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**RESEARCH REPORT**  
**NIFS Series**

# Theoretical study of structure of electric field in helical toroidal plasmas

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A set of transport equations is analyzed, including the bifurcation of the electric field. The structure of the electric field is studied by use of the theoretical model for the anomalous transport diffusivities. The steep gradient of the electric field is obtained at the electric domain. The suppression of the anomalous transport diffusivity is studied in the presence of the strong shear of the electric field. The hard transition with the multiple ambipolar solutions is examined in the structure of the radial electric field. The details of the structure of the electric domain interface are investigated.

*Key words* helical plasmas, radial electric field, transport barrier, electric domain

## 1 Introduction

Many types of the improved confinement states have been found in toroidal plasmas. Among the variety of the improved confinement states, the H-mode in tokamaks has been studied most intensively. Through evolution of research, it is widely recognized that the structure of the electric field influences the various improved confinement modes. Nevertheless, quantitative analysis of the generation and the structure of the radial electric field in the high temperature plasmas is far from satisfactory. Study of the confinement mechanisms has also been done for helical plasmas [1].

Recently, the internal transport barrier has been found in electron cyclotron resonance heating (ECRH) plasma in the compact helical system (CHS) and the steep gradient in the profile of the radial electric field has been obtained in the inner region [2]. In Wendelstein7-AS (W7-AS), studies on the change of the electron transport triggered by the neoclassical transport have also been done theoretically [3] and experimentally [4, 5]. More recently, a change in the anomalous transport in the central region has also been reported in W7-AS. To study the existence of the transport barrier in the experimental conditions of helical plasmas, an investigation of the electric field bifurcation is needed. The interface of domains with different electric polarities has been pointed out for helical plasmas. It is well known that neoclassical transport dominant in the bipolar part of the particle flux in helical plasmas and multiple solutions of the ambipolar condition are allowed [6]. To study the interface of neighboring domains with different electric polarities, one-dimensional transport analysis is needed. We have examined the one-dimensional transport equations which describe the temporal evolutions of the density, the electron and ion temperatures, and the radial electric field in a cylindrical heliotron configuration in order to examine the detailed structure of

electric domain [7]. There are two important issues. The first is the formation of the electric field domain, which is associated with the steep gradient of  $E_r$ . The generation of the electric field in helical systems could be investigated more quantitatively because the neoclassical transport is found to play the dominant role in generating the radial electric field [6, 8]. The second is the study of the turbulent transport and the neoclassical energy transport so as to understand the formation of the internal transport barrier.

In order to analyze the structure of the electric field quantitatively, the self-consistent transport study is done in which both the electric field bifurcation and suppression of the anomalous transport are included. Here, we use the transport model (e.g. [1]) for anomalous diffusivities to describe the turbulent plasma. The reduction of the anomalous transport diffusivities is obtained due to the strong electric field shear at the electric domain. The hard transition of  $E_r$  which induces the steep gradient is examined. The neoclassical diffusivities are found to have a peak near the domain interface where the electric field vanishes. In this article, the structure of the electric domain interface is examined in detail.

## 2 One-dimensional model transport equations

In this section, the model equations used here are shown. The cylindrical coordinate is used and  $r$ -axis is taken in the radial cylindrical plasma in this article. The region  $0 \leq r \leq a$  is considered, where  $a$  is the minor radius. The expression for the radial neoclassical flux associated with helical-rippled trapped particle is given as [9]

$$\Gamma_j^{na} = -\epsilon_t^2 \sqrt{\epsilon_h} v_{dj}^2 n_j \int_0^\infty dx x^{\frac{5}{2}} e^{-x} \tilde{\nu}_j \frac{A_j(x, E_r)}{\omega_j^2(x, E_r)}, \quad (1)$$

where  $x \equiv m_j v^2 / (2T_j)$ ,  $A_j(x, E_r) = n'_j / n_j - Z_j e E_r / T_j + (x - 3/2) T'_j / T_j$ ,  $\omega_j^2(x, E_r) = 3\tilde{\nu}_j^2(x) + 1.67(\epsilon_t / \epsilon_h)(\omega_E + \omega_{Bj})^2 + (\epsilon_t / \epsilon_h)^{\frac{3}{2}} \omega_{Bj}^2 / 4 + 0.6 |\omega_{Bj}| \tilde{\nu}_j$  and  $\tilde{\nu}_j(x) = \nu_{thj} / (\epsilon_h x^{\frac{3}{2}})$ . Here, the relations  $\omega_E = -E_r / (rB)$ ,  $\omega_{Bj} = -T_j \epsilon'_h x / (Z_j e r B)$  and  $v_{dj} = -T_j / (Z_j e r B)$  are used. The quantities  $m_j$ ,  $n_j$ ,  $T_j$ ,  $\nu_{thj}$  are the mass, the density, the temperature, the collision frequency using the thermal velocity for the species  $j$  and the parameters  $\epsilon_t$  and  $\epsilon_h$  are the toroidal and helical ripple, respectively. The prime denotes the derivative with respect to the radial direction. This expression for the particle flux is the connection formula and is applicable to both the collisionless and collisional regimes. The total particle flux  $\Gamma^t$  is written as

$$\Gamma^t = \Gamma^{na} - D_a \frac{\partial n}{\partial r}. \quad (2)$$

Here,  $D_a$  is the anomalous particle diffusivity. The energy flux related with neoclassical ripple transport is given as [9]

$$Q_j^{na} = q_j^{na} + \frac{5}{2} \Gamma_j^{na} T_j = -\epsilon_t^2 \sqrt{\epsilon_h} v_{dj}^2 n_j T_j \int_0^\infty dx x^{\frac{7}{2}} e^{-x} \tilde{\nu}_j(x) \frac{A_j(x, E_r)}{\omega_j^2(x, E_r)}. \quad (3)$$

The total heat flux  $Q_j^t$  of the species  $j$  is written as

$$Q_j^t = Q_j^{na} - n\chi_a \frac{\partial T_j}{\partial r}. \quad (4)$$

Here,  $\chi_a$  is the anomalous heat diffusivity. The theoretical model for the anomalous heat conductivity obtained by the eigenvalue problem for the ballooning mode and the interchange mode is adopted and will be explained later. The neoclassical diffusion coefficient for the electric field is expressed by [10]

$$D_{E_r} = -\frac{e}{\epsilon_\perp} \frac{3}{16\sqrt{2}\pi} \frac{Z_j e n_j \nu_{thj} T_j^4}{T_j (Z_j e)^4} \frac{\epsilon_t^4}{\sqrt{\epsilon_h}} \left(1 + \frac{\epsilon_t}{\epsilon_h}\right) \int_{x_b}^{\infty} \frac{dx e^{-x} x^3}{\left(|E_r| + \left|x \frac{T_j}{Z_j e} \epsilon_h'\right|\right)^4}, \quad (5)$$

where  $x_b = [\nu_{thj}/(\epsilon_h (|E_r| + |T_j/(Z_j e) \epsilon_h'|))]^{2/3}$ . The anomalous diffusion coefficient for the radial electric field is denoted by  $D_{Ea}$ .

The equation for the density is

$$\frac{\partial n}{\partial t} = -\frac{1}{r} \frac{\partial}{\partial r} (r\Gamma^t) + S_n, \quad (6)$$

the term  $S_n$  represents the particle source such as the ionization effect. The equation for the electron temperature is given as

$$\frac{3}{2} \frac{\partial}{\partial t} (nT_e) = -\frac{1}{r} \frac{\partial}{\partial r} (rQ_e^t) - \frac{m_e}{m_i} \frac{n}{\tau_e} (T_e - T_i) + P_{he}, \quad (7)$$

where the term  $\tau_e$  denotes the electron collision time and the second term in the right hand side represents the heat exchange between ions and electrons. The term  $P_{he}$  represents the absorbed power due to the ECRH heating and its profile is assumed to be proportional to  $\exp(-(r/(0.2a))^2)$  for simplicity. The equation for the ion temperature is

$$\frac{3}{2} \frac{\partial}{\partial t} (nT_i) = -\frac{1}{r} \frac{\partial}{\partial r} (rQ_i^t) + \frac{m_e}{m_i} \frac{n}{\tau_e} (T_e - T_i) + P_{hi}. \quad (8)$$

The term  $P_{hi}$  represents the absorbed power of ions and its profile is also assumed to be proportional to  $\exp(-(r/(0.2a))^2)$ .

The radial electric field equation in a nonaxisymmetric system is expressed by [10]

$$\frac{\partial E_r}{\partial t} = -\frac{e}{\epsilon_\perp} \sum_j Z_j \Gamma_j^{na} + \frac{1}{r} \frac{\partial}{\partial r} \left( \sum_j Z_j (D_{Ej} + D_{Ea}) r \frac{\partial E_r}{\partial r} \right), \quad (9)$$

where  $\epsilon_\perp$  is the perpendicular dielectric coefficient as  $\epsilon_\perp = \epsilon_0((c^2/v_A^2) + 1)(1 + 2q^2)$ . Here,  $\epsilon_0$  is the dielectric constant in the vacuum,  $c$  is the speed of light,  $v_A$  is the velocity of Alfvén wave and  $q$  is the safety factor. The parameter  $Z_j$  is a charge number of the species  $j$ . The factor  $(1 + 2q^2)$  is introduced from the toroidal effect. Equation (9) is solved together with the density and the temperature (ion and electron) equations (6), (7) and (8).

### 3 Boundary conditions and the model of anomalous transport coefficients

The density, temperature and electric field equations (6)-(9) are solved under the appropriate boundary conditions. We fix the boundary condition at the center of the plasma ( $r=0$ ) such that  $n' = T_e' = T_i' = E_r (= -\phi') = 0$ , where  $\phi$  is the electrostatic potential of the electric field. For the diffusion equation of the radial electric field, the boundary condition at the edge ( $r=a$ ) is chosen as  $\sum_j Z_j \Gamma_j = 0$ . This simplification is employed because the electric field bifurcation in the core plasma is the main subject of this study. The boundary conditions at the edge ( $r=a$ ) with respect to the density are those expected CHS device:  $-n/n' = 0.05(m)$ ,  $-T_e/T_e' = -T_i/T_i' = 0.02(m)$ .

The machine parameters are similar to those of CHS device, such as  $R = 1(m)$ ,  $a = 0.2(m)$ , the toroidal magnetic field  $B = 1(T)$ , toroidal mode number  $m = 8$  and the poloidal mode number  $\ell = 2$ . We set the safety factor and the helical ripple coefficient as  $q = 3.3 - 3.8(r/a)^2 + 1.5(r/a)^4$  and  $\varepsilon_h = 0.231(r/a)^2 + 0.00231(r/a)^4$ , respectively [2]. The particle source  $S_n$  is set to be  $S_n = S_0 \exp((r-a)/L_0)$ , where  $L_0$  is set to be  $0.01(m)$  and the value of  $S_0$  is strongly influenced by the particle confinement time.

The value for the anomalous diffusivities of the particle and the electric field is chosen  $D_a = 10(m^2 s^{-1})$ . This value is set to be constant spatially and temporally. In this study, we adopt the model for the anomalous heat conductivity based on the theory of the self-sustained turbulence due to the ballooning mode and the interchange mode, both driven by the current diffusivity. The reduction of the anomalous transport due to the inhomogeneous radial electric field was reported in the toroidal helical system. The anomalous transport coefficient for the temperatures is given as  $\chi_a = \chi_0/(1 + G\omega_{E1}^2)$ , where  $\chi_0 = F(s, \alpha)\alpha^{\frac{3}{2}}c^2 v_A/(\omega_{pe}^2 q R)$ , where  $\omega_{pe}$  is the electron plasma frequency. The factor  $F(s, \alpha)$  is the function of the magnetic shear  $s$  and the normalized pressure gradient  $\alpha$ , defined by  $s = r q'/q$  and  $\alpha = -q^2 R \beta'$ . For the ballooning mode turbulence for the system with a magnetic well, we employ the anomalous thermal conductivity  $\chi_{a,BM}$  [11]:  $F_{BM} = C/\sqrt{2(1-2s_1)(1-2s_1+3s_1^2)}$  ( $s_1 < 0$ ) and  $F_{BM} = C(1+9\sqrt{2}s_1^{5/2})/(\sqrt{2}(1-2s_1+3s_1^2+2s_1^3))$  ( $s_1 > 0$ ), where  $s_1 = s - \alpha$  for the negative pressure gradient and  $s_1 = \alpha - s$  for the positive pressure gradient. The factor for the suppression due to the electric field shear  $\omega_{E1} = a\tau_{AP}E_r'/(s\tau B)$ ,  $G = 1/(2\alpha^2)$ , where  $\tau_{AP} = a\sqrt{\mu_0 m_i n}/B_p$ . In the case of the interchange mode turbulence [1], the factor  $F$  has been given by  $F_{IM} = 3C(\Omega'/2)^{\frac{3}{2}}(R/a)^{\frac{3}{2}}/(qs^2)$ , where  $\Omega' = (r/R)^2(m/\ell)(r/a)^{-2}((r/a)^4/q)'$  for the anomalous heat conductivity  $\chi_{a,IM}$ . The factor for the suppression due to the electric field shear is  $\omega_{E1} = \tau_{AP}E_r'/B$  and  $G = 0.52D_0^{-1}$ , where  $D_0 = \Omega'\beta'a^2R^2/(2\tau^2)$ . For the standard parameters in CHS experiment, the numerical factor  $C$  is chosen to be 10. We use this value of  $C$  throughout this paper. The greater one of the two diffusivities is adopted,  $\chi_a = \max(\chi_{a,BM}, \chi_{a,IM})$ . The approximation  $D_{Ea} = \chi_a$  is employed, where the validity of this approximation is discussed in ref. [12].

In order to set the averaged temperature of electrons to be around 250(eV) and the density to be around  $1 \times 10^{19}(m^{-3})$ , the absorbed power of electrons is 100(kW) and the coefficient  $S_0$  is  $7 \times 10^{24}(m^{-3}s^{-1})$  for the choice of above values of the anomalous transport coefficients. The averaged ion temperature  $\bar{T}_i$  is chosen to be about  $T_i = 150(eV)$ , where the absorbed power of ions is fixed at 50kW.

#### 4 Results of analysis

Using the parameters and boundary conditions given, we analysis equations (1)-(4). The stationary solutions of the radial electric field are shown in figure 1(a) for  $\bar{n} = 1 \times 10^{19}$ ,  $\bar{T}_e = 250(eV)$  and  $\bar{T}_i = 150(eV)$ . The density and the temperature profiles of the electrons and the ions are shown in figures 1(b) and (c), respectively. In figure 1(c), the dashed curve represents the case of the ion temperature and the full curve shows the profile of the electron temperature, respectively. At the point ( $r = r_T(0.12m)$ ), the transition of the radial electric field is found. The circles in figure 1(a) show the values of the electric field which satisfy the local ambipolar condition for the calculated profiles of the density and the temperatures of figure 1(b) and (c). Multiple solutions are allowed for the local ambipolar condition in the parameter region examined here. We call the hard transition when multiple

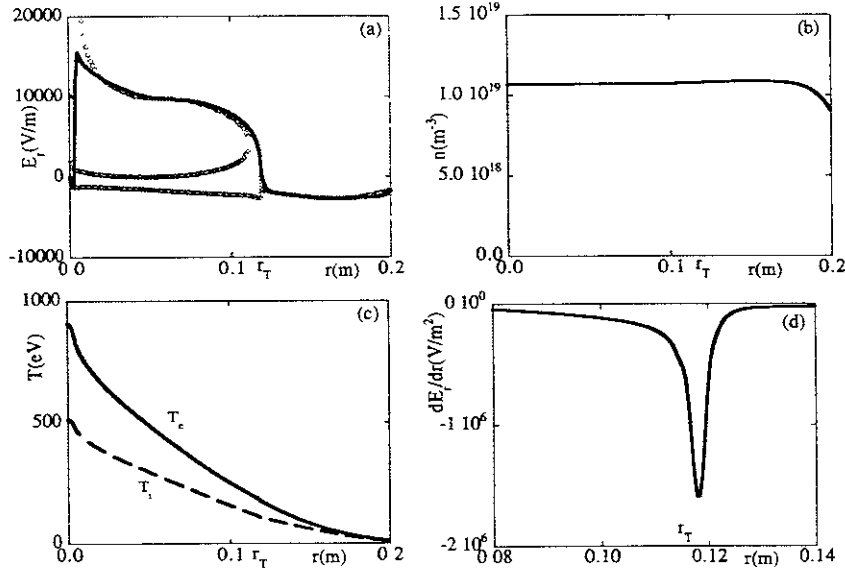


Fig. 1. (a) Radial dependence of the electric field (full curve); circles show the electric field derived from the ambipolar condition. (b) Radial profile of the density and (c) profiles of the temperatures of ions and electrons.

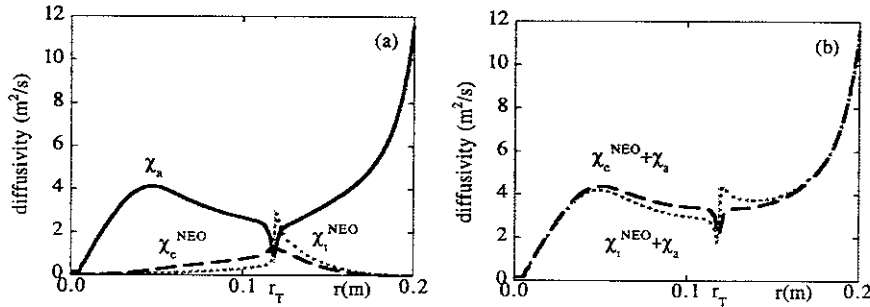


Fig. 2. Radial profiles of the anomalous and neoclassical diffusivities in figure 2(a). In figure 2(b), the sum of the anomalous and neoclassical diffusivities is shown.

solutions exist for the local ambipolar condition. In the case of figure 1(a), the electron root for  $r < r_T$  is sharply connected to the ion root for  $r > r_T$  with a thin layer between them. The transition point should be determined by the Maxwell construction [13]. We confirm that the Maxwell construction is satisfied in the case of figure 1(a). The profile of the derivative of the radial electric field is observed in figure 1(d). The peak at the transition point  $r = r_T$  is found in figure 1(d).

The transport barrier is obtained for the both channels of the neoclassical transport and the anomalous transport, although it is not very clear in both the electron and ion temperature profiles in figure 1(c). In figure 2(a), the anomalous transport diffusivity  $\chi_a$  is shown with the solid line. At the transition point, the reduction is obtained due to the strong electric field shear. The neoclassical diffusivities of electrons  $\chi_c^{NEO}$  and ions  $\chi_i^{NEO}$  are also shown with the dashed line and the dotted line, respectively. In the case of the spatial transition, the electric field goes across zero. Therefore, the neoclassical diffusivities have a peak near the surface where the relation  $E_r \approx 0$ , because they depend on the value of  $E_r$  itself. In figure 2(b), the sum of the anomalous and the neoclassical diffusivities is shown. The case of electrons and the case of ions are obtained with dashed line and the dotted line, respectively. The total suppression can be seen but is small compared with that of the anomalous diffusivity. This is because the neoclassical transport diffusivity has a peak near the radius  $r = r_T$ .

## 5 Study of electric field structure in detail

In this section, we investigate the detail of the structure of the electric field shear in the case of the hard transition discussed in the previous section. When the self-consistent analysis by use of the theoretical model for the anomalous transport coefficient is done, the interesting physical issues are obtained

In figure 1(d), there is the difference between the half widths at the half maximum of the inner side ( $r < r_T$ ) and the outer side ( $r > r_T$ ) in the profile of

the electric field shear. The origin of this asymmetry is discussed in ref. [14]. The quantity related with the area  $r > r_T$  between the lines of  $E_r' = 0$  and  $E_r'$  profile is given as

$$\left| \frac{\partial E_r}{\partial r} \right|_{right}^2 \approx \frac{1}{\epsilon_0 \epsilon_{\perp} D_{Ea}} \int_{E_1}^{E_{u1}} J dE_r, \quad (10)$$

where  $J = e(\Gamma_i^{na} - \Gamma_e^{na})$ ,  $E_1$  is the electric field which is the ion root of the local ambipolar condition and  $E_{u1}$  is in the range of  $E_1 < E_{u1} < E_2$ . Here,  $E_2$  is the value of  $E_r$  at  $r = r_T$ . The quantity related with the area  $r < r_T$  is shown as

$$\left| \frac{\partial E_r}{\partial r} \right|_{left}^2 \approx -\frac{1}{\epsilon_0 \epsilon_{\perp} D_{Ea}} \int_{E_{u2}}^{E_3} J dE_r, \quad (11)$$

where  $E_3$  is the electric field which is the electron root of the local ambipolar condition and  $E_{u2}$  is in the range  $E_2 < E_{u2} < E_3$ . The quantity  $|\partial E_r / \partial r|_{right}^2$  (derived from the ion dominant current) is smaller than that of  $|\partial E_r / \partial r|_{left}^2$  (derived from the electron dominant current). Therefore, the asymmetry is obtained and the half width of the inner side is wider than that of the outer side due to the dependence the neoclassical current on the radial electric field.

Next, we compare the solution with the turbulent transport model and that with the constant  $D_{Ea}$ . In the case of the constant  $D_{Ea}$  [7], the spatial transition occurs to the negative ambipolar solutions before the positive ambipolar solutions of  $E_r$  vanishes when the radial point moves outward (shown in figure 3) and the Maxwell's construction holds at the transition point. However, the transition takes place after the positive ambipolar solutions of  $E_r$  vanishes in figure 1(a). This is because there is the contribution from the diffusion term of the electric field (the second term in the right hand side in equation (9)). The condition for the

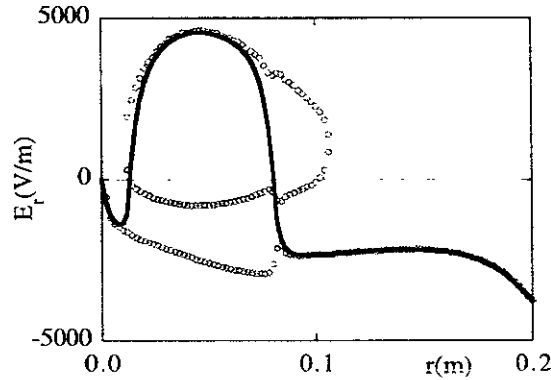


Fig. 3. Profile of the radial electric field in the case of the constant  $D_{Ea}$  (solid line). Circles show the solutions which satisfies the local ambipolar condition.



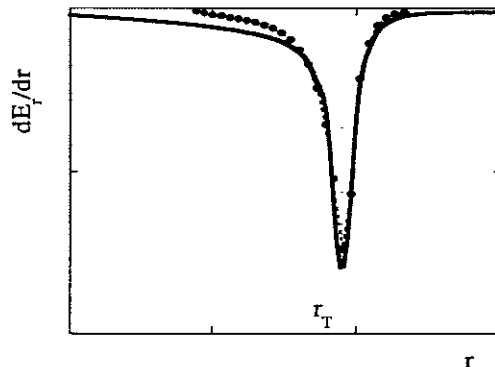


Fig. 4. Schematic figure of the profile of  $E'_r$  in the cases of the theoretical model of  $D_{Ea}$  (solid line) and the constant  $D_{Ea}$  (dashed line).

suppression due to the electric field shear is satisfied where the width in the profile of the electric field shear is smaller than  $0.007(m)$ .

In figure 4, the spatial profiles of the gradient of  $E_r$  are shown in the cases of the anomalous diffusivity  $D_{Ea}$  (explained in Sec. 3) as well as of the constant  $D_{Ea}$  (shown in figure 3). The anomalous diffusivity  $D_{Ea}$  which is reduced due to  $E'_r$  is denoted by  $D_{Ea}(E'_r)$  and the constant  $D_{Ea}$  is denoted by  $D_{Ea}(const.)$ . The solid line represents the case of  $D_{Ea}(E'_r)$  and the dashed line shows the case of  $D_{Ea}(const.)$ , respectively. The values of the axes are in the arbitrary units. The value of  $E'_r$  is adjusted to be the same width at the half maximum in both cases. It has been known that the peak of  $|E'_r|$  and the inverse of the half width depends on  $D_{Ea}^{-1/2}$  when  $D_{Ea}$  is constant [7]. In order to identify the impact of the transport reduction, two profiles (results of figure 1(d) and the stretched profile for the case of the constant  $D_{Ea}$ ) are overlayed in figure 4. The magnitude of the peak of the electric field shear in this study is about twice as that of the case of the constant  $D_{Ea}$  which gives the same half width at the half maximum. In the case of the self-consistent solution, the value of  $|E'_r|$  is larger away from the interface, therefore,  $|E'_r|$  has much prominent tail.

## 6 Summary and Discussions

In this paper, the structure of the radial electric field in helical plasmas is theoretically studied. The temporal and spatial evolutions of the plasma density, the temperatures and the radial electric field are examined. A numerical formula is employed to determine the neoclassical components of particle and heat fluxes in helical plasmas. The analysis is done by use of one-dimensional transport model equations. Theoretical model of the ballooning mode or the interchange mode is adopted for the anomalous heat conductivity and the anomalous diffusion coefficient

of the electric field.

The stationary structure of the radial electric field is shown and the hard transition with the multiple ambipolar  $E_r$  is obtained in this study of  $T_e/T_i \approx 2$ . The connection from the positive electric field (electron root) to the negative electric field (ion root) is seen with the rapid change. The magnitude and the spatial distribution of the transport reduction is examined due to the strong electric field shear. In the case of the electric field interface between the positive  $E_r$  and the negative  $E_r$  regions, the neoclassical transport takes a peak near the interface. When the value of  $T_e$  is much higher than the value of  $T_i$  ( $T_e/T_i \approx 10$ ) and the transition type becomes soft (without multiple ambipolar  $E_r$ ), the gradient of the electric field gets weaker at the electric domain. In that case, no suppression of the anomalous transport diffusivities is obtained and the transport barrier is not seen. The condition for the suppression of the anomalous diffusivities is suggested to be rather high  $T_i$  in addition to the low density and high  $T_e$ . Compared with the previous analysis of the constant  $D_{Ea}$ , the detailed study of the profile of the electric field shear is also done. The difference between the cases of the constant  $D_{Ea}$  and this study in the  $|E'_r|$  profile near the interface is found. The longer tail in the  $|E'_r|$  profile is shown in this study compared to the previous analysis by use of the constant  $D_{Ea}$ .

In CHS device, The spatial transition from the larger positive  $E_r$  to the smaller positive  $E_r$  is observed [2]. Such a spatial transition dose not induce a local peak of  $\chi_j^{NEO}$ , and should be searched for in simulations. The analysis of the dynamics of the electric field is needed to examine the electric pulsation observed in CHS device[15]. These are left for future studies.

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