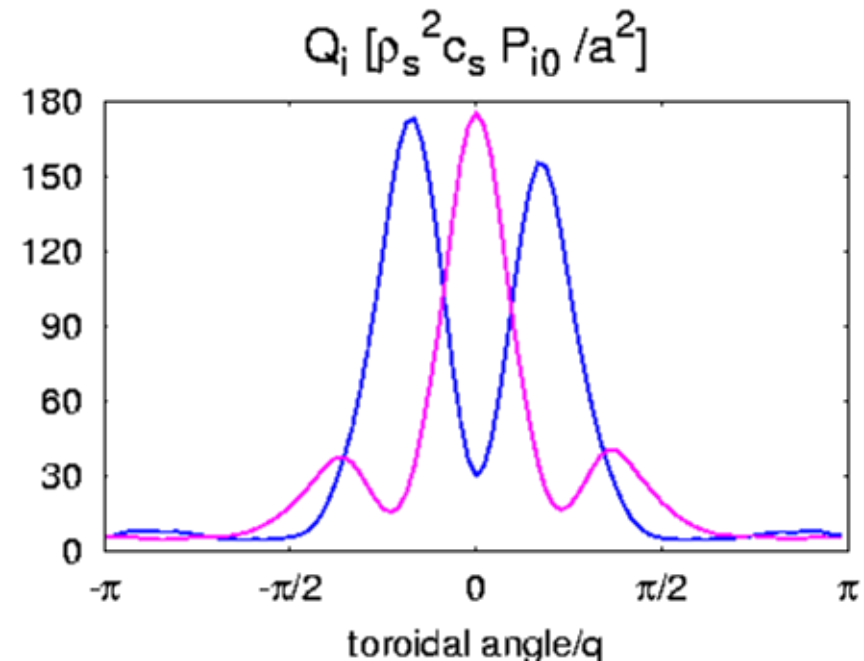
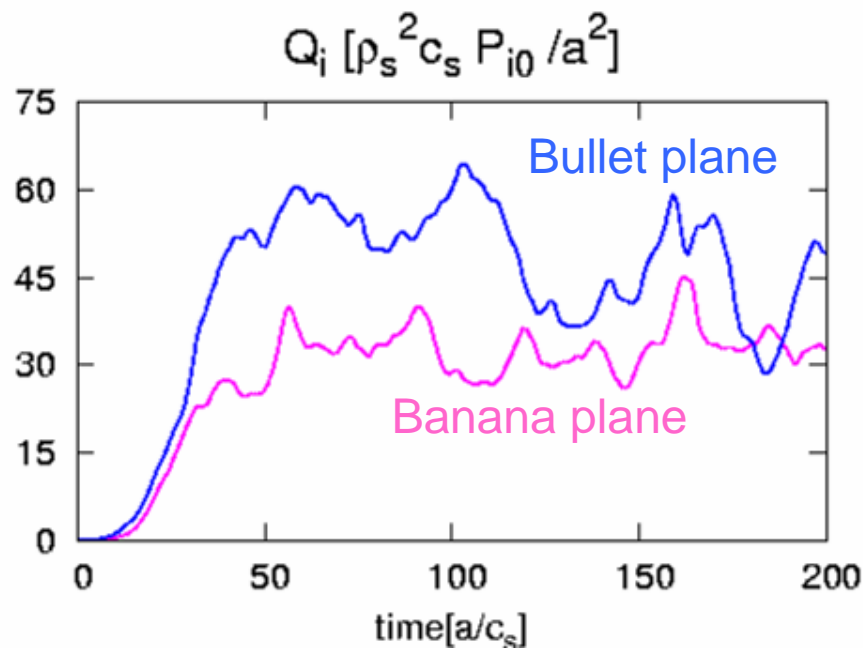
[Xanthopoulos & Jenko, PoP 2006]



# Adiabatic ITG turbulence in NSCX



Two different flux tubes on the same magnetic surface:  
The turbulent transport differs by a few 10%;  
moreover, the parallel mode structures differ.

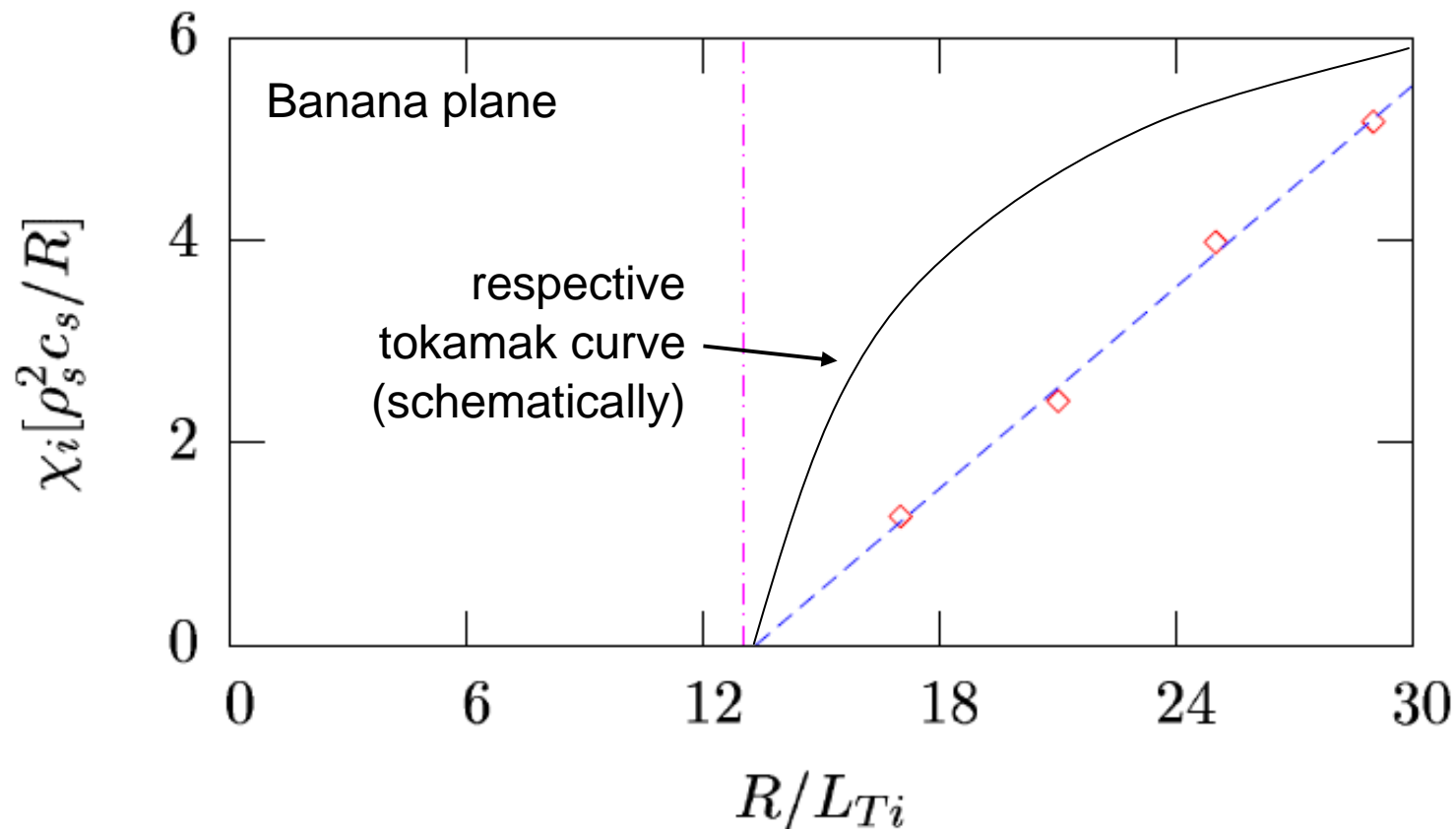


**Critical gradients also differ; softening of turbulence onset!**

# Flux-gradient relationship (adiabatic ITG modes)



- Offset-linear scaling for  $\chi$  – not Q
- **Moderate profile stiffness**

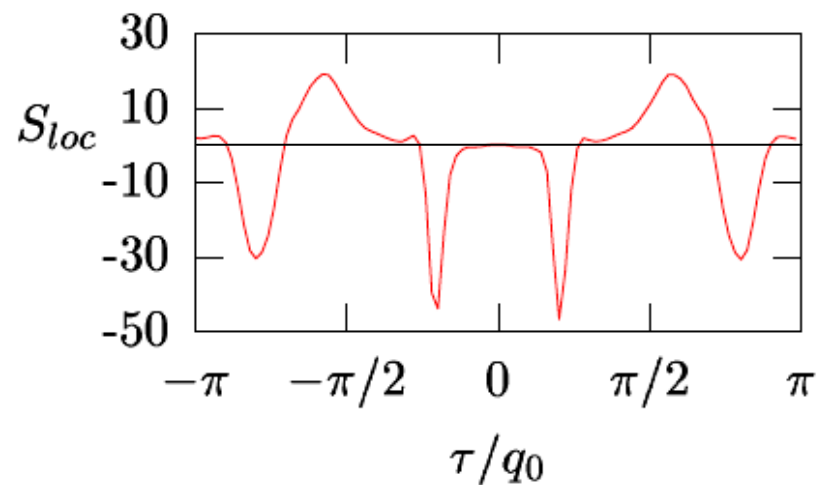
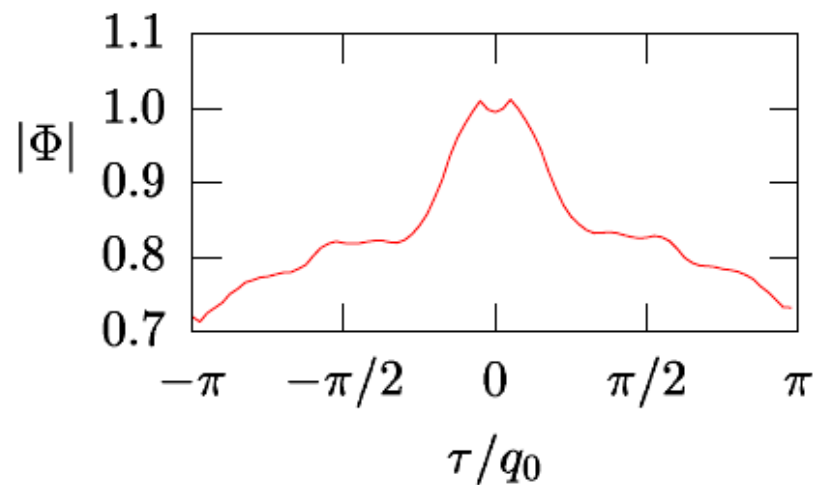


# Parallel mode structure and linear threshold



NCSX exhibits strong ballooning controlled by localized bad curvature and local shear.

Example (*nonlinear* GENE simulation):



**Linear thresholds of NCSX, W7-X, AUG, DIII-D are similar, but they can be increased by increasing the effective  $k_{\parallel}$**

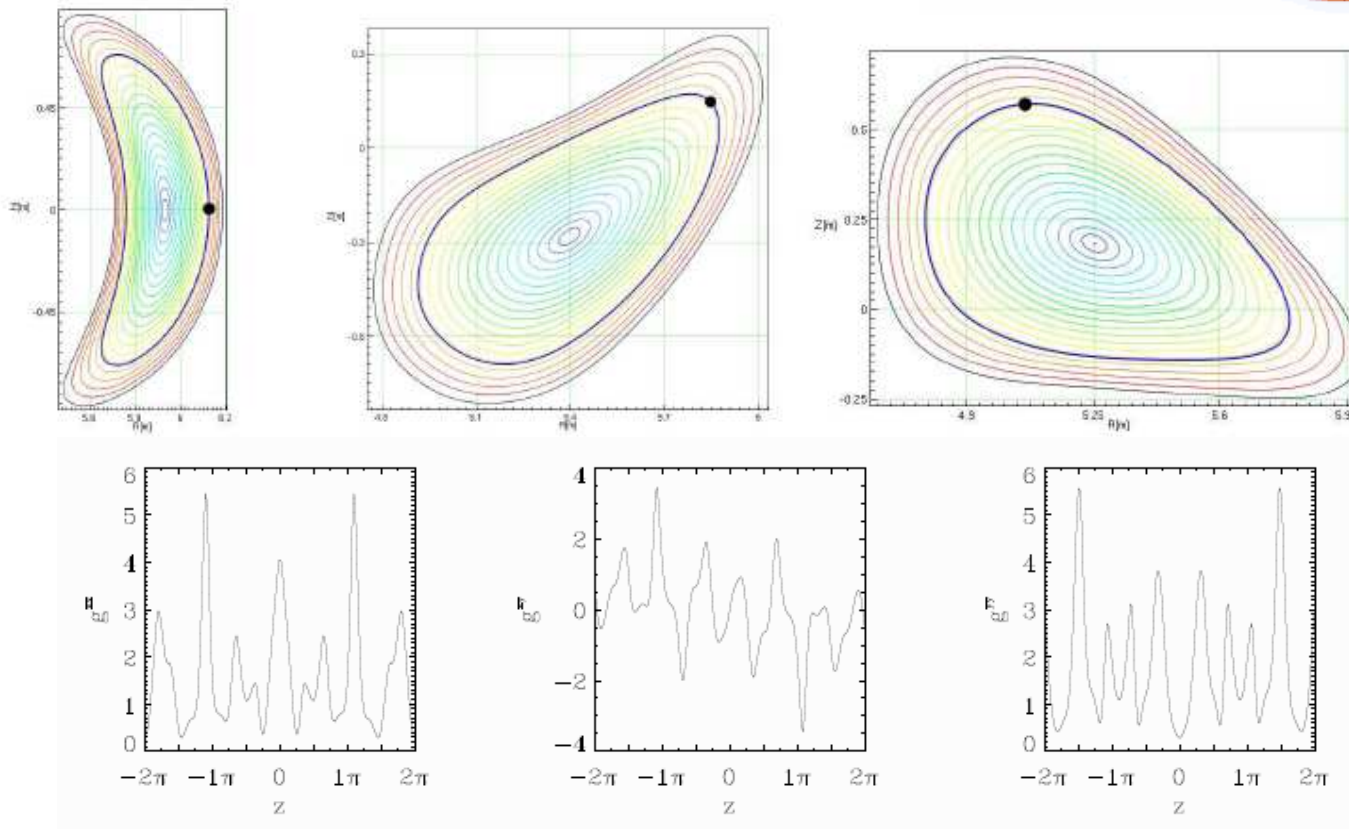
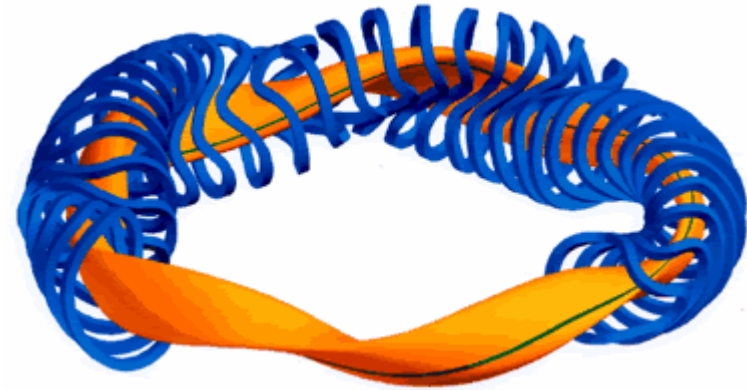


Second example:  
Wendelstein 7-X

# Geometric coefficients for W7-X

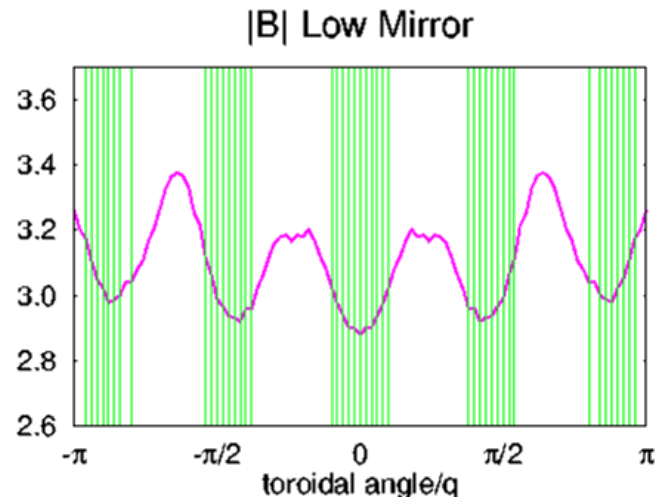


Wendelstein 7-X stellarator: optimized with respect to neoclassical transport

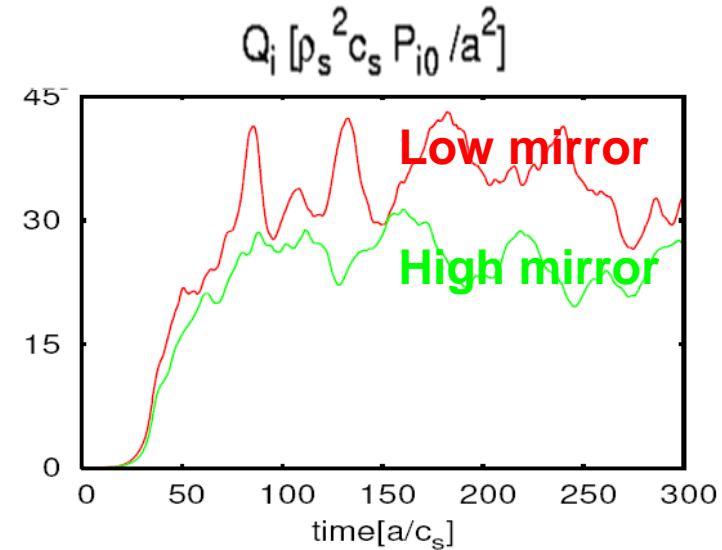
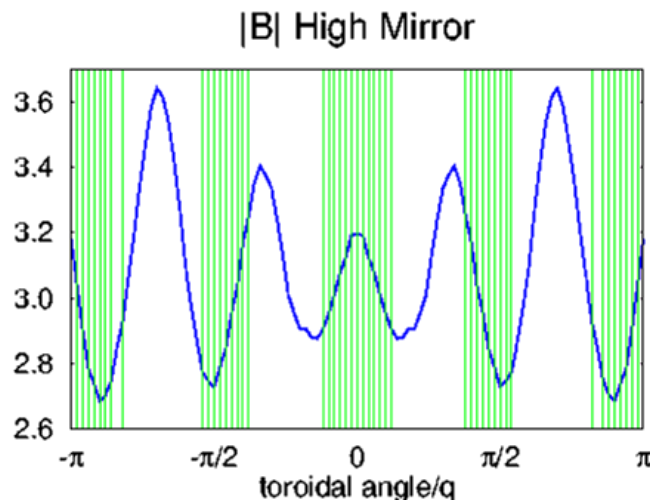


[Xanthopoulos & Jenko, PoP 2006]

# ITG-ae turbulence: Subtle geometric effects



Bad curvature regions

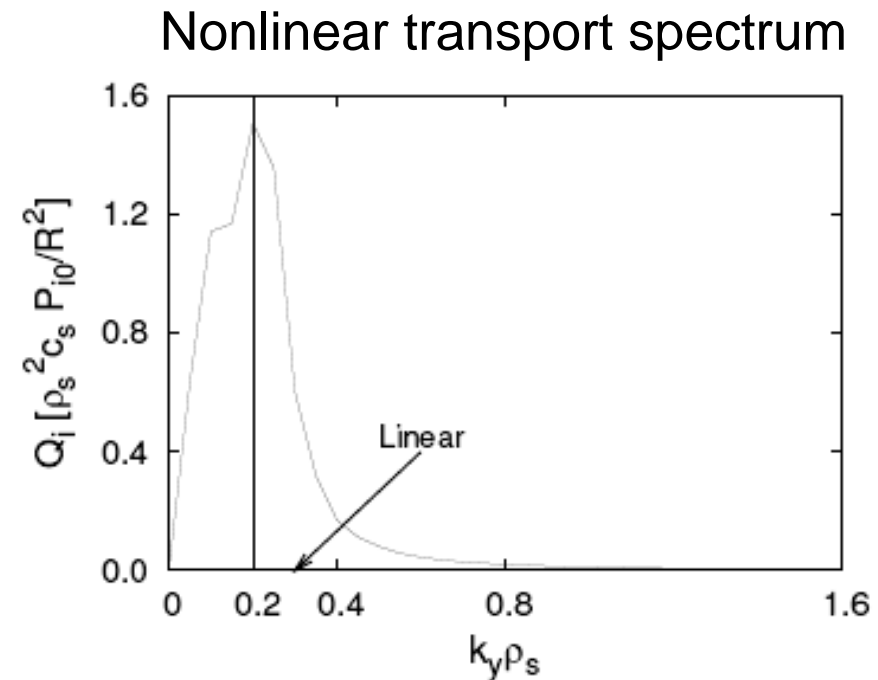
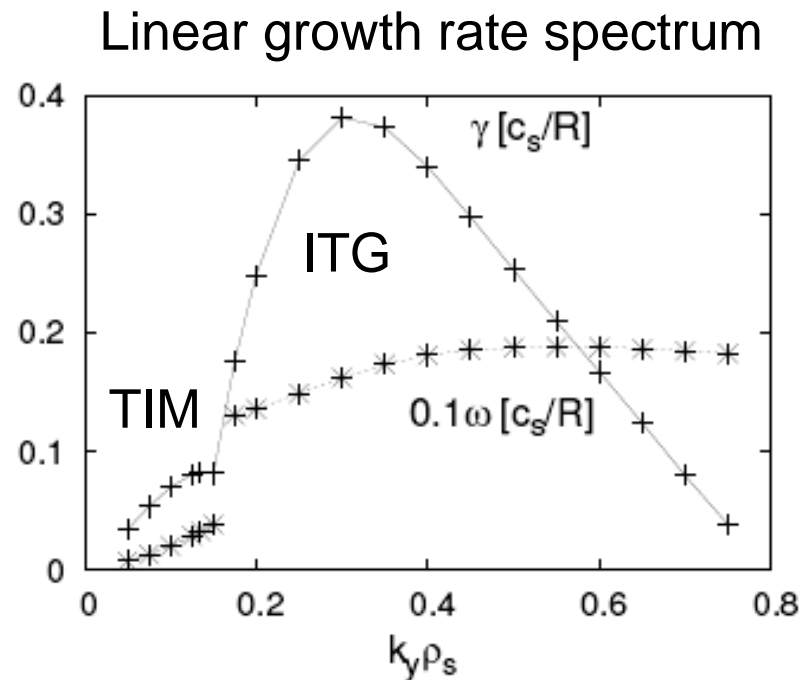


Two configurations which are geometrically virtually identical yield clearly differing results – although the linear physics is almost the same; there must be geometric control of the NL saturation mechanism



# Nonlinear ITG/TIM coexistence

GENE simulations for W7-X (close to the magnetic axis; adiabatic electrons):  
Trapped ion modes and ITG modes coexist linearly and nonlinearly.



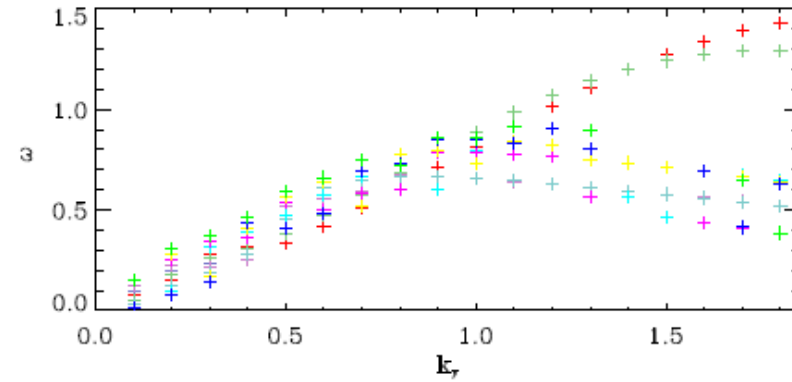
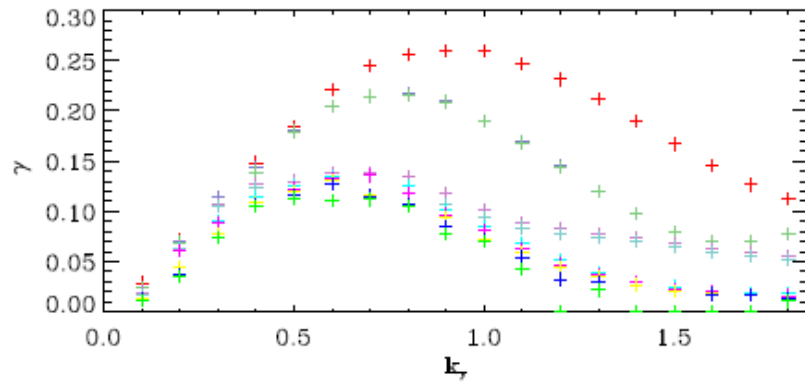
[Xanthopoulos, Merz, Görler & Jenko, PRL 2007]

**Destructive interference phenomena?**

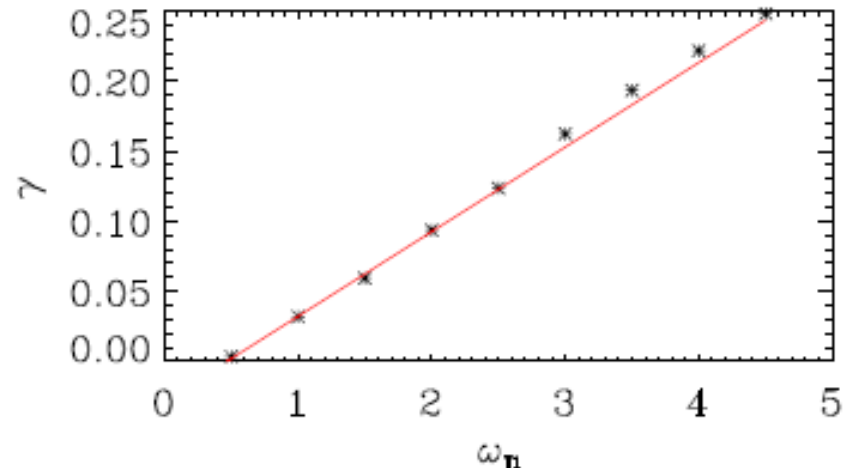
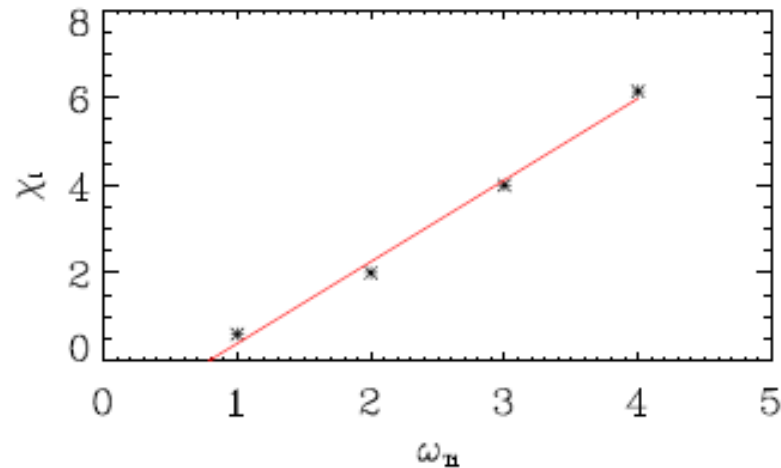
# ITG turbulence in W7-X (adiabatic electrons)



Many modes are unstable, with similar growth rates.



Nonlinear runs exhibit strong ZF activity, 35% Dimits shift.

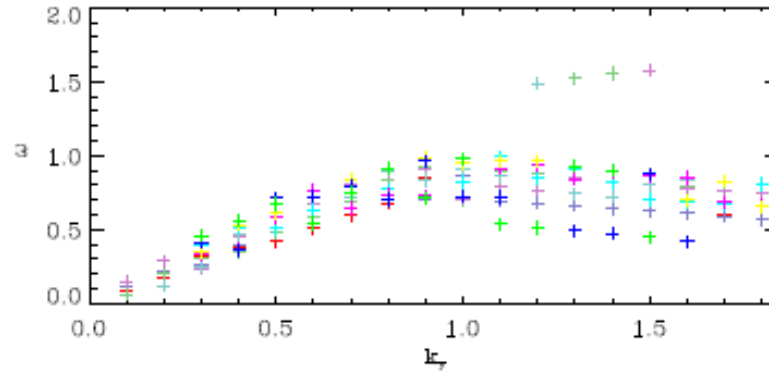
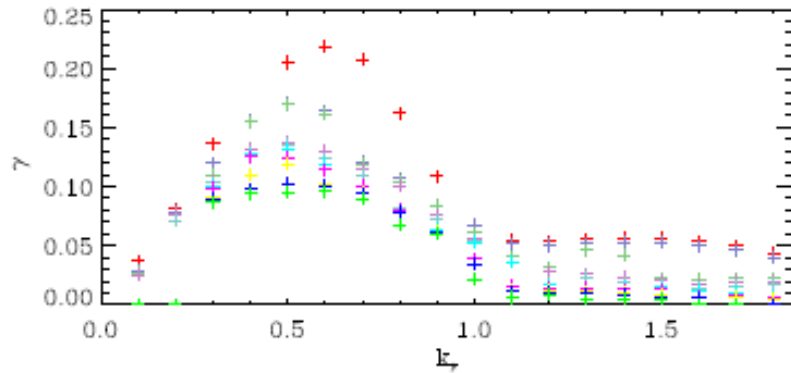


[F. Merz, PhD Thesis 2008]

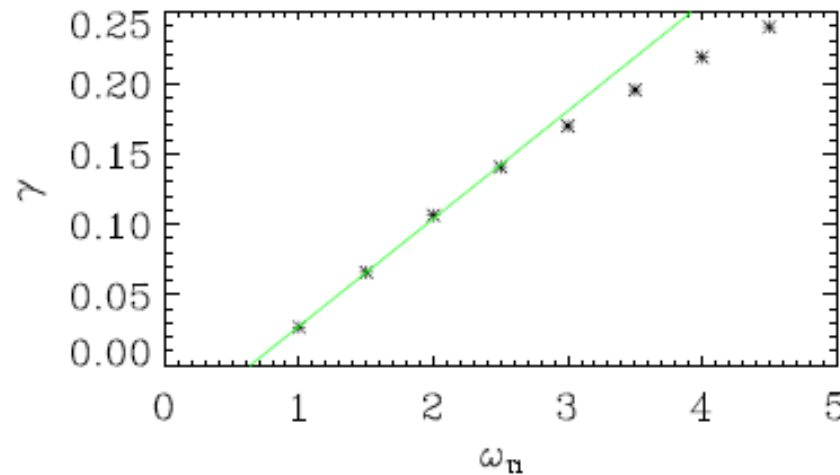
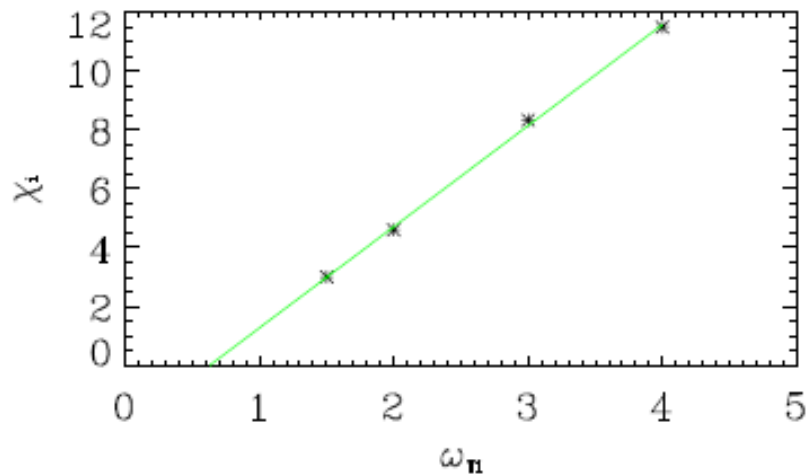
# ITG turbulence in W7-X (kinetic electrons)



Many modes are unstable, with similar growth rates.



Nonlinear runs exhibit weak ZF activity, no Dimits shift.



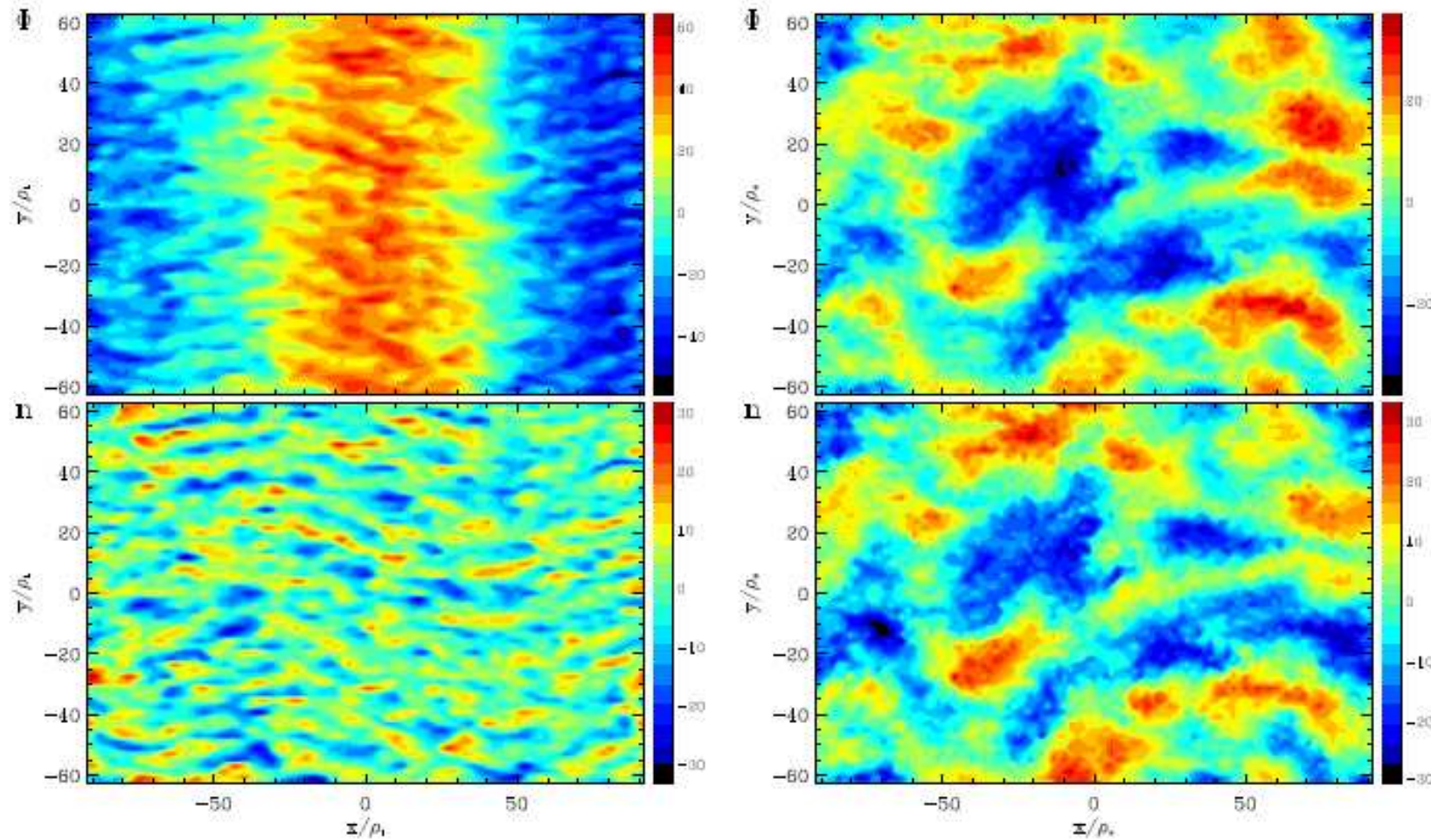
[F. Merz, PhD Thesis 2008]

# ITG turbulence in W7-X: Role of zonal flows



Adiabatic electrons

Kinetic elec



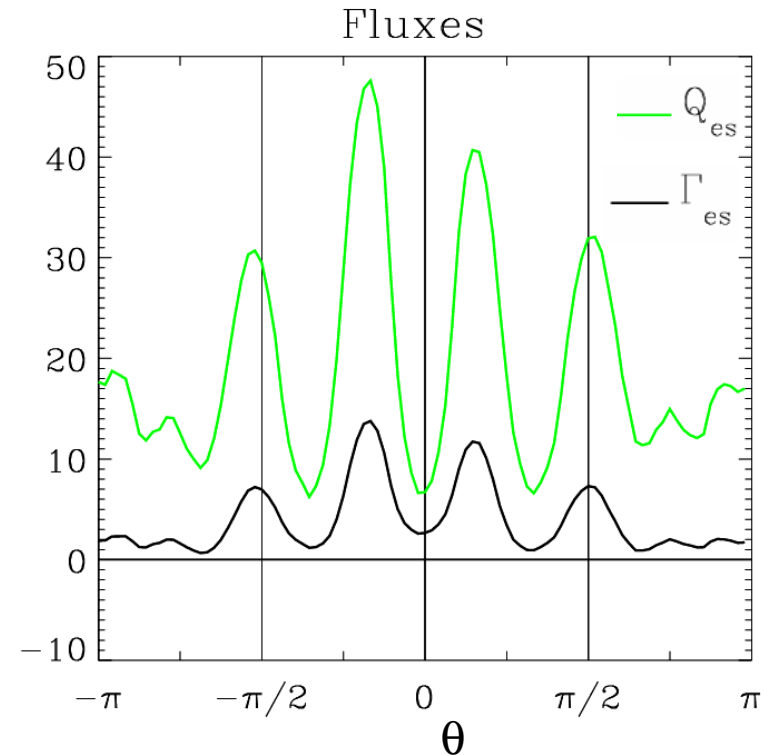
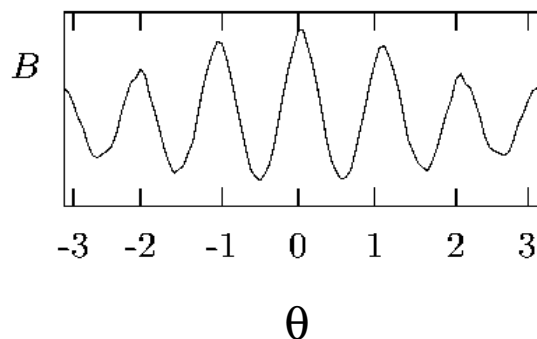
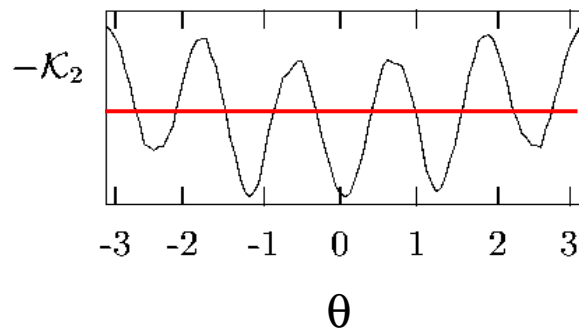
[F. Merz, PhD Thesis 2008]

Like in tokamaks, kinetic electrons reduce the impact of zonal flows.

# Properties of TEM turbulence in W7-X



- Parallel structure: Transport reflects the structure of the magnetic wells
- Regions where bad curvature and magnetic wells overlap dominate transport



- Side remark: Nonlinear and linear mode structure are quite similar; zonal flows are weak
- Potential for turbulence control

# Conclusions



## Gyrokinetic simulations for stellarators:

- Comprehensive (local) gyrokinetic turbulence simulations are becoming feasible; nonlocal codes to be developed
- In principle, 3D shaping allows for fine-tuning:
  - linear drive of microinstabilities
  - nonlinear saturation (e.g., zonal flow physics)
  - destructive interference

These changes affect critical gradients and turbulence onset

- Potential for systematic optimization of turbulent transport needs to be explored in more detail in the future