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Cross Sections for Electron-Impact Induced Transitions Between Excited States in He: $n, n' = 2, 3$ and 4

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CROSS SECTIONS FOR ELECTRON-IMPACT INDUCED TRANSITIONS BETWEEN EXCITED STATES IN He: $n, n' = 2, 3$ AND 4

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Abstract

Cross sections σ and corresponding maxwellian rate coefficients $\langle v\sigma \rangle$ have been calculated for all 153 spin-allowed and spin-forbidden transitions between excited states in He with the principal quantum numbers $n, n' = 2, 3$ and 4 induced by electron impact. Calculations have been performed using Coulomb-Born approximation with exchange (CBE) in the partial wave representation with orthogonalized wavefunctions of the initial and final states in the incident electron energy range from threshold up to 2000 eV for spin-allowed transitions ($\Delta S=0$) and up to 200 eV for spin-forbidden (intercombination, $\Delta S=1$) transitions where the corresponding excitation cross sections are still relatively large. The fitting parameters for σ and $\langle v\sigma \rangle$ of spin-allowed transitions have been obtained. The results are compared with experimental data and other calculations.

[keywords: excitation, electron scattering, partial wave method, model potential, cross section, rate coefficient]

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1. Introduction

A knowledge of excitation cross sections and rate coefficients of He atoms from the ground and excited states is required for many physical applications: gaseous discharges, rare-gas lasers¹⁾, fusion²⁾ and astrophysical^{3,4)} plasmas, diagnostics and heating of plasma by neutral He beams⁵⁾, etc. While the information about excitation in He from the ground state is quite essential (see, e.g., refs.⁵⁻⁸⁾), relatively little is known about excitation from excited states with the principal quantum numbers $n \geq 2$, especially regarding experimental data. In this respect theoretical calculations are of a special interest.

Our aim in this work is to perform calculations of the excitation cross sections and the corresponding rate coefficients between excited ($n, n' = 2, 3$ and 4) states in He in a wide electron-impact energy range: from threshold up to 2000 eV for spin-allowed transitions ($\Delta S=0$) and up to 200 eV for spin-forbidden (intercombination, $\Delta S=1$) transitions.

2. Theoretical approaches

a) Born approximation

In the Born approximation the wavefunctions of the incident and scattered electrons are described by the plane waves $\exp(-ikr)$ and the excitation cross section for transition $0 - 1$ is given by the Fourier components of the electron-atom interaction potential $V_k(r)$ ⁹⁾ *:

$$\sigma^B = \sum_{\kappa} Q_{\kappa}(0-1) \sigma_{\kappa}^B(l_0, l_1) \quad (1)$$

$$\sigma_{\kappa}^B(l_0, l_1) = \frac{8}{(2l_0 + 1)k_0^2} \int_{k_0 - k_1}^{k_0 + k_1} |R^B(q)|^2 \frac{dq}{q^3} [\pi a_0^2] \quad (2)$$

$$R_{\kappa}^B(q) = [(2\kappa + 1) (2l_0 + 1) (2l_1 + 1)]^{1/2} \binom{l_0 l_1 \kappa}{0 0 0} \int_0^{\infty} P_0(r) P_1(r) [j_{\kappa}(qr) - \delta_{\kappa 0}] dr \\ = q^2 \int_0^{\infty} V_{\kappa}(r) j_{\kappa}(qr) r^2 dr \quad (3)$$

$$\kappa = \kappa_{\min}, \kappa_{\min} + 2, \dots, l_0 + l_1; \quad \kappa_{\min} = |l_0 - l_1|, \quad (4)$$

*) Atomic units are used: $e=m=\hbar=1$.

where $P(r)$ is the radial wavefunction of the bound electron, Q_κ is the angular coefficient, V_κ is the interaction matrix element, q is the momentum transfer $q = k_0 - k_1$, $j_\kappa(x)$ is the spherical Bessel function. From the energy conservation law one has

$$E - E' \equiv \frac{k_0^2}{2} - \frac{k_1^2}{2} = \Delta E, \quad k_0 \pm k_1 = \sqrt{2E}(1 \pm \sqrt{1 - \Delta E/E}), \quad (5)$$

where $\Delta E = E_0 - E_1$ is the transition energy, E_0 and E_1 being the binding energies of the initial and final states. E and E' are the energies of the incident and scattered electron, respectively.

The accurate calculations of the Born cross sections in He are given in refs.^{10,11)}.

b) Bethe formula

For dipole (optically allowed) transitions with $\kappa = 1, \Delta l = \pm 1, \Delta S = 0$ induced by electron impact, an approximate formula for the excitation cross section can be obtained from (3) using the expansion:

$$j_\kappa(qr) \approx \frac{q^\kappa}{(2\kappa+1)!!} r^\kappa, \quad qr \ll 1 \quad (6)$$

The result is known as the Bethe formula

$$\sigma = \frac{8f}{E\Delta E} \ln \frac{q_0}{k_0 - k_1} [\pi a_0^2], \quad (7)$$

where f is the oscillator strength of the transition 0 - 1 and q_0 is the cutting-off parameter. The reasonable estimation for q_0 is given by¹²⁾:

$$q_0 = \min(k_0 + k_1, \sqrt{2E_0}) \quad (8)$$

The Bethe formula and its modifications are often used for estimation of the dipole excitation cross sections because of its simplicity, but the accuracy of the Bethe formula is less than that of the Born approximation.

c) Model potential

If the interaction matrix element $V_\kappa(r)$ in (3) is known one can calculate the Born cross sections without knowing the radial wavefunctions $P(r)$. In ref.¹³⁾ a model potential $V^M(r)$ was suggested in the form:

$$V_\kappa^M(r) = \frac{\lambda_\kappa r^\kappa}{(r^2 + r_0^2)^{\kappa+1/2}}, \quad \kappa \neq 0, \quad (9)$$

where r_0 is the cutting-off (effective) radius and λ_κ is the interaction constant. The model potential (9) has the correct asymptotics at $r \rightarrow 0$ and $r \rightarrow \infty$. For dipole transitions ($\kappa=1$) one has

$$V_1^M(r) = \frac{\lambda r}{(r^2 + r_0^2)^{3/2}}, \quad \lambda_i = \left(\frac{3(2l_0+1)}{Q_i} \frac{f}{2\Delta E} \right)^{1/2}, \quad (10)$$

where ΔE is the transition energy.

The sophisticated numerical calculations of the excitation cross sections showed that a reasonable fit of the model potential to the exact one can be achieved if one puts¹⁴⁾

$$r_0 = \frac{n_0^* n_1^*}{z(\Delta + 0.5)}, \quad \Delta = n_1^* - n_0^*, \quad (11)$$

$$n^* = n - \Delta = z(E_{nl} / Ry)^{-1/2}, \quad (12)$$

where E_{nl} is the energy level counted from the ionization limit, n^* is the effective quantum number and Δ is the quantum defect. Here z is the spectroscopic symbol: for neutrals $z = 1$, for positive ions $z > 1$.

With the model potential $V_1^M(r)$ the expression for the Born dipole cross section can be written in a closed analytical form:

$$\sigma = \frac{8f}{E\Delta E} [\Phi(x_{\min}) - \Phi(x_{\max})] [\pi a_0^2], \quad \Phi(x) = (x^2 / 2) [K_0(x)K_2(x) - K_1^2(x)] \quad (13)$$

$$x_{\max, \min} = r_0(k_0 \pm k_1), \quad (14)$$

where $K(x)$ is the MacDonald function, $k_0 \pm k_1$ are given in (5) and f is the oscillator strength. The function $\Phi(x)$ to within 1.5% is fitted by the formula

$$\Phi(x) \approx e^{-2x} \ln \left(2.193 + 0.681 \frac{1 + \ln(1 + 0.8\sqrt{x})}{x} \right) \quad (15)$$

At high electron-impact energies $E \gg \Delta E$, Eq.(13) gives for the cross section:

$$\sigma = \frac{8f}{E \Delta E} \ln \frac{1.36 E^{1/2}}{r_0 \Delta E} [\pi a_0^2], \quad E \gg \Delta E, \quad (16)$$

that corresponds to the excitation rate coefficient

$$\langle v\sigma \rangle = 1.74 \frac{f \beta^{1/2}}{z \Delta} e^{-\Delta E/T} \ln \frac{1.26 z}{\Delta E r_0 \beta^{1/2}} [10^{-7} \text{ cm}^3 \text{ s}^{-1}], \quad \beta = z^2 Ry / T \ll 1 \quad (17)$$

For transitions $n_0 - n_1$, i.e. averaged over the quantum numbers l and m , one can use in (13, 16, 17) the corresponding oscillator strength. In the case of high n -values the Kramers formula is used:

$$f(n_0 - n_1) = \frac{2C}{n_0^2} \left(\frac{n_0 n_1}{\Delta n(n_0 + n_1)} \right)^3, \quad \Delta n = n_1 - n_0, \quad C = 16 / 3\sqrt{3}\pi \approx 1 \quad (18)$$

d) Ochkur approximation

For spin-forbidden transitions with $\Delta S=1$ the Ochkur approximation [15] is used which is similar to the Born approximation:

$$\sigma^O = \sum_{\kappa} \frac{2S_1 + 1}{2(2S_p + 1)} Q_{\kappa}(0-1) \sigma_{\kappa}^O(l_0, l_1) \quad (19)$$

$$\sigma_{\kappa}^O(l_0, l_1) = \frac{8\pi}{(2l_0 + 1)k_0^2} \int_{k_0 - k_1}^{k_0 + k_1} |R_{\kappa}^O(q)|^2 \frac{dq}{q^3} [\pi a_0^2] \quad (20)$$

$$R_{\kappa}^O(q) = [(2\kappa + 1) (2l_0 + 1) (2l_1 + 1)]^{1/2} \begin{pmatrix} l_0 l_1 \kappa \\ 0 0 0 \end{pmatrix}_{k_0} \int_0^{\infty} P_0(r) P_1(r) j_{\kappa}(qr) dr \quad (21)$$

$$\kappa = \kappa_{\min}, \quad \kappa_{\min} + 2, \dots, \quad l_0 + l_1; \quad \kappa_{\min} = |l_0 - l_1|, \quad (22)$$

where S_1 is the spin of an atom in the final state, S_p is the spin of the parent ion. As seen from (21) the integral $R_{\kappa}^O(q)$ does not contain a term with δ -function which describes the interaction of the incident electron with a target nucleus and is of the order of k_0^{-2} . Due to the additional factor q^2/k_0^2 the exchange cross section decreases at large E as

$$\sigma_{\kappa}^O \propto E^{-3}, \quad E \rightarrow \infty, \quad \Delta S = 1. \quad (23)$$

We note that the q -representation of the excitation cross section for forbidden transitions in the Born approximation is only possible in the Ochkur approach. In the general case it is necessary to use the expansion of the wavefunctions on the partial waves of the incident and scattered electrons.

e) Partial wave method

For transitions with a change of spin $\Delta S \neq 0$ it is necessary to take into account the electron exchange effect. The inclusion of this effect in the framework of the Born approximation (Ochkur approach) is applicable only for neutral atoms. Moreover, in many cases it is often required to perform the procedure of unitarization (normalization) of the Born cross sections which is especially important for the intermediate and low energies.

All these effects are included in the so-called generalized Born approximation¹²⁾ using the partial wave representation. Let us consider the excitation of an atom or ion by electron impact:

$$X_z(a_0) + e(E, \lambda_0) \rightarrow X_z^* + e(E_1, \lambda_1), \quad (24)$$

where λ denotes the orbital momenta of the incident and scattered electrons (partial waves). In the first order of the perturbation theory the excitation cross section can be written in the form:

$$\sigma = \sum_{\kappa} Q'_{\kappa}(0-1) \sigma'_{\kappa}(l_0, l_1) + \sum_{\kappa} Q_{\kappa}(0-1) \sigma''_{\kappa}(l_0, l_1) \quad (25)$$

The first sum in (25) describes the contribution of direct and interference terms for which the angular parts Q are exactly the same, while the second sum is connected with exchange excitation. The angular coefficients Q depend only on all angular (orbital and spin) momenta of an atom or ion and a type of the coupling scheme (see ref.¹²⁾). The cross sections σ_{κ} are the one-electron cross sections depending only on the quantum numbers nl of the bound electron and the incident electron energy E . In the case of intercombination transitions with $\Delta S=1$ the first sum in (25) equals to zero, so the transitions take place mainly due to the electron exchange effects.

The cross sections σ_{κ} can be written in the form:

$$\sigma'_{\kappa}(l_0, l_1) = \frac{4}{(2l_0+1)(2\kappa+1)k_0^2} \sum_{\lambda} R_{\kappa}^d (R_{\kappa}^d - R_{\kappa}^s) [\pi a_0^2] \quad (26)$$

$$\sigma''_{\kappa}(l_0, l_1) = \frac{4}{(2l_0+1)(2\kappa+1)k_0^2} \sum_{\lambda} (R_{\kappa}^s)^2 [\pi a_0^2] \quad (27)$$

$$R_{\kappa}^s = \sum_{\kappa'} (-1)^{l_0+l_1+\kappa'} (2\kappa+1) \begin{Bmatrix} \kappa l_0 l_1 \\ \kappa' l_0 l_1 \end{Bmatrix} \quad (28)$$

$$R_{\kappa}^d = [(2l_0 + 1)(2l_1 + 1)(2\lambda_0 + 1)(2\lambda_1 + 1)]^{1/2} \begin{pmatrix} l_0 l_1 K \\ 000 \end{pmatrix} \begin{pmatrix} \lambda_0 \lambda_1 K \\ 000 \end{pmatrix} \times 2 \iint F_{k_0 \lambda_0}(r'') F_{k_1 \lambda_1}(r'') \frac{r''^{\kappa}}{r''^{\kappa+1}} P_0(r') P_1(r') dr' dr'' \quad (29)$$

$$R_{\kappa''}^e = [(2l_0 + 1)(2l_1 + 1)(2\lambda_0 + 1)(2\lambda_1 + 1)]^{1/2} \begin{pmatrix} l_0 \lambda_1 K'' \\ 000 \end{pmatrix} \begin{pmatrix} \lambda_0 l_1 K'' \\ 000 \end{pmatrix} \times 2 \iint F_{k_0 \lambda_0}(r'') F_{k_1 \lambda_1}(r'') \frac{r''^{\kappa''}}{r''^{\kappa+1}} P_0(r') P_1(r') dr' dr'' \quad (30)$$

Here $P(r)$ are the radial wavefunctions of the bound electron, $F(r)$ are the radial wavefunctions of the incident and scattered electrons; values of k_0 and k_1 satisfy Eq. (5). The indexes κ and κ'' are changed in the limits given by the properties of 3j- and 6j-symbols :

$$\kappa_{\min} \leq \kappa \leq \kappa_{\max}, \quad \kappa''_{\min} \leq \kappa'' \leq \kappa''_{\max} \quad (31)$$

$$\kappa_{\min} = \max(|l_0 - l_1|, |\lambda_0 - \lambda_1|), \quad \kappa_{\max} = \min(l_0 + l_1, \lambda_0 + \lambda_1), \quad (32)$$

$$\kappa''_{\min} = \max(|\lambda - l_0|, |l_1 - \lambda_0|), \quad \kappa''_{\max} = \min(l_0 + \lambda_1, l_1 + \lambda_0). \quad (33)$$

Eqs. (25-33) represent the Coulomb-Born approximation if the wavefunctions of the incident and scattered electrons are the Coulomb functions, the radial parts $F_{kl}(r)$ of which satisfy the equations:

$$\left[\frac{d^2}{dr^2} - \frac{\lambda(\lambda+1)}{r^2} + \frac{z-1}{r} + k^2 \right] F_{kl}(r) = 0, \\ F_{kl}(r) = 0, \quad r \rightarrow 0, \\ F_{kl}(r) \approx k^{-1/2} \sin \left(kr + \frac{z-1}{k} \ln(2kr) - \frac{\pi\lambda}{2} + \delta_{\lambda} \right), \quad r \rightarrow \infty \quad (34)$$

where δ_{λ} is the phase shift. For neutral targets ($z=1$) the function $F_{kl}(r)$ becomes the component $j_{\lambda}(kr)$ of the plane wave and the CB approximation becomes the Born approach in the partial wave representation.

At threshold energy $E=E_{th}=\Delta E$, the cross sections (25-33) are zero, $\sigma_{th}=0$, for neutral atoms, and $\sigma_{th}=\text{constant}$ for ions. CBE method provides the following asymptotics for excitation cross sections at $E \rightarrow \infty$:

$$\sigma \propto \begin{cases} (\ln E)/E, & \Delta S = 0, \Delta I = \pm 1 \\ E^{-1}, & \Delta S = 0, \Delta I \neq \pm 1 \\ E^{-3}, & \Delta S = 1. \end{cases} \quad (35)$$

In general, the total wavefunctions of the system electron+ion in the initial and final states are not orthogonal because the bound $P(r)$ and continuous $F(r)$ wavefunctions correspond to the different potentials of z/r and $(z-1)/r$ types. This disadvantage can be removed by introducing the orthogonalized wavefunctions $\Phi_{k\lambda}(r)$ (see ref.¹⁵):

$$\begin{aligned}\Phi_{k_0\lambda_0}(r) &= F_{k_0\lambda_0}(r) - \langle F_{k_0\lambda_0}(r) | P_1 \rangle P_1 \delta_{l_1\lambda_0} \\ \Phi_{k_1\lambda_1}(r) &= F_{k_1\lambda_1}(r) - \langle F_{k_1\lambda_1}(r) | P_0 \rangle P_0 \delta_{l_0\lambda_1}\end{aligned}\quad (36)$$

Therefore, we will call CBE approximation the first order the approach (25-34) with the Coulomb functions (34) for the direct part R^d and with the orthogonalized functions (36) for the exchange part R^e . The CBE method defined this way provides for intercombination transitions ($\Delta S=1$) the same accuracy as the Born approximation for spin-allowed transitions ($\Delta S=0$). For multicharged ions ($z \gg 1$) the functions F and Φ practically coincide because

$$\langle F_{kl} | P_{nl} \rangle \propto z^{-1}$$

3. Comparison with experiment and other calculations

In this work calculations of the excitation cross sections between excited states in He have been performed by the ATOM code using CBE approximation (25-34) in the partial wave representation (see ref.⁹ in detail). The results are shown in Figs. 1-153 in comparison with available experimental data and calculations.

In this work the calculated CBE excitation cross sections σ and corresponding rate coefficients $\langle v\sigma \rangle$ for spin-allowed transitions ($\Delta S = 0$) are fitted by approximation formulae:

$$\sigma = \frac{\pi a_0^2}{2l_0 + 1} \left(\frac{Ry}{DE} \right)^2 \left(\frac{E_1}{E_0} \right)^{3/2} \frac{C}{u + \varphi} \left(\frac{u}{u + \alpha} \right)^{1/2} \quad (37)$$

$$\langle v\sigma \rangle = \frac{10^{-8} \text{ cm}^3 \text{s}^{-1}}{2l_0 + 1} \left(\frac{Ry E_1}{DE E_0} \right)^{3/2} e^{-\Delta E/T} \frac{A \beta^{1/2} (\beta + 1)(\alpha \beta + 1)^{-1/2}}{\beta + \chi} \quad (38)$$

$$\alpha = \Delta E / DE, \quad u = (E - \Delta E) / DE, \quad \beta = DE / T, \quad (39)$$

where C , φ , A and χ are the fitting parameters, E_0 and E_1 are the atomic energy levels of the initial and final states counted from the ionization limit, ΔE is the excitation energy. In this work a scaling value $DE=5\text{Ry}$ is used. The reduced electron energy u and the temperature β are changed in the limits:

$$0.02 \leq u \leq 16.0, \quad 0.25 \leq \beta \leq 8.0, \quad E_{\max} = 2000 \text{ eV}. \quad (40)$$

The fitting parameters C , φ , A and χ for triplet-triplet transitions and singlet-singlet transitions are given in Tables 1 and 2, respectively. The oscillator strengths f also calculated by the

ATOM code are given in the Tables. Errors (in %) of fittings by Eqs. (37) and (38) are presented in the 6th and 9th columns, respectively.

The present results are compared with the following data:

Flannery et al. (1975) - a ten-channel eikonal approximation,
Fon et al. (1981) - the five-state R-matrix calculations,
Badnell (1984) - Hartree-Fock approximation with orthogonalized wavefunctions of the core and valence electron,
Berrington et al. (1985) - an R-matrix calculation with eleven lowest target states included,
Mathur et al. (1987) - a distorted wave approximation (DWA),
Kingston (1992) - an R-matrix calculation,
Bray et al. (1993) - DWA,
de Heer et al. (1995) - preferred data obtained from compilation;
Rall et al., (1989) - experiment.

As seen from the Figures, some dipole cross sections have the double-peak structure (e.g., 2^1S-3^1P , 2^1S-4^1P , 2^1P-4^1S , 3^3P-3^3D , 3^3P-4^3D , 4^3S-4^3P transitions). Our calculations show that the additional maximum at low electron energy is connected with the strong influence of the exchange effect which is very important for He-like systems. In Figs. 154-159 the contribution of the pure exchange part in (25) (with zero direct and interference parts $\sigma_{\kappa} = 0$) is shown together with the total excitation cross sections and the model cross sections (13,14) also calculated by the ATOM code.

In Figs. 160-170 a comparison of CBE results with Ochkur approximation is given for some intercombination transitions ($\Delta S=1$). It is seen that the pure Ochkur approximation Eqs. (19-22) can be used at relatively high (as compared to ΔE) incident electron energies $E > 10-20$ eV where the intercombination cross sections have the asymptotic $\sigma \propto E^{-3}$.

4. Conclusion

A comparison of the calculated excitation cross sections for He performed in this work by the CBE method using orthogonalized wavefunctions showed that at electron energies $E > 20$ eV our results are close to recommended data and sophisticated calculations. At low energies $E < 20$ eV our cross sections are relatively high as compared to the other calculations. However, to make some definite decision the further experiments have to be carried out for transitions between excited states in He.

Table 1. Transition energies ΔE (eV), oscillator strengths f , fitting parameters, Eqs.(37-40), and effective radius r_0 , Eq.(11), for triplet-triplet transitions in He.

Transit.	ΔE (eV)	f	C	Φ	Err. (%)	A	χ	Err. (%)	$r_0(a_0)$
2s-2p	1.14	0.539	1.46×10^3	0.224	12	1.13×10^3	0.24	6	4.36
	2.89			54.2	19	87.0	0.624	5	
	3.19			78.8	50	57.8	0.0983	13	2.84
	3.25			143	25	258	0.712	2	
	3.77			25.5	35	48.8	0.726	2	
	3.89			59.5	70	45.7	0.106	11	2.42
	3.91			79.5	30	169	0.869	3	
	3.92			12.3	25	38.1	1.50	12	
2p-3s	1.75	0.069	482	0.475	12	260	0.125	20	4.15
	2.04			259	20	385	0.572	7	
	2.11			4.85×10^3	25	2.77×10^3	0.120	20	3.72
	2.63			105	40	76.4	0.171	15	3.17
	2.74			119	20	230	0.801	1	
	2.77			1.59×10^3	40	1.28×10^3	0.206	10	3.02
	2.77			119	40	249	0.786	1	
	8.38 $\times 10^{-3}$								
3s-3p	0.288	0.89	9.11×10^3	0.162	30	7.93×10^3	0.285	15	10.7
	0.355			343	2	638	0.793	3	
	0.875			202	2	320	0.657	10	
	0.989			176	60	180	0.252	10	6.11
	1.02			160	20	285	0.716	5	
	1.02			203	20	43	0.919	1	
3p-3d	0.0664	0.112	1.59×10^4	5.44×10^{-2}	30	1.89×10^4	0.441	10	15.6
	0.587			2.44×10^3	26	1.62×10^3	0.181	18	8.58
	0.700			909	3	1.30×10^3	0.556	9	
	0.729			7.86×10^3	17	4.80×10^3	0.147	20	7.50
	0.730			1.78×10^3	10	3.10×10^3	0.748	5	
3d-4s	0.520	0.022	84.8	6.69×10^{-3}	12	172	0.890	1	
	0.634			516	60	498	0.252	12	8.22
	0.662			1.25×10^3	7	1.58×10^3	0.453	12	
	0.663			3.52×10^4	18	1.96×10^4	0.121	25	7.98
4s-4p	0.114	1.21	2.90×10^4	0.108	25	3.09×10^4	0.356	12	19.9
	0.142			1.31×10^3	2	2.49×10^3	0.822	4	
	0.143			211	7	439	0.916	1	
4p-4d	0.0281	0.20	6.65×10^4	0.0286	18	8.79×10^4	0.494	8	27.8
	0.0292			1.17×10^3	4	2.26×10^3	0.842	3	
4d-4f	0.00105	3.88 $\times 10^{-3}$	8.51 $\times 10^4$	5.74×10^{-3}	17	1.44×10^5	0.670	4	31.8

Table 2. Transition energies ΔE (eV), oscillator strengths f , fitting parameters Eqs.(37-40) and effective radius r_0 , Eq. (11), for singlet-singlet transitions in He.

Transit.	ΔE (eV)	f	C	ϕ	Err. (%)	A	χ	Err. (%)	$r_0(a_0)$
2s-2p	0.565	0.346	1.79×10^3	0.141	13	1.61×10^3	0.302	14	4.36
	2.30			70.7			0.571		
	2.46			309			0.0214		
	2.46			209			0.572		
	3.05			30.6			0.602		
	3.12			160			0.0320		
	3.12			76.7			0.603		
	3.12			21.7			0.676		
2p-3s	1.74	0.044	340	0.690	20	156	0.0835	25	4.26
	1.89			299			0.523		
	1.89			6.32×10^3			0.111		
	2.49			7.90×10^3			0.0971		
	2.56			82.7			0.662		
	2.56			139			218		
	2.56			1.96×10^3			0.195		
	2.56			172			0.591		
3s-3p	0.154	0.571	1.10×10^4	0.106	20	1.11×10^4	0.359	12	13.3
	0.154			291			0.772		
	0.752			238			0.650		
	0.816			775			0.0976		
	0.816			341			0.712		
	0.816			262			0.770		
	0.60			1.50×10^3			0.154		
	0.66			989			0.546		
3p-4s	0.66	0.62	1.09×10^4	0.344	40	6.87×10^3	0.159	20	8.00
	0.66			1.94×10^3			0.722		
	0.599			51.1			0.88.6		
	0.66			306			0.323		
	0.66			1.28×10^3			0.441		
	0.66			3.46×10^4			0.120		
	0.0627	0.783	3.59×10^4	0.0620	40	4.20×10^4	0.428	5	24.0
	0.0627			1.21×10^3			0.821		
	0.0636			168			0.865		
4d-4p	9.93×10^{-6}	4.20x10 ⁻⁵	7.85×10^5	0.0418	100	2.65×10^5	0.162	10	31.8
	8.51×10^{-4}			3.16×10^4			0.676		
4f-4p	8.18×10^{-4}		1.03×10^3	6.64×10^{-3}	1	1.98×10^3	0.870	3	

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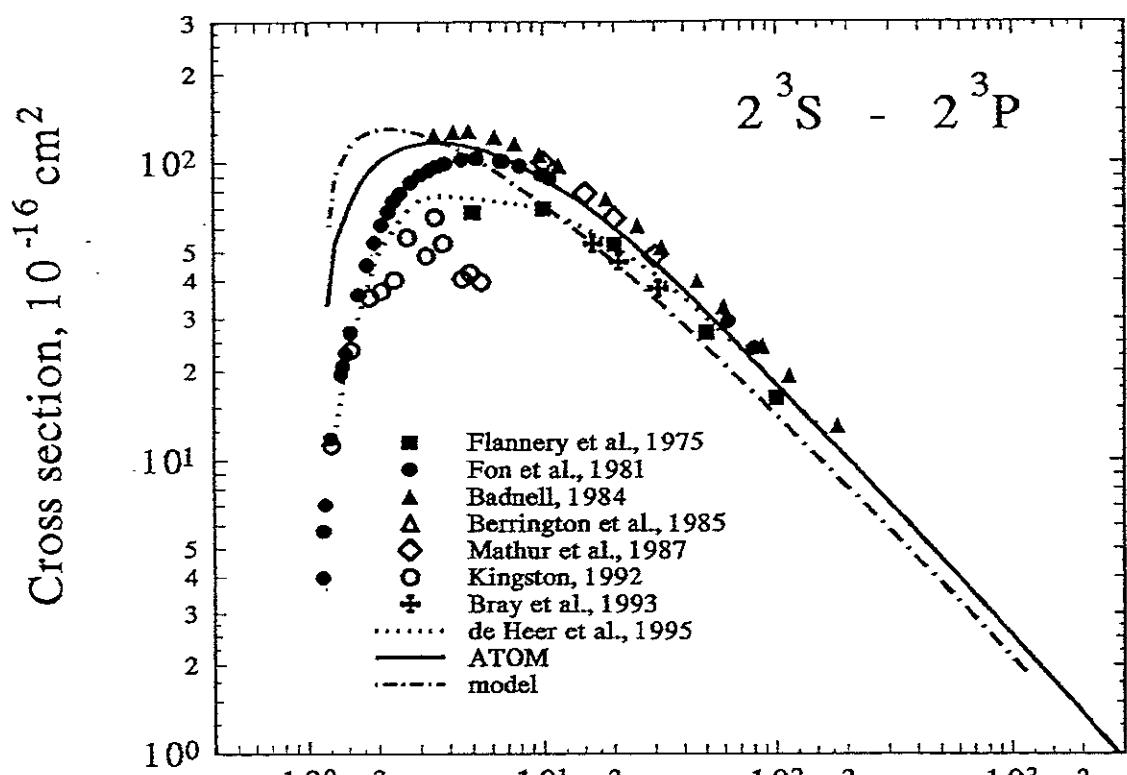


Fig.1 Electron energy, eV

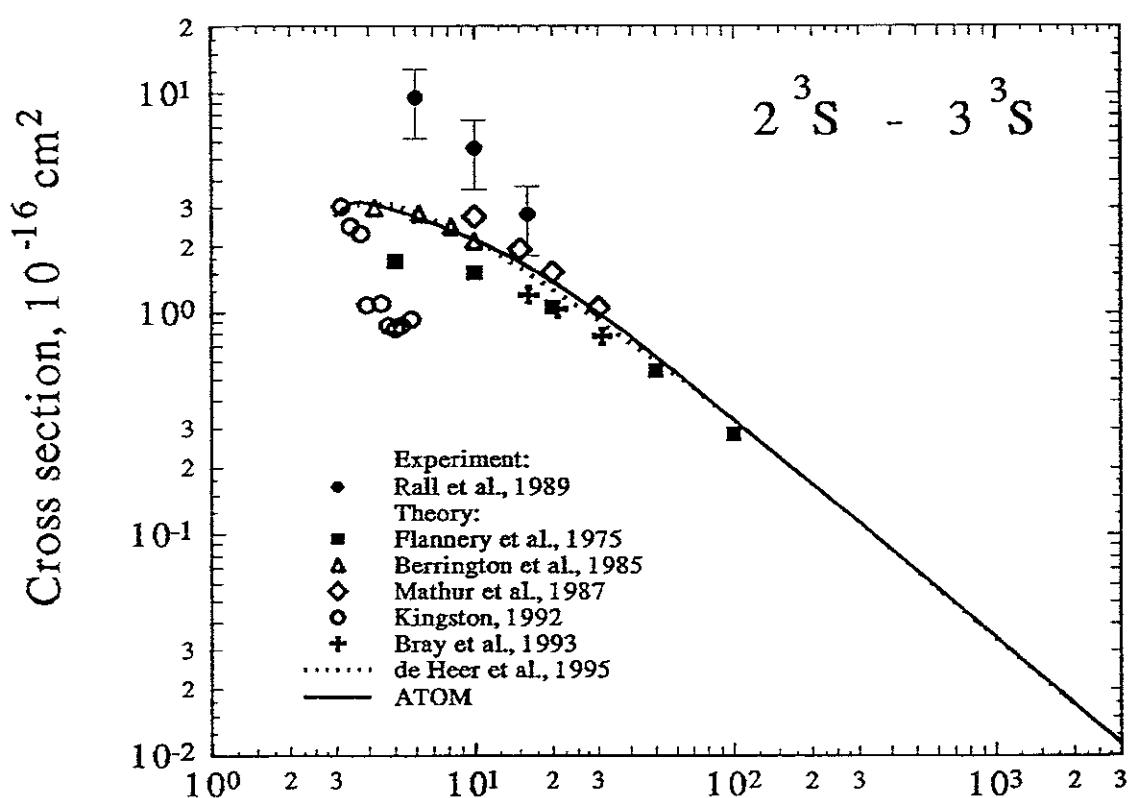


Fig.2 Electron energy, eV

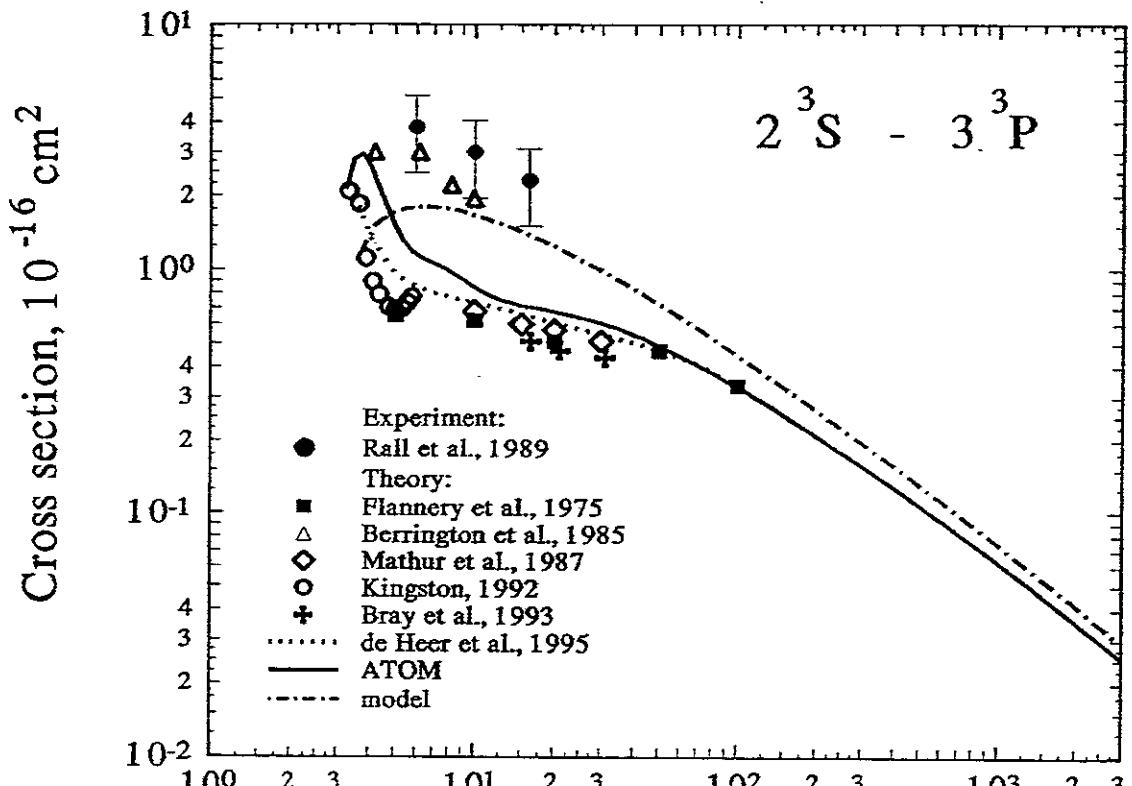


Fig.3 Electron energy, eV

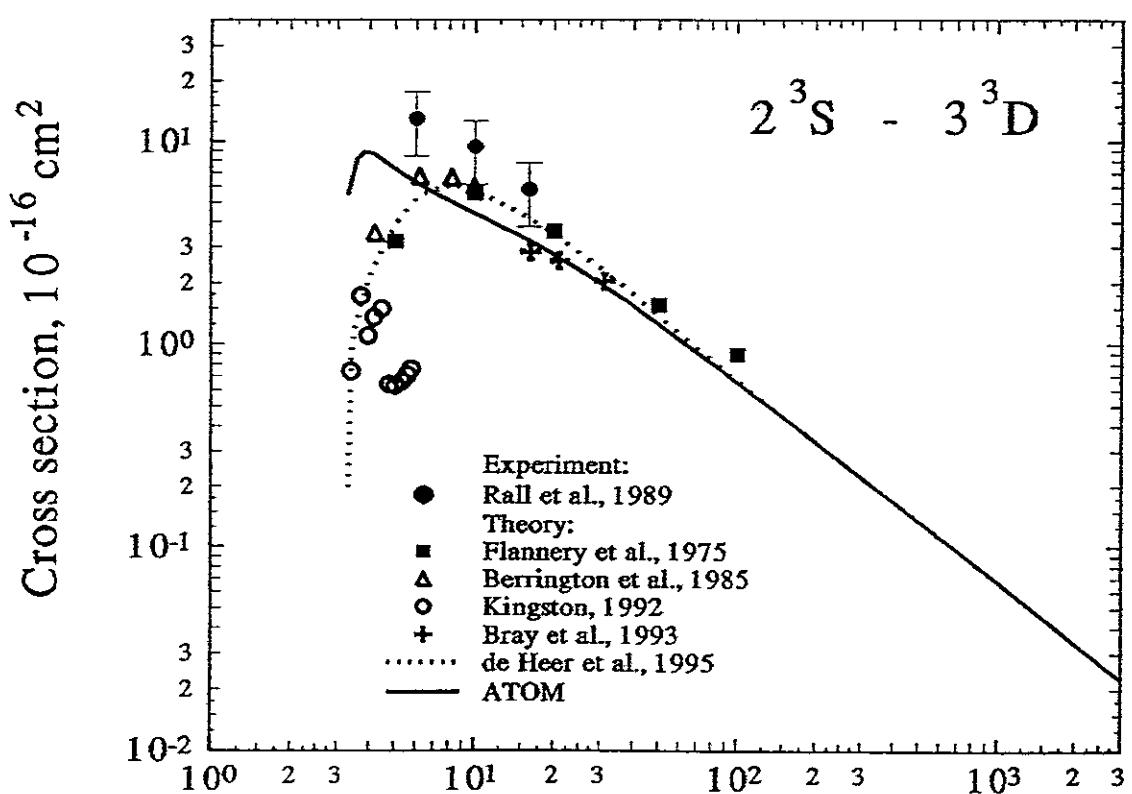


Fig.4 Electron energy, eV

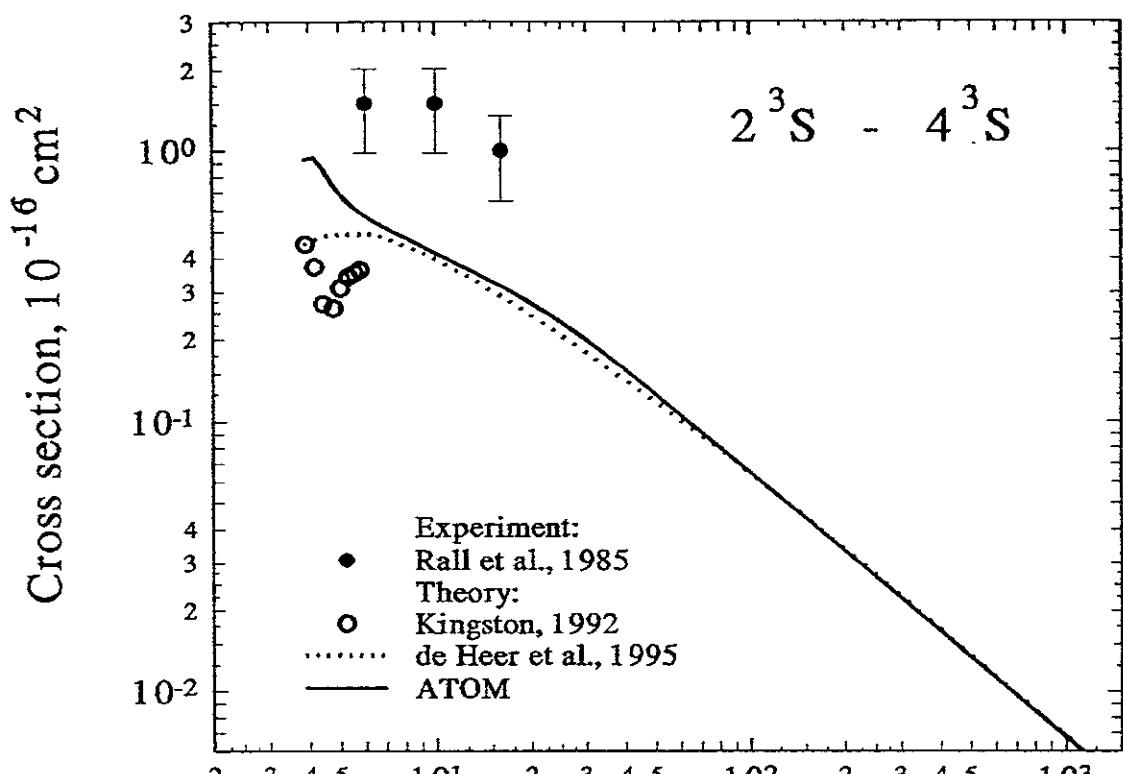


Fig.5

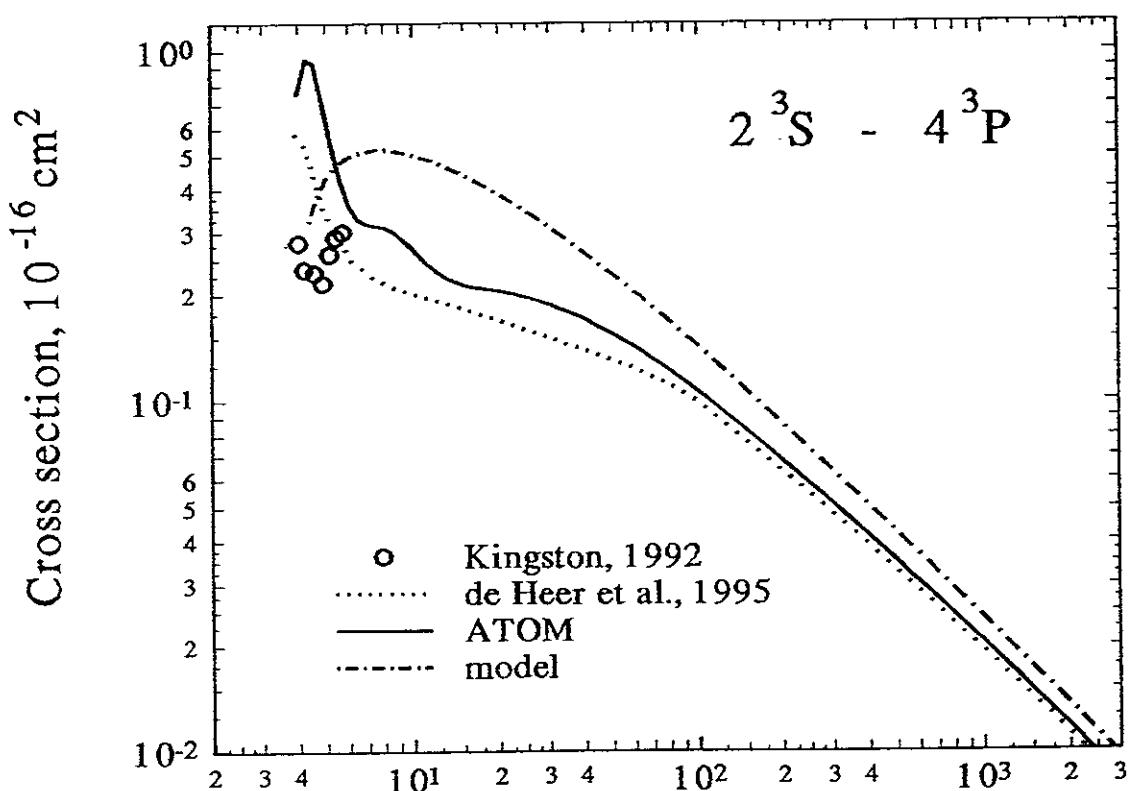


Fig.6

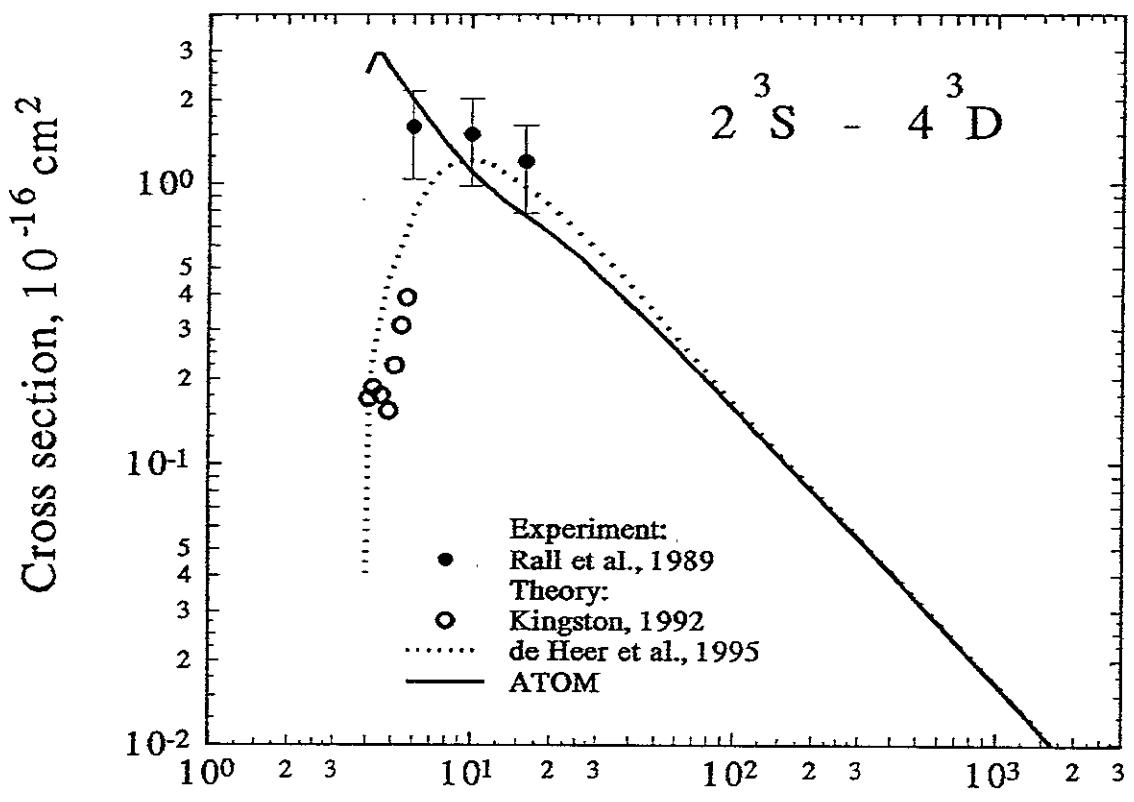


Fig.7 Electron energy, eV

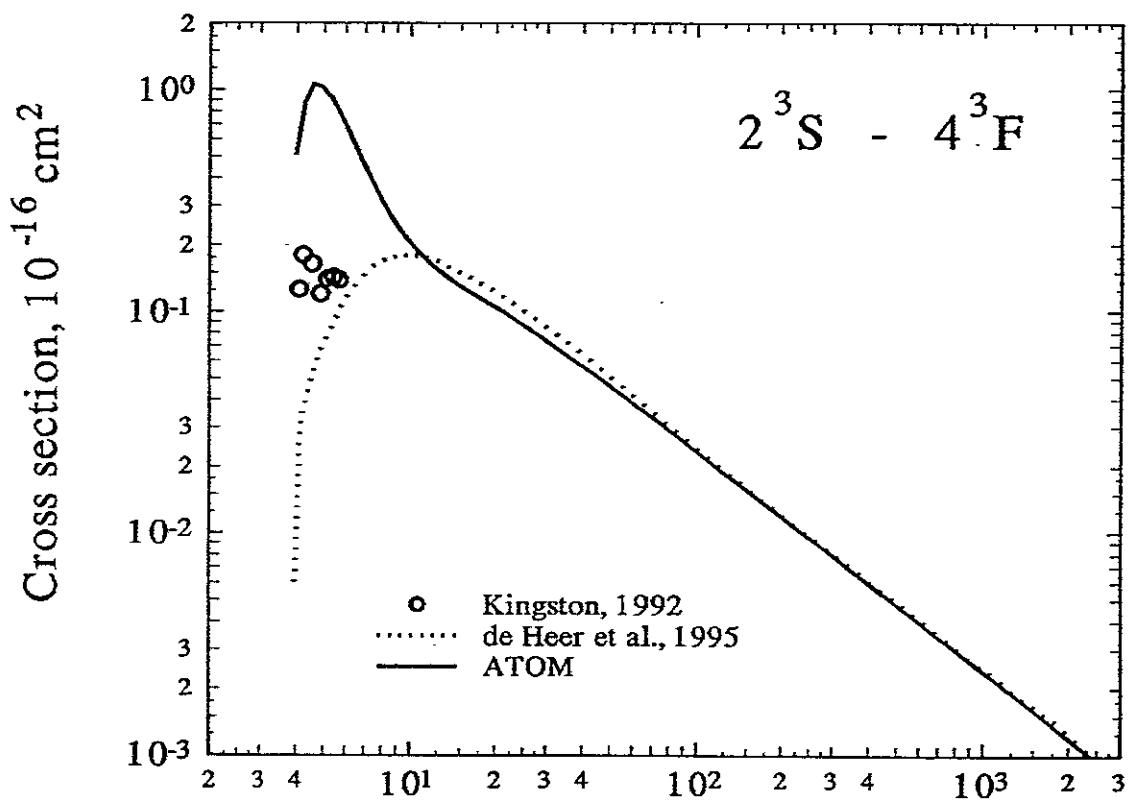


Fig.8 Electron energy, eV

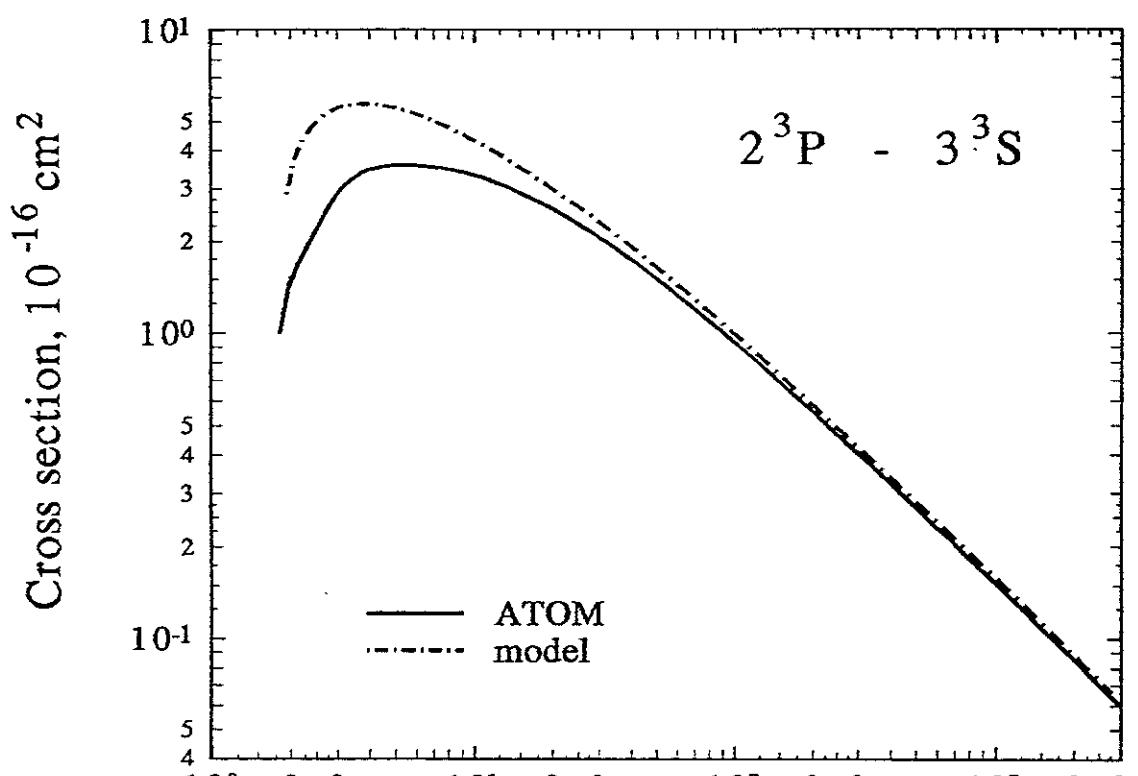


Fig.9 Electron energy, eV

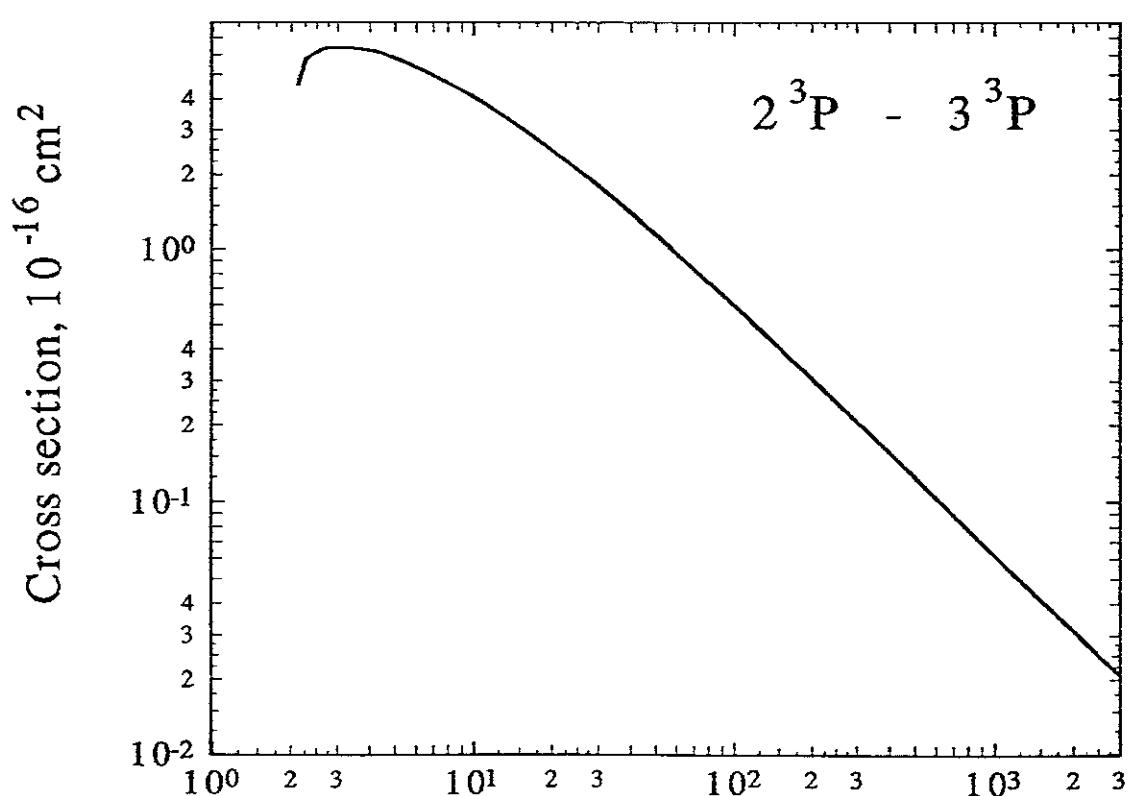


Fig.10 Electron energy, eV

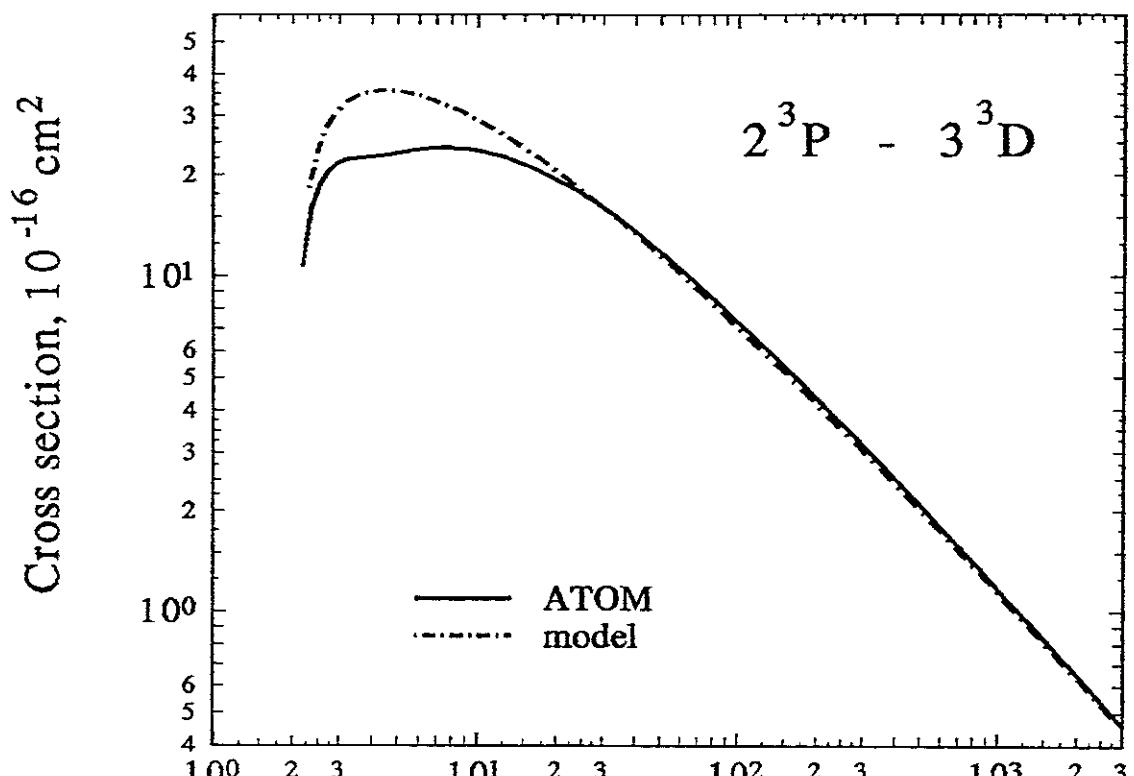


Fig.11 Electron energy, eV

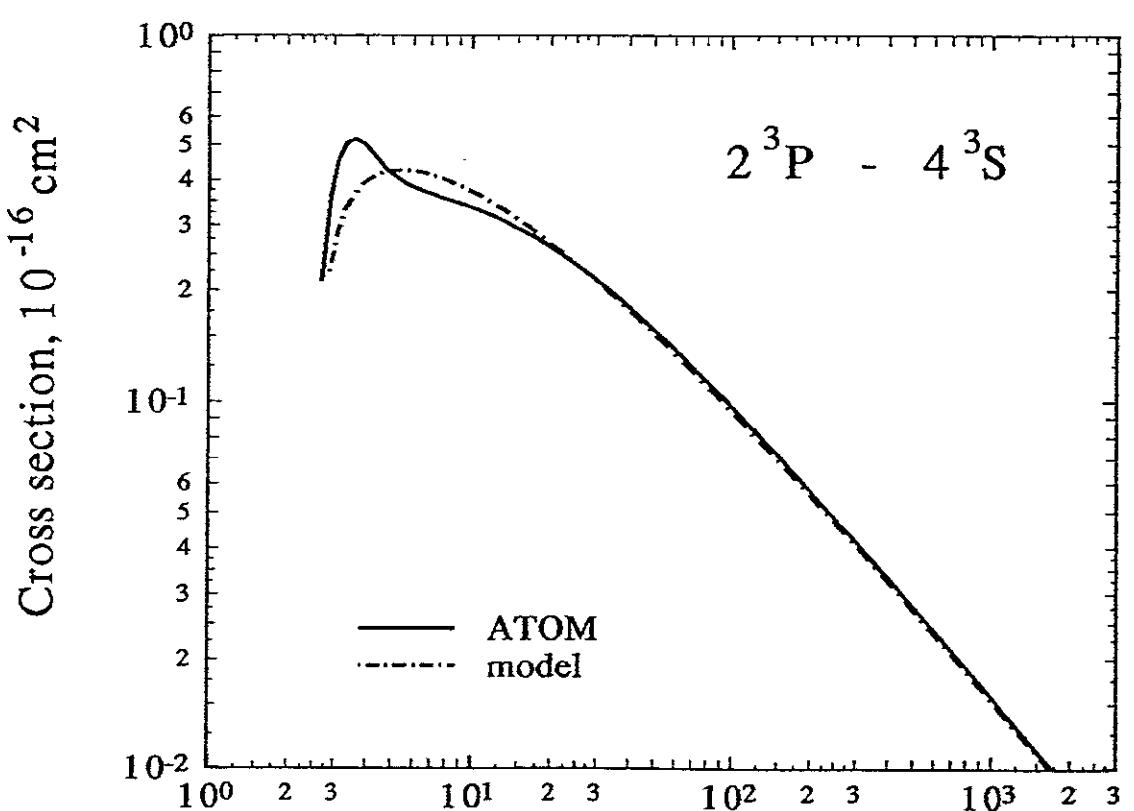


Fig.12 Electron energy, eV

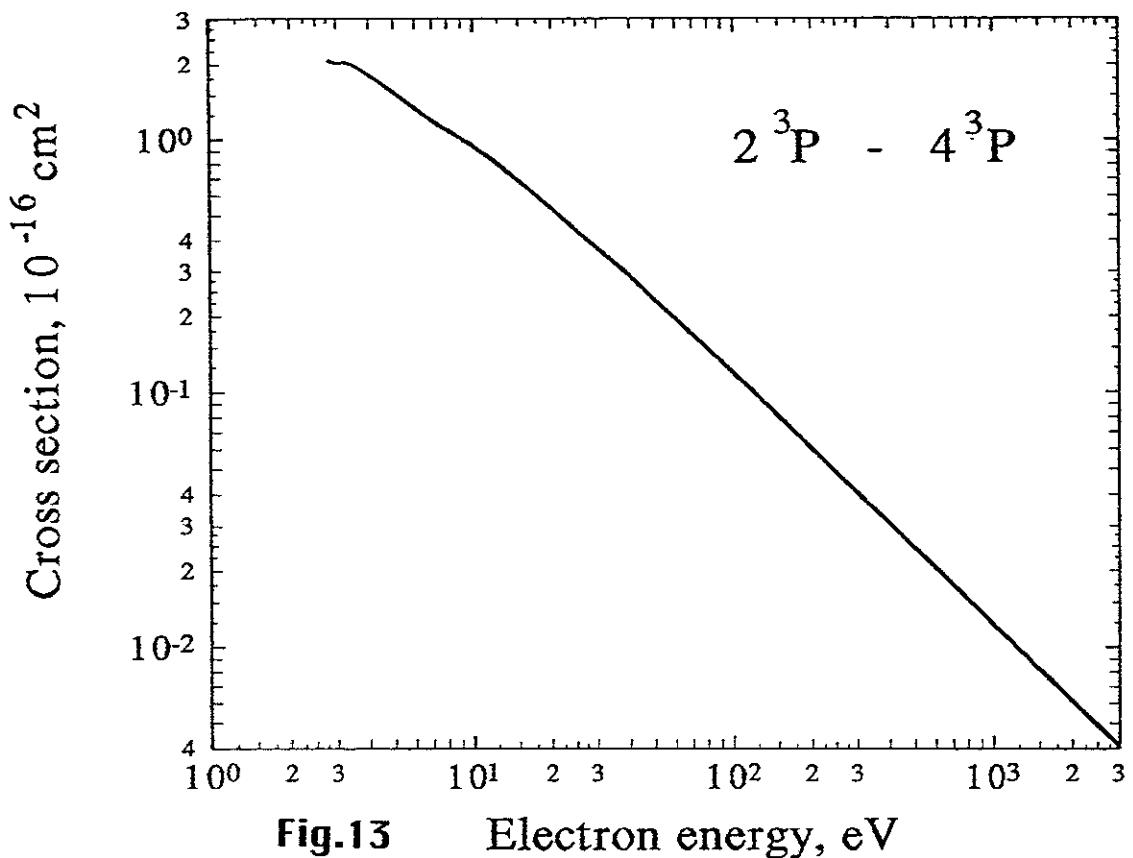


Fig.13 Electron energy, eV

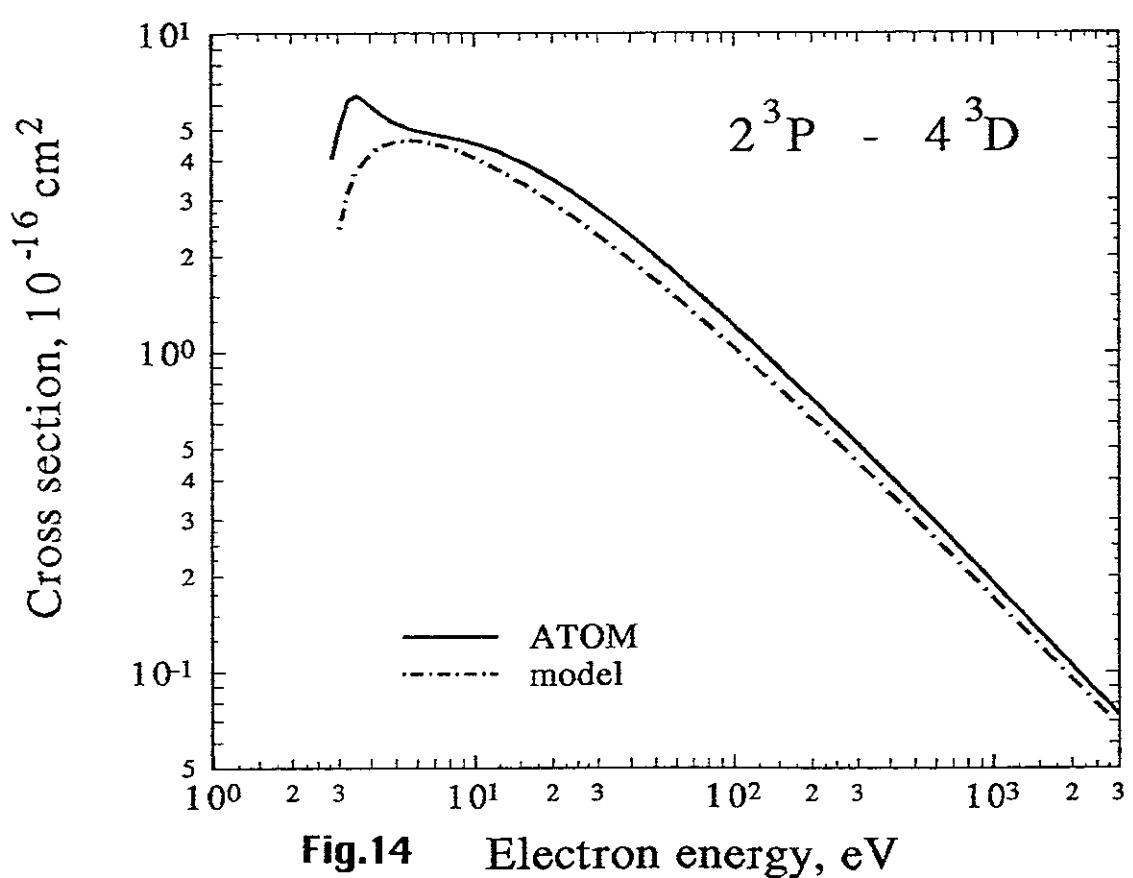


Fig.14 Electron energy, eV

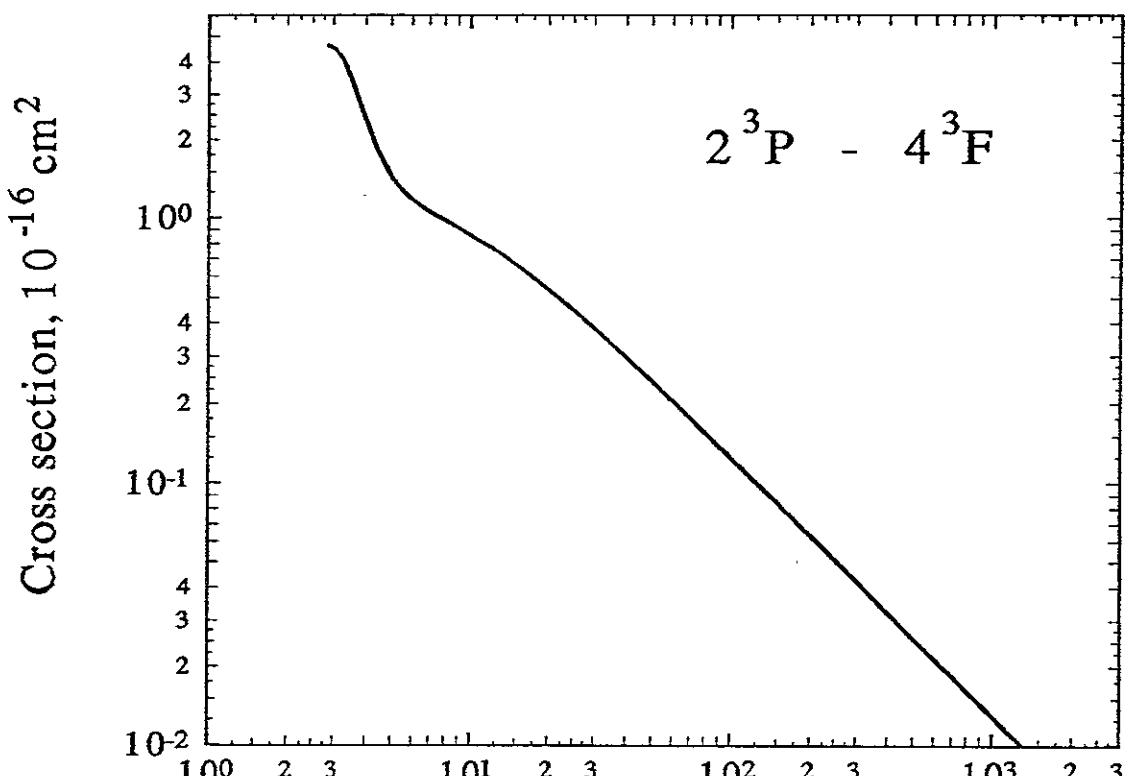


Fig.15 Electron energy, eV

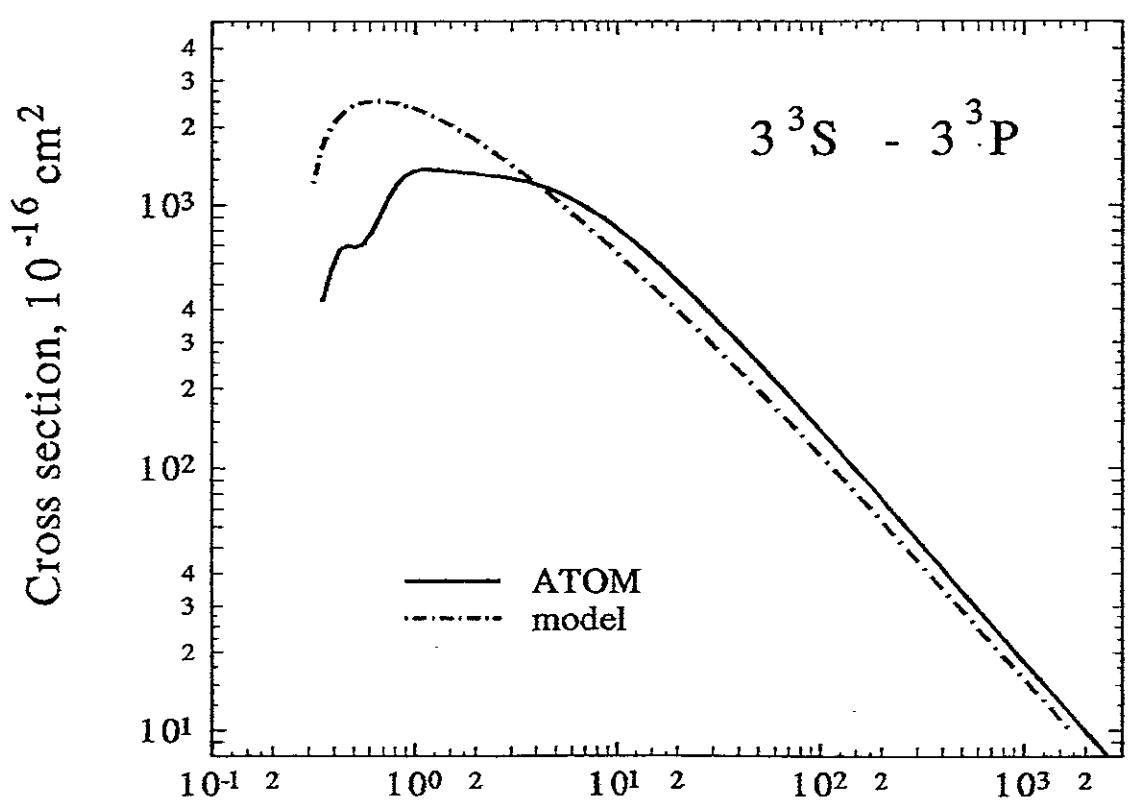


Fig.16 Electron energy, eV

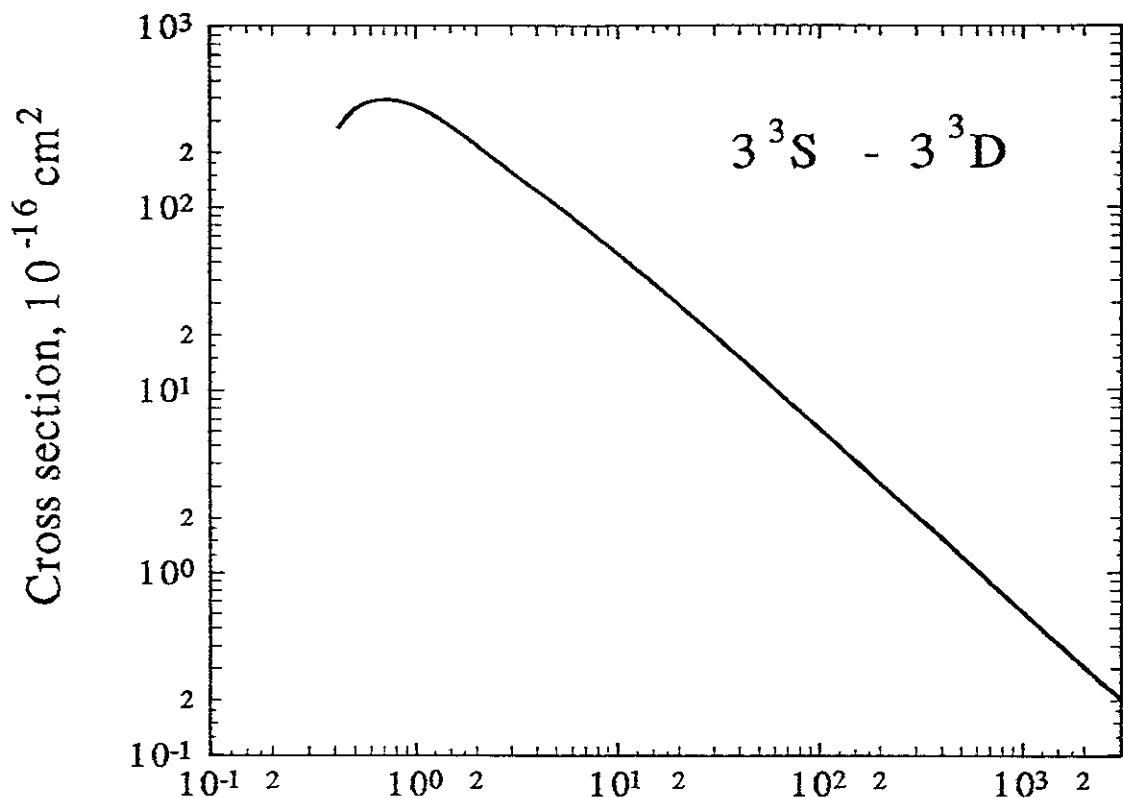


Fig.17 Electron energy, eV

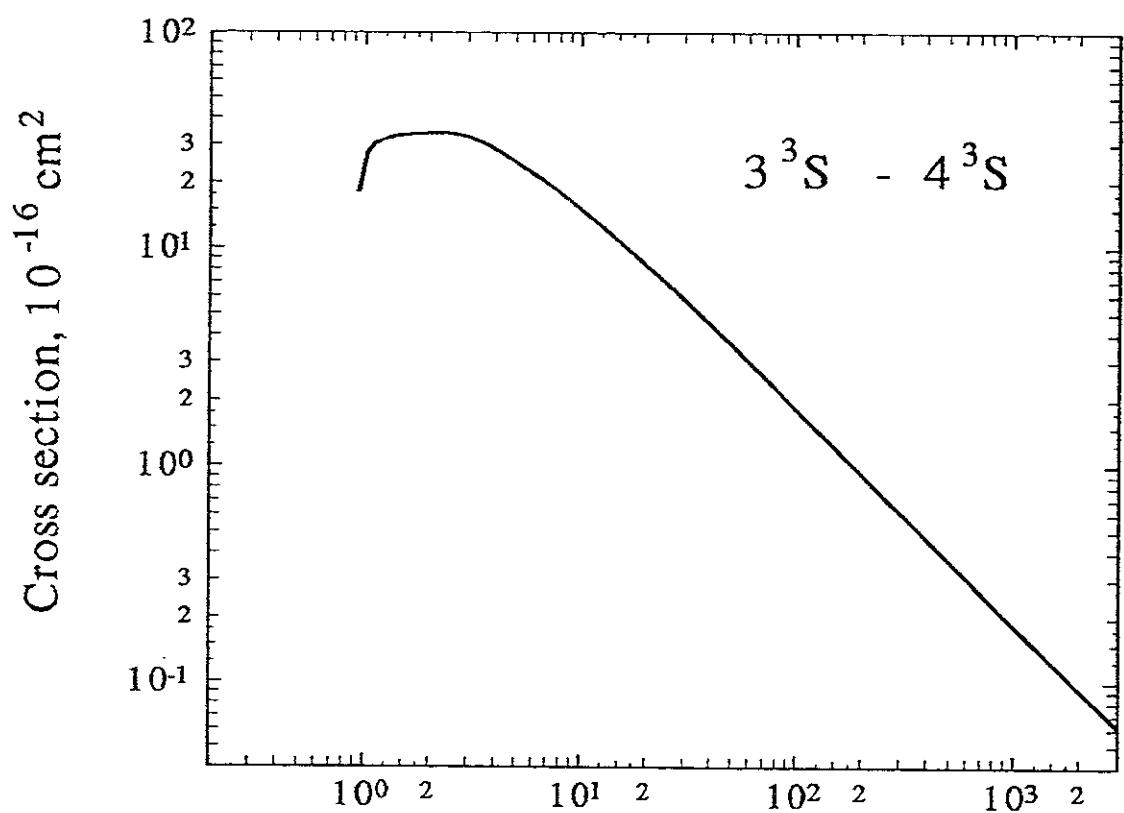


Fig.18 Electron energy, eV

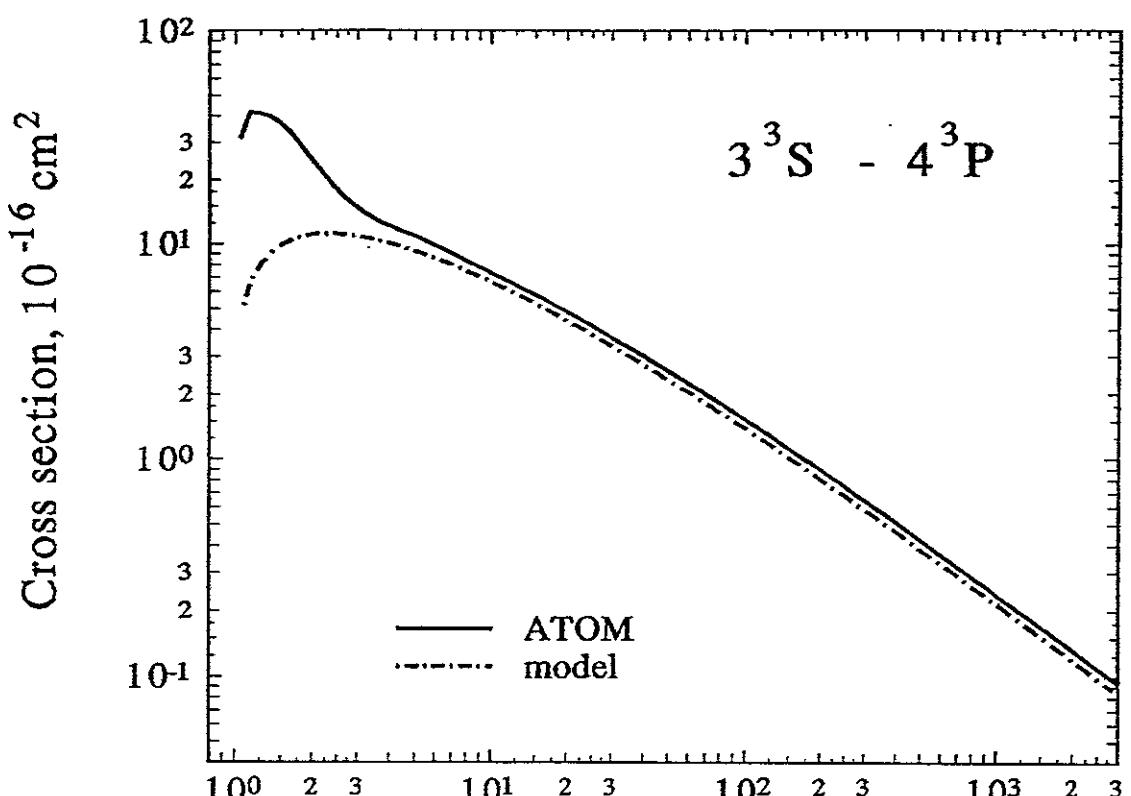


Fig.19 Electron energy, eV

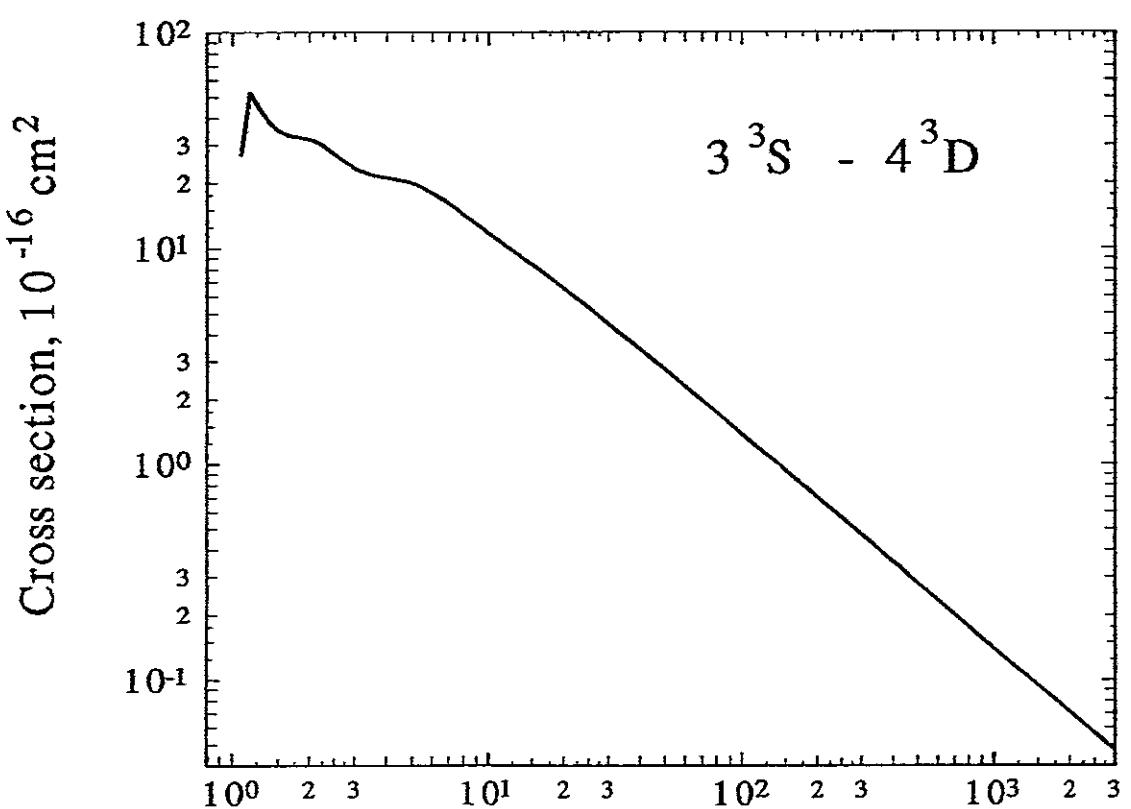


Fig.20 Electron energy, eV

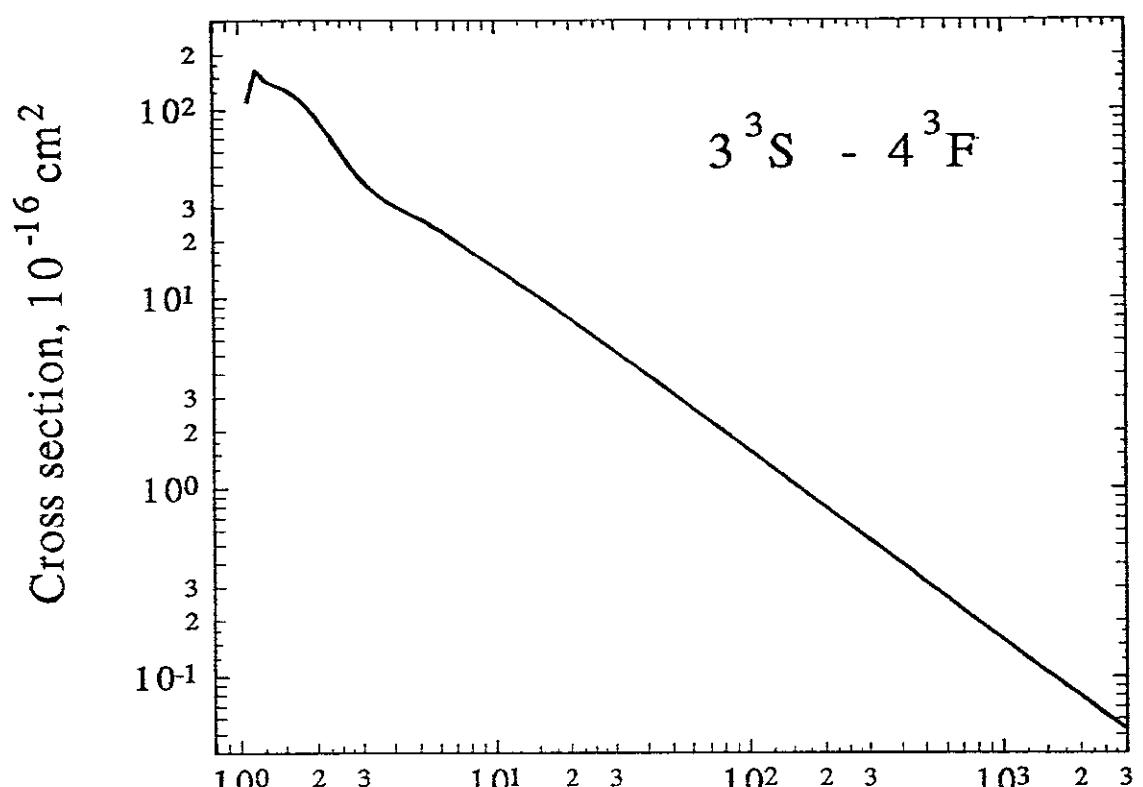


Fig.21 Electron energy, eV

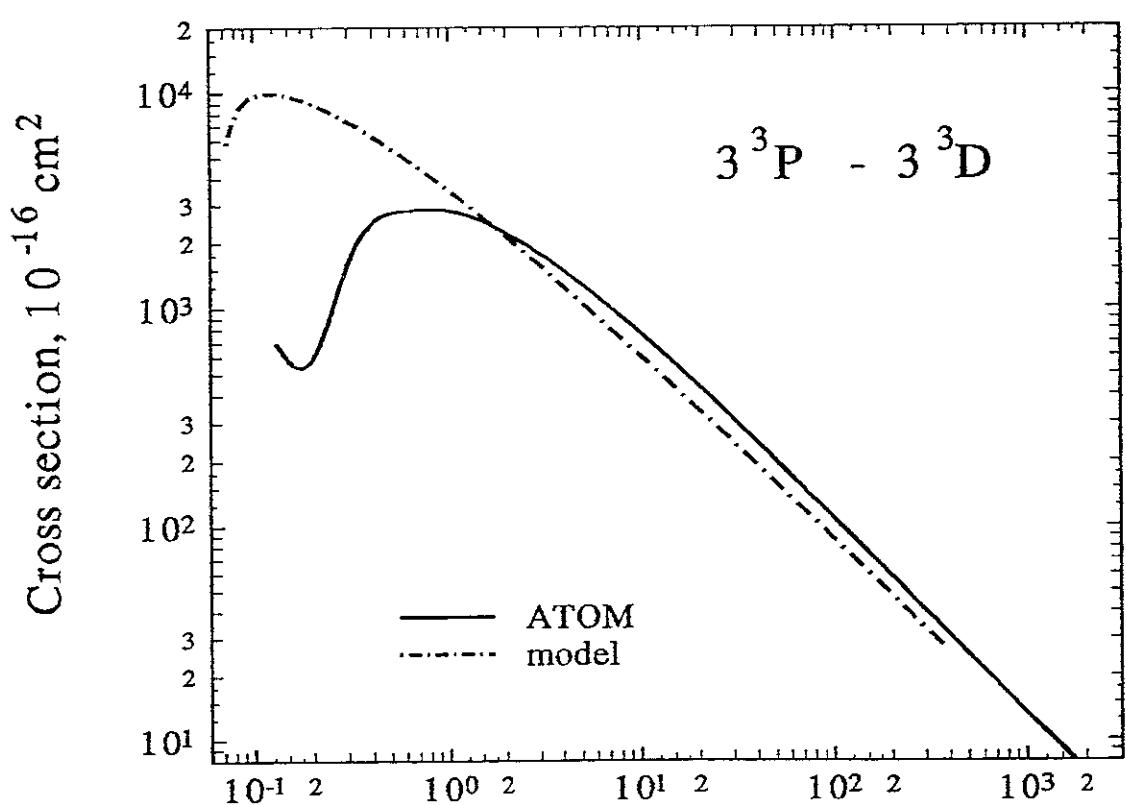
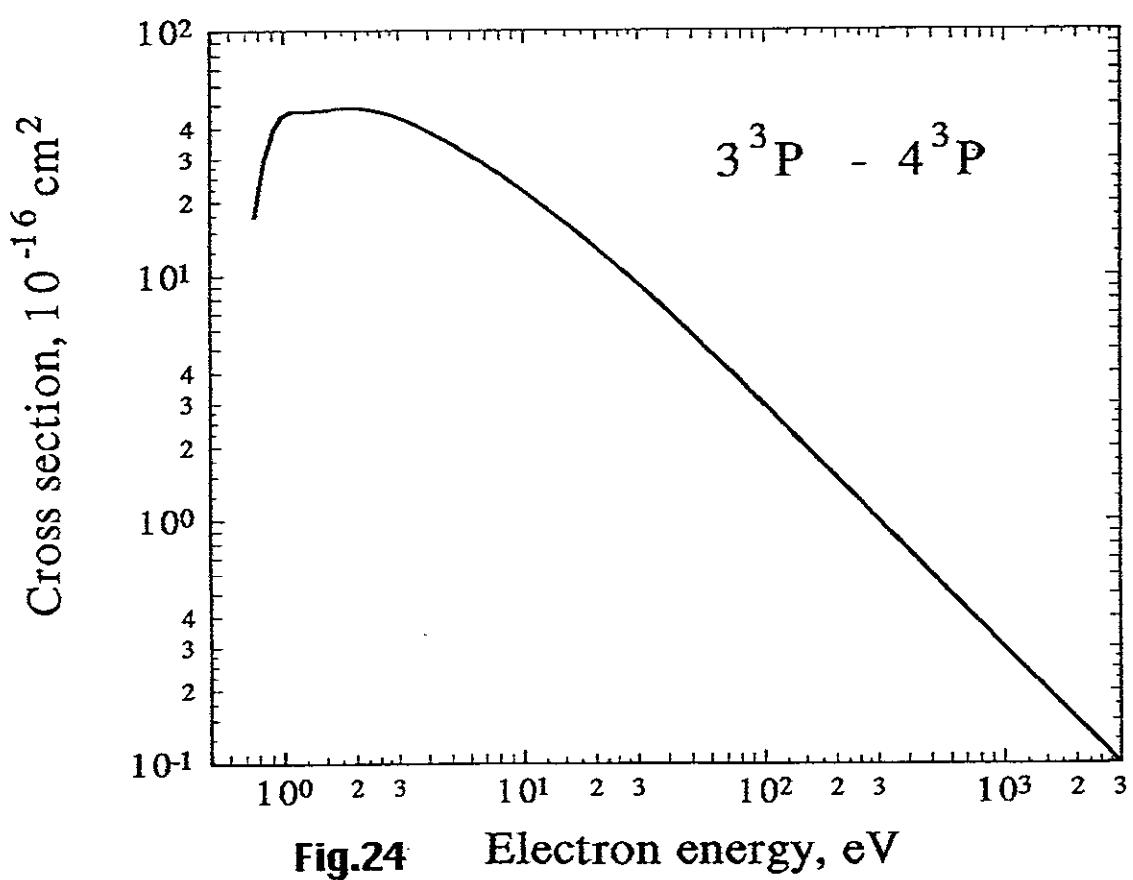
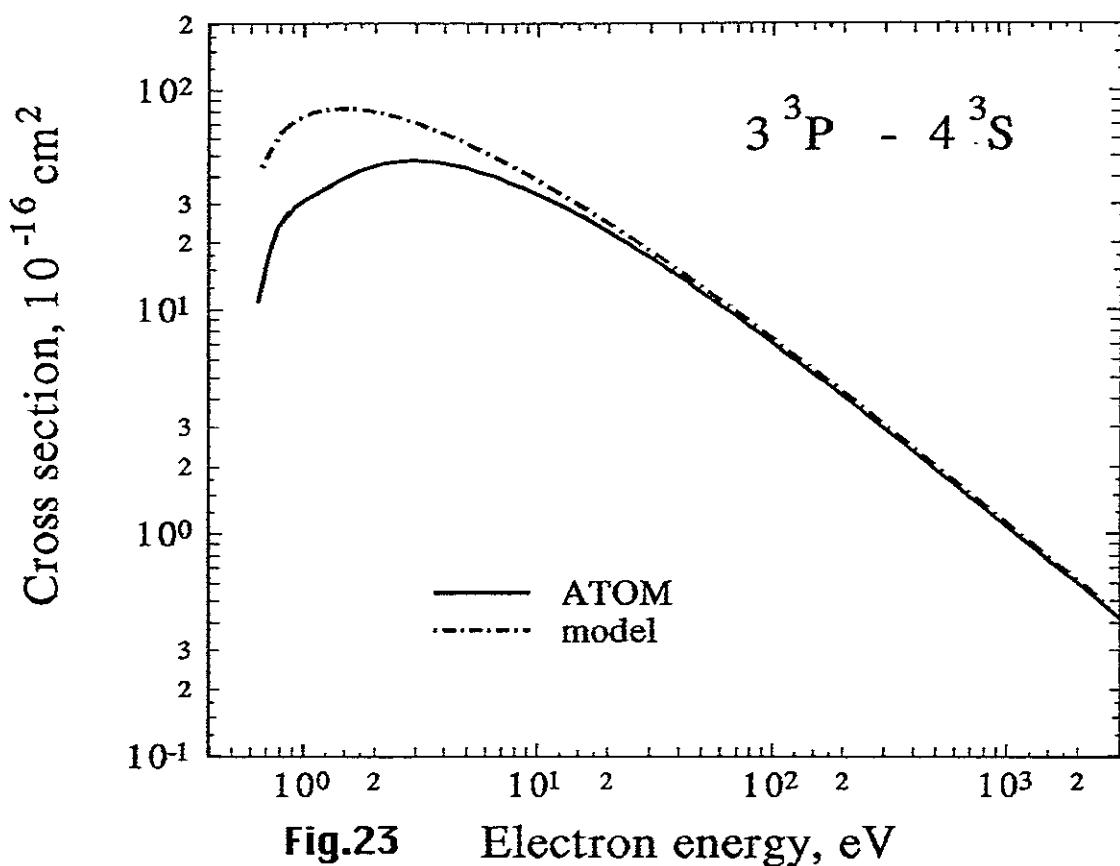
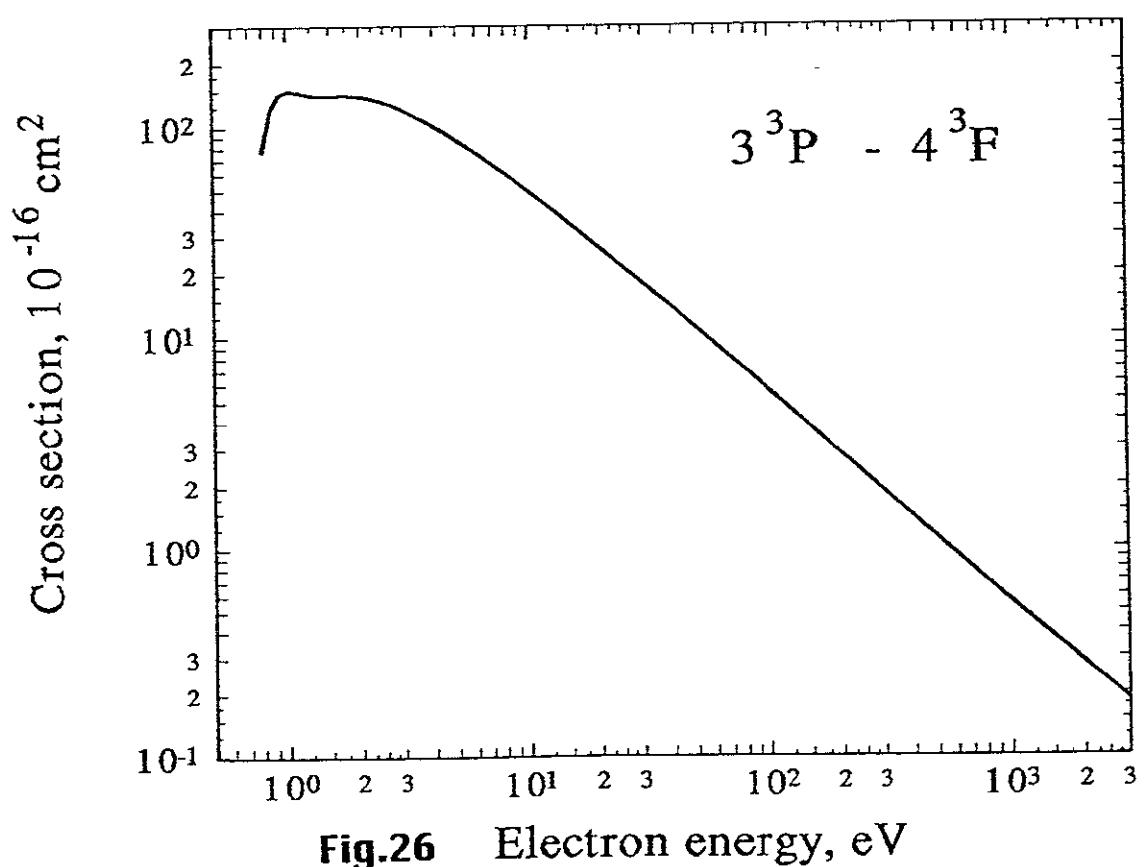
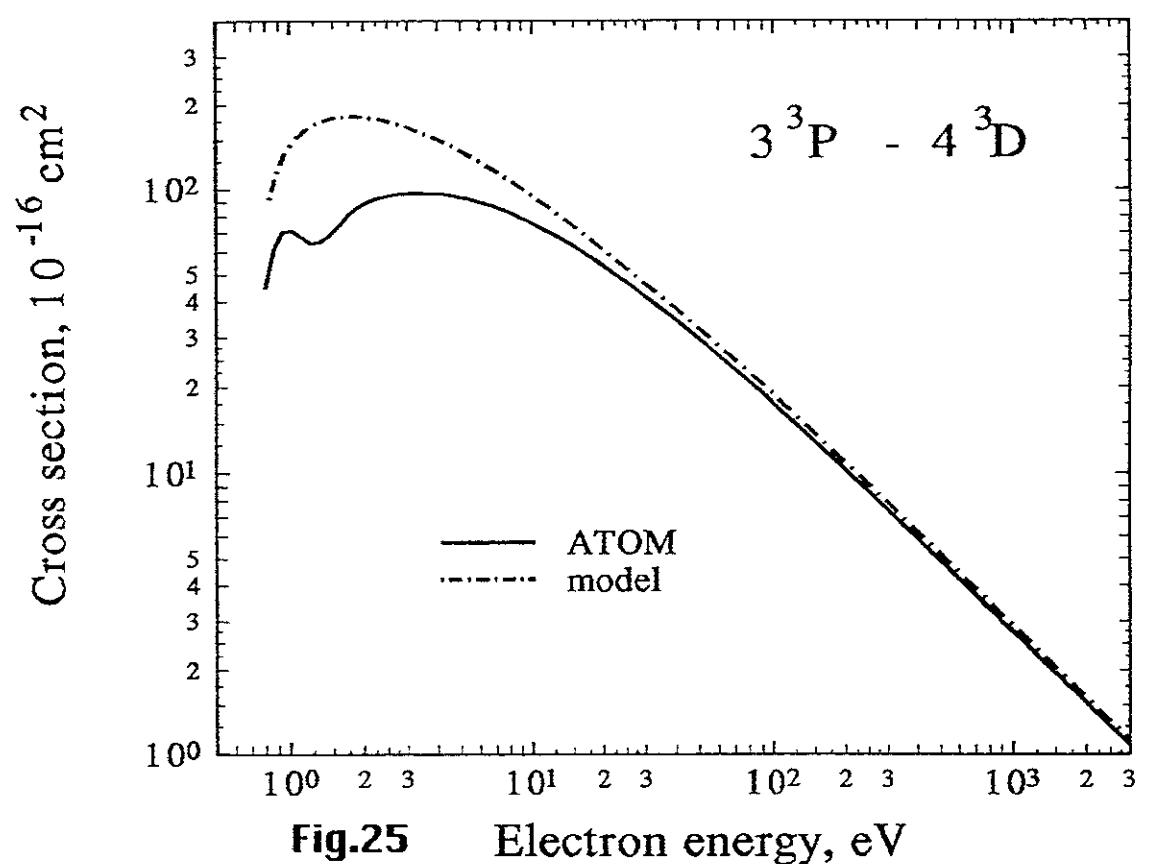


Fig.22 Electron energy, eV





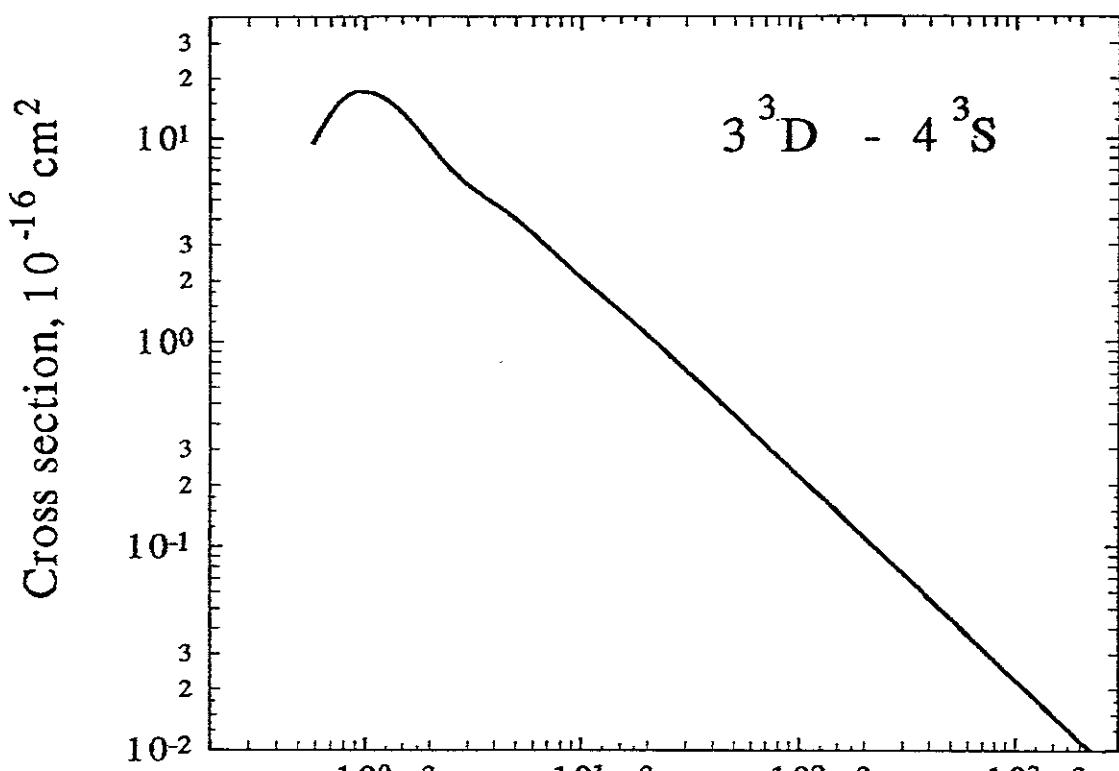


Fig.27 Electron energy, eV

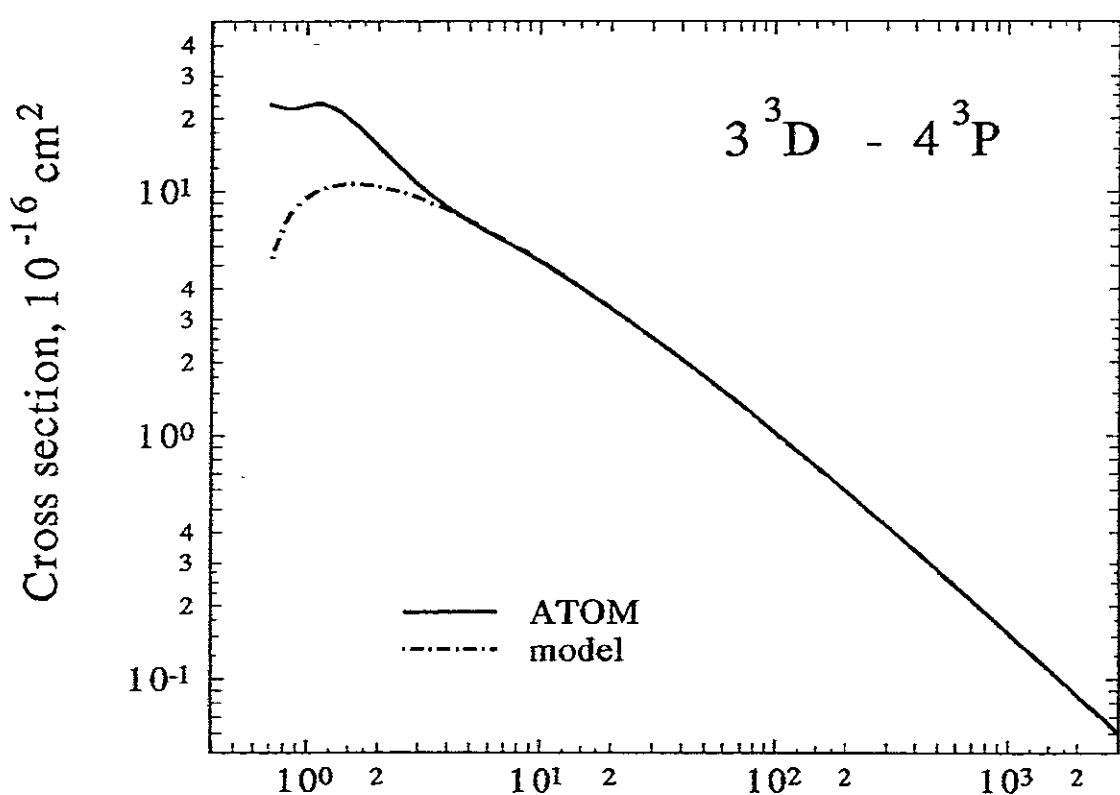
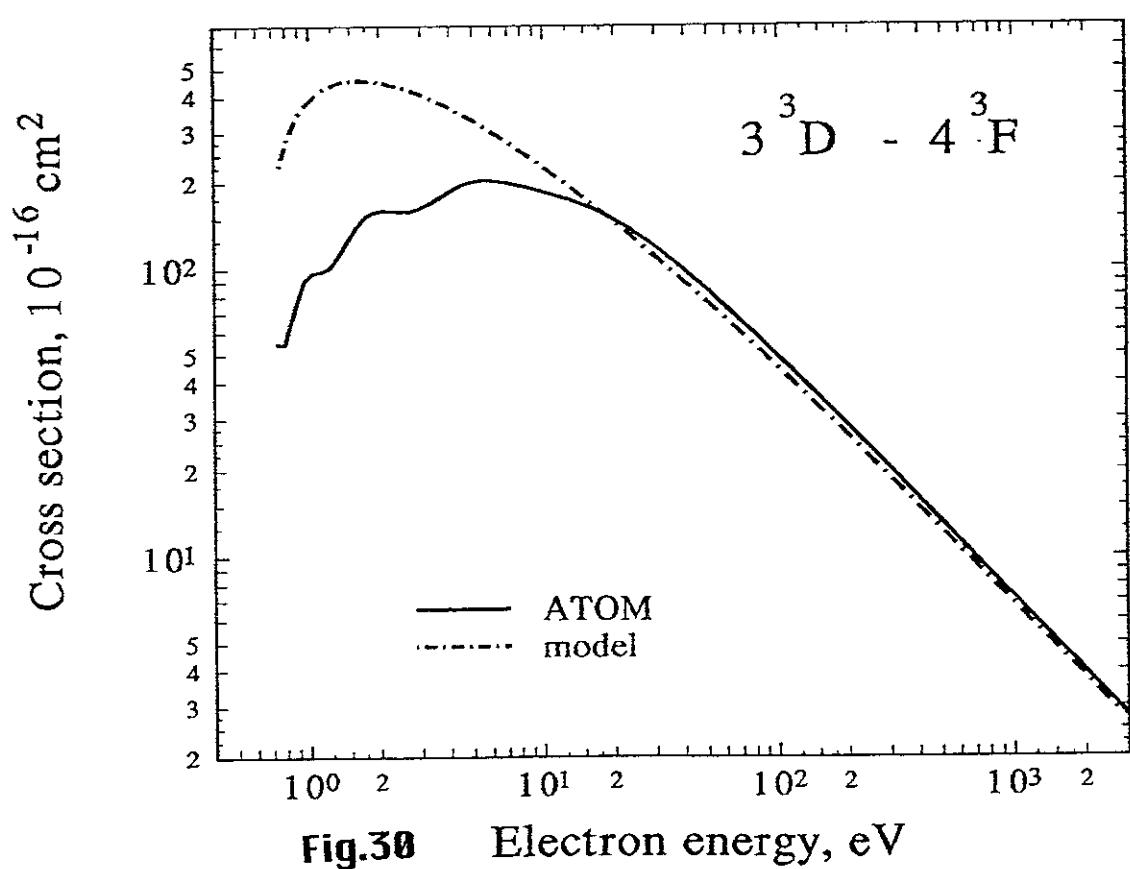
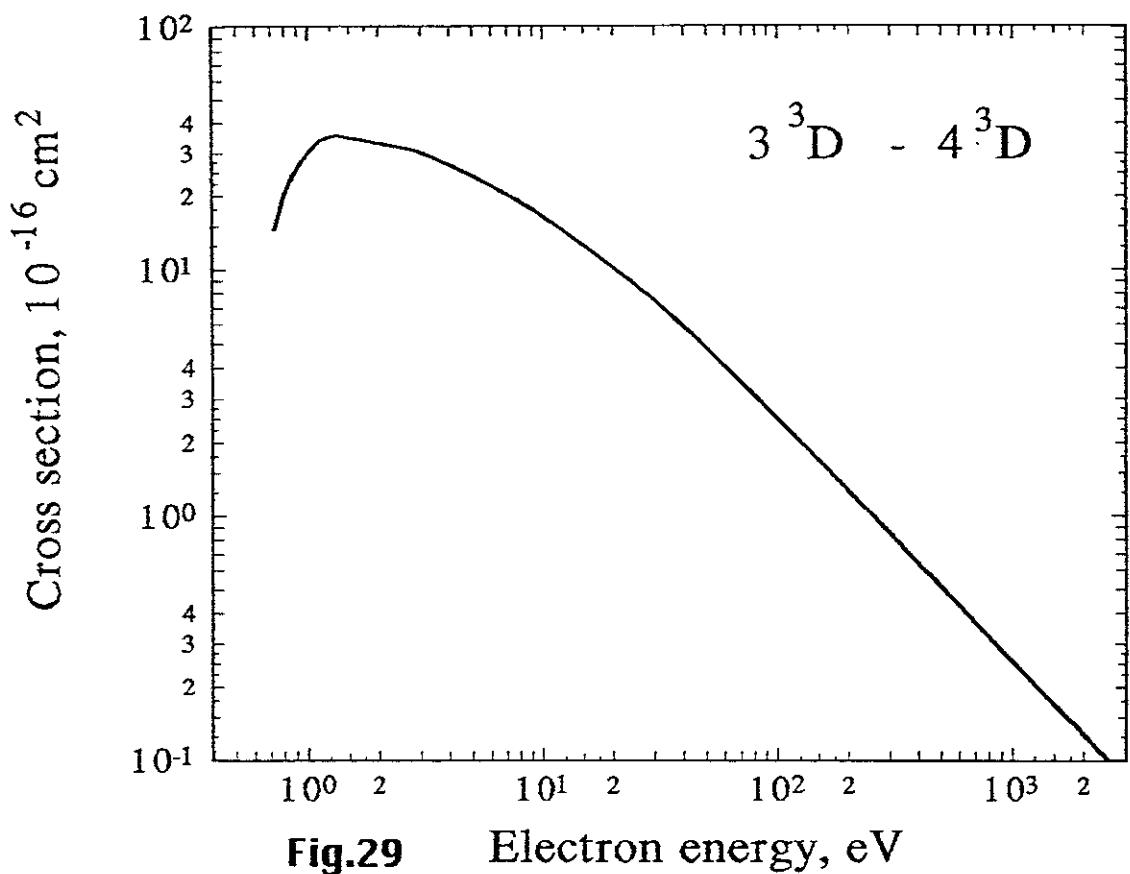


Fig.28 Electron energy, eV



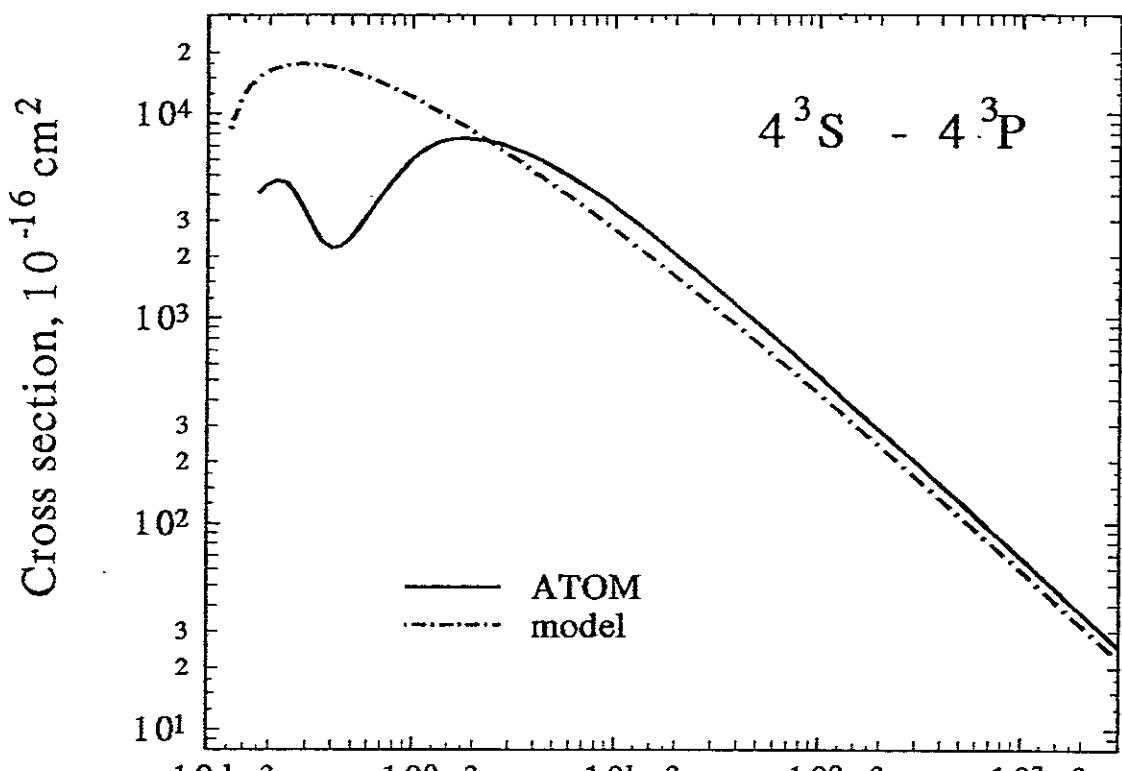


Fig.31 Electron energy, eV

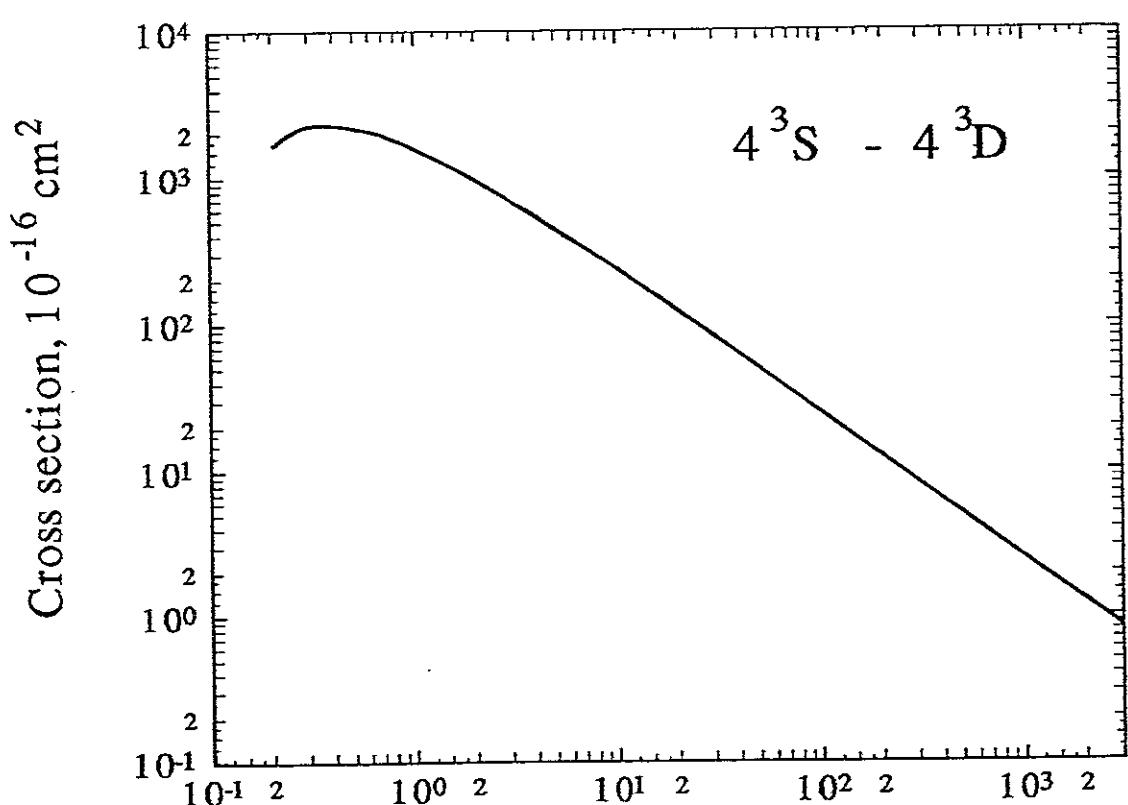


Fig.32 Electron energy, eV

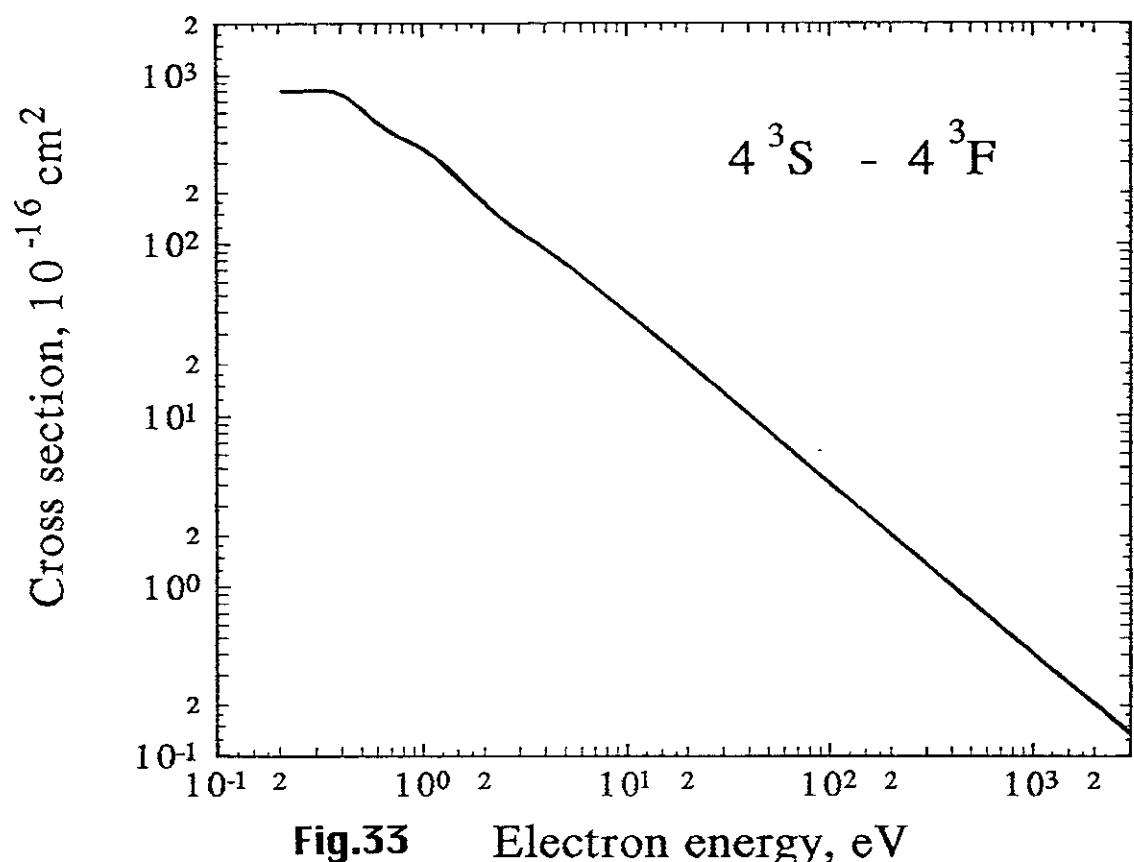


Fig.33 Electron energy, eV

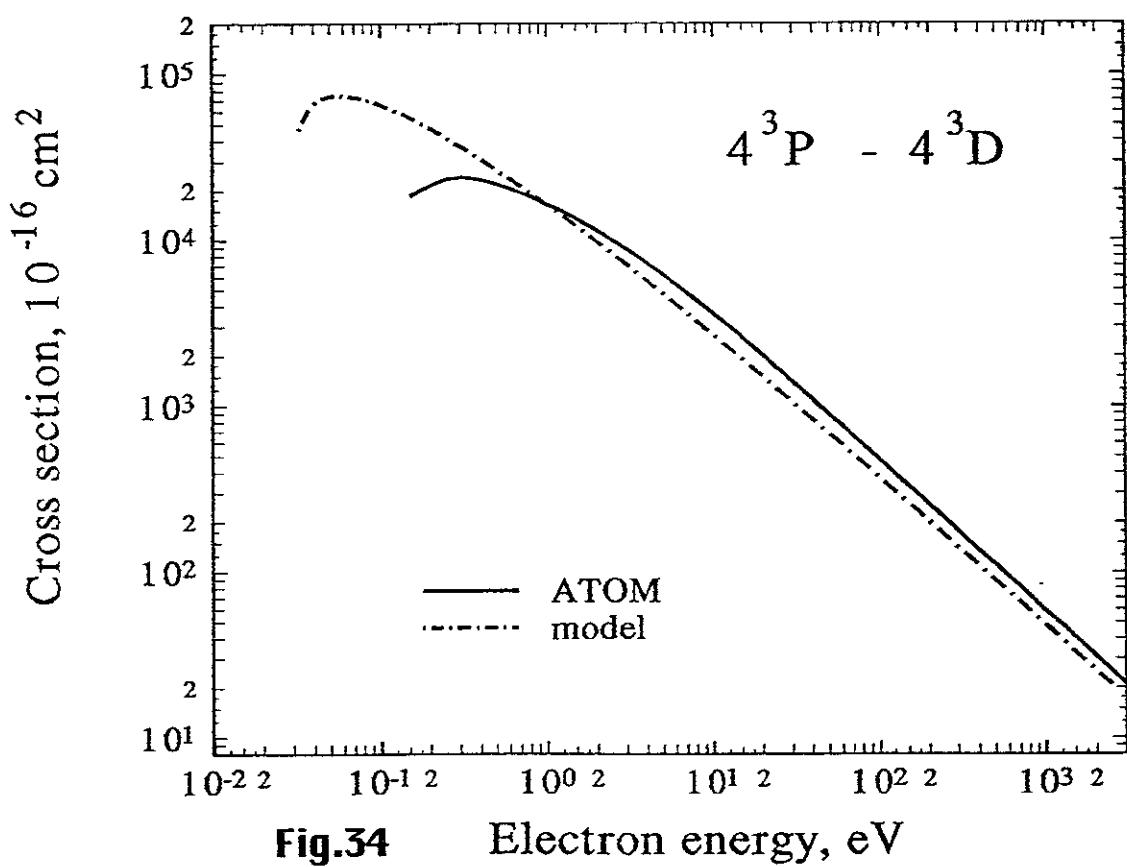
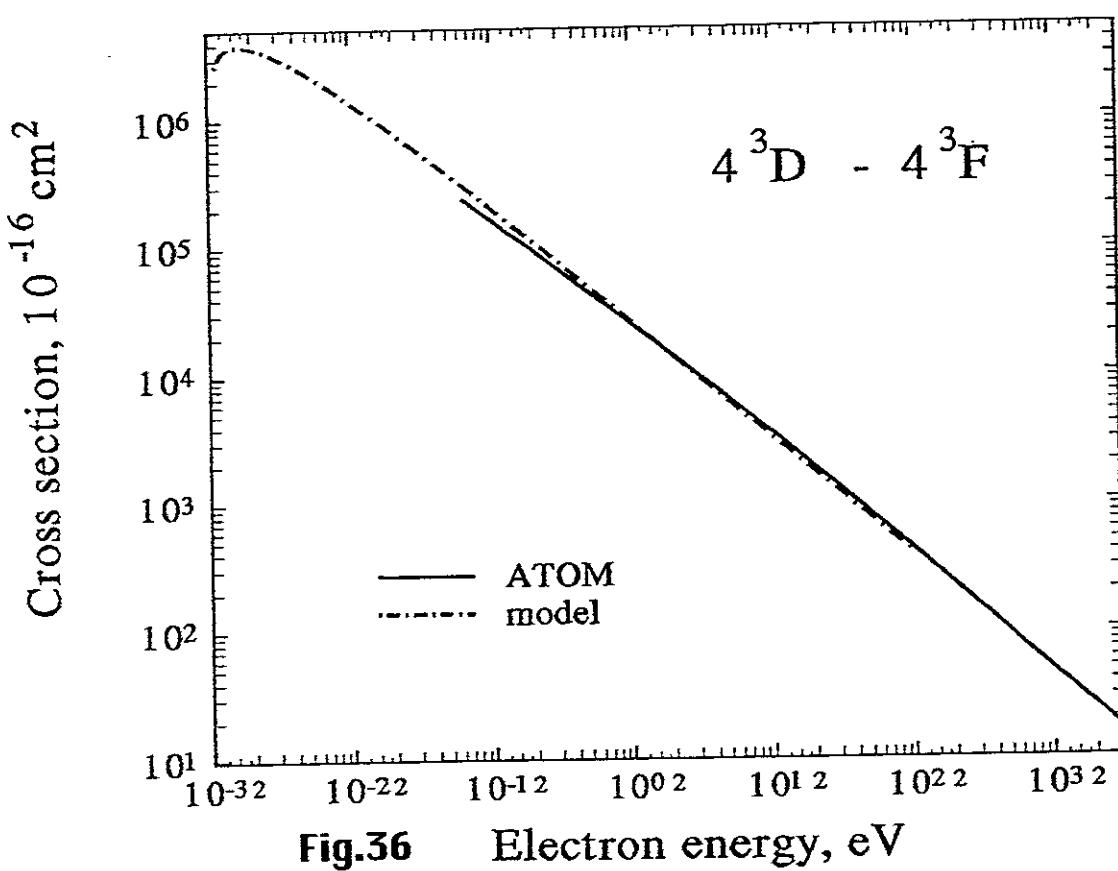
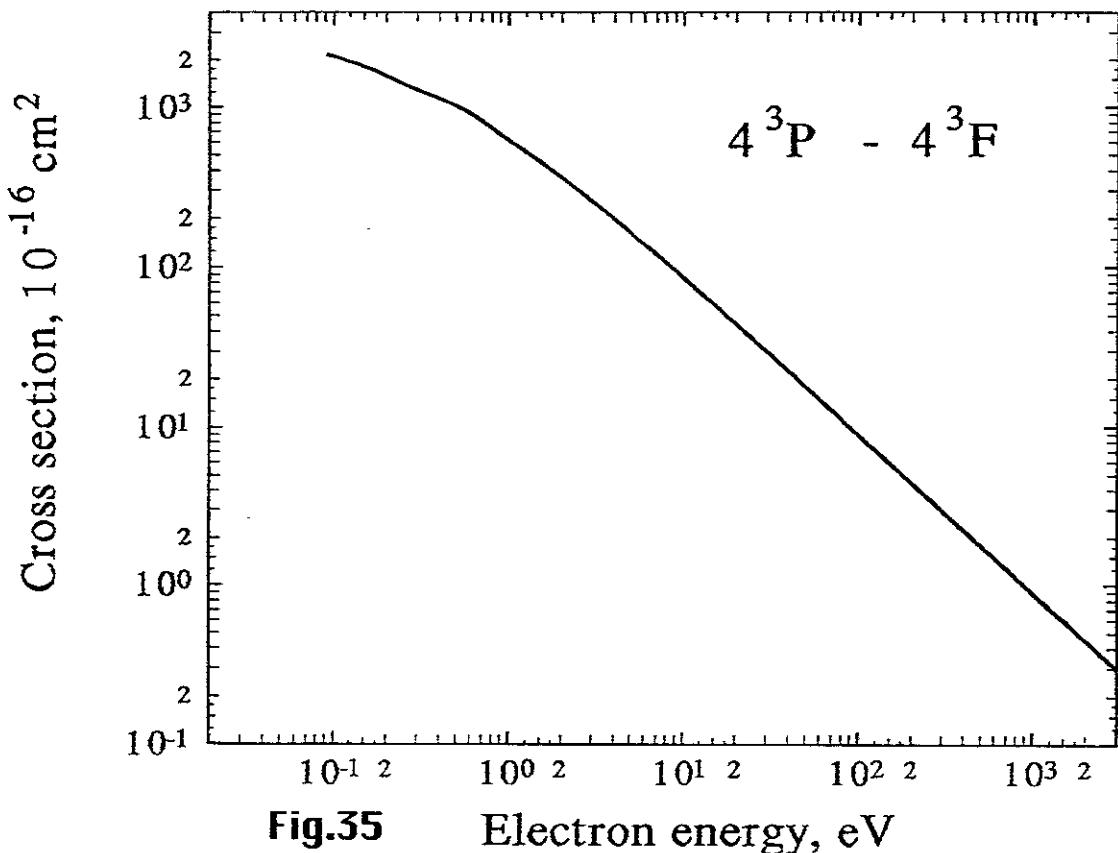


Fig.34 Electron energy, eV



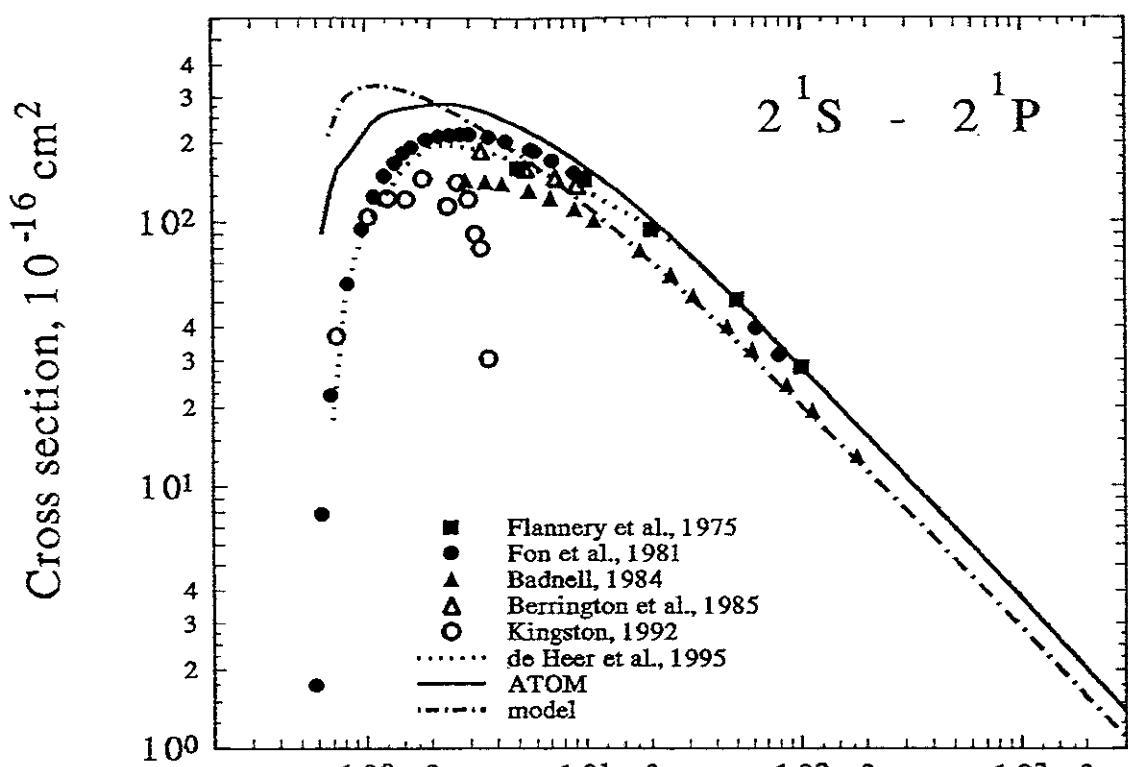


Fig.37

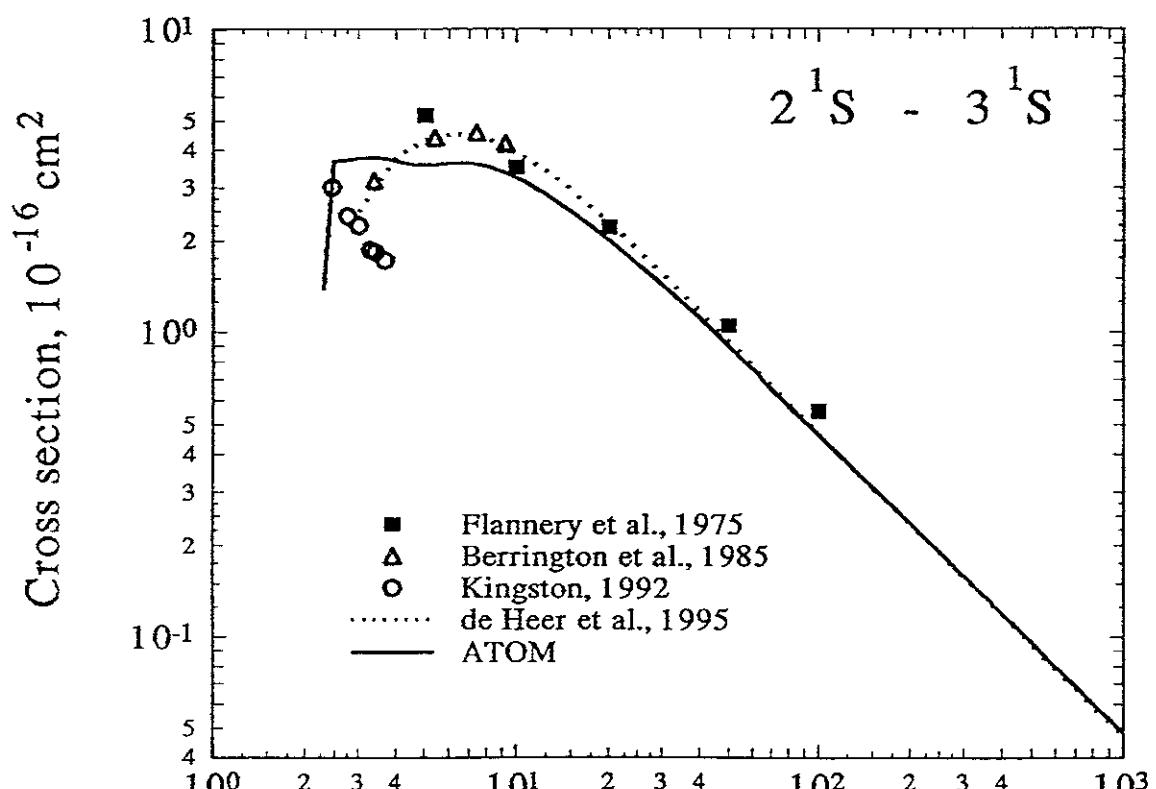


Fig.38

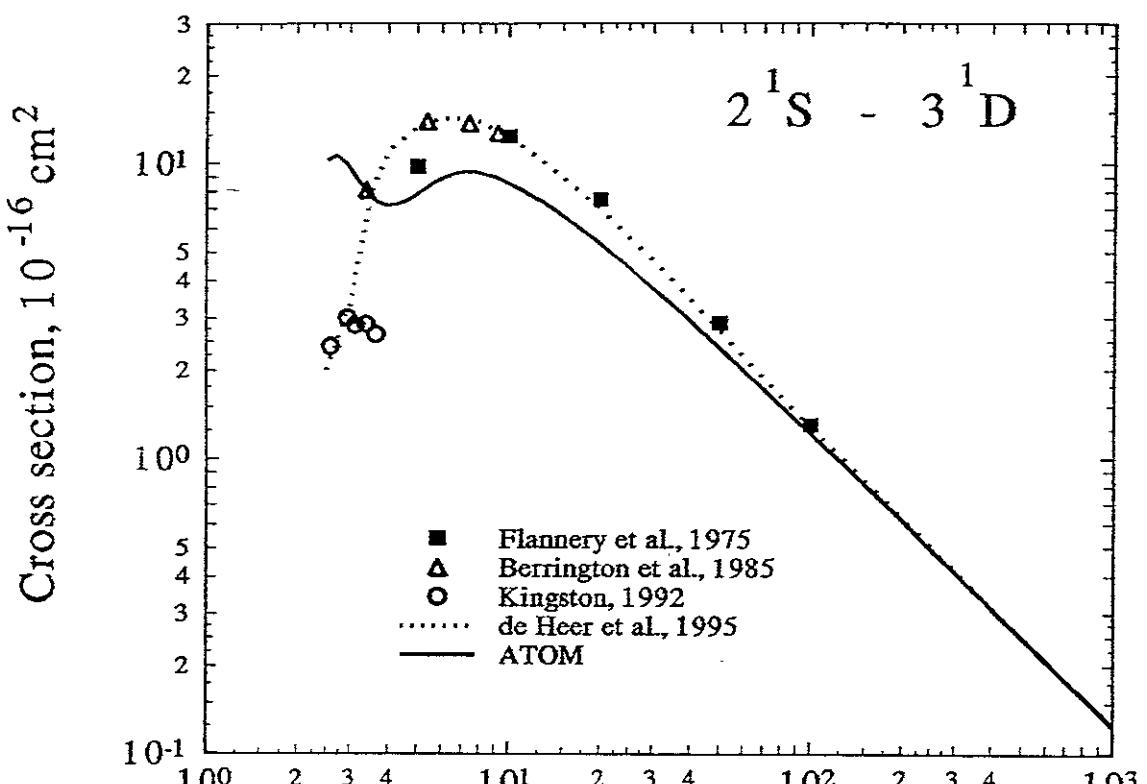


Fig.39 Electron energy, eV

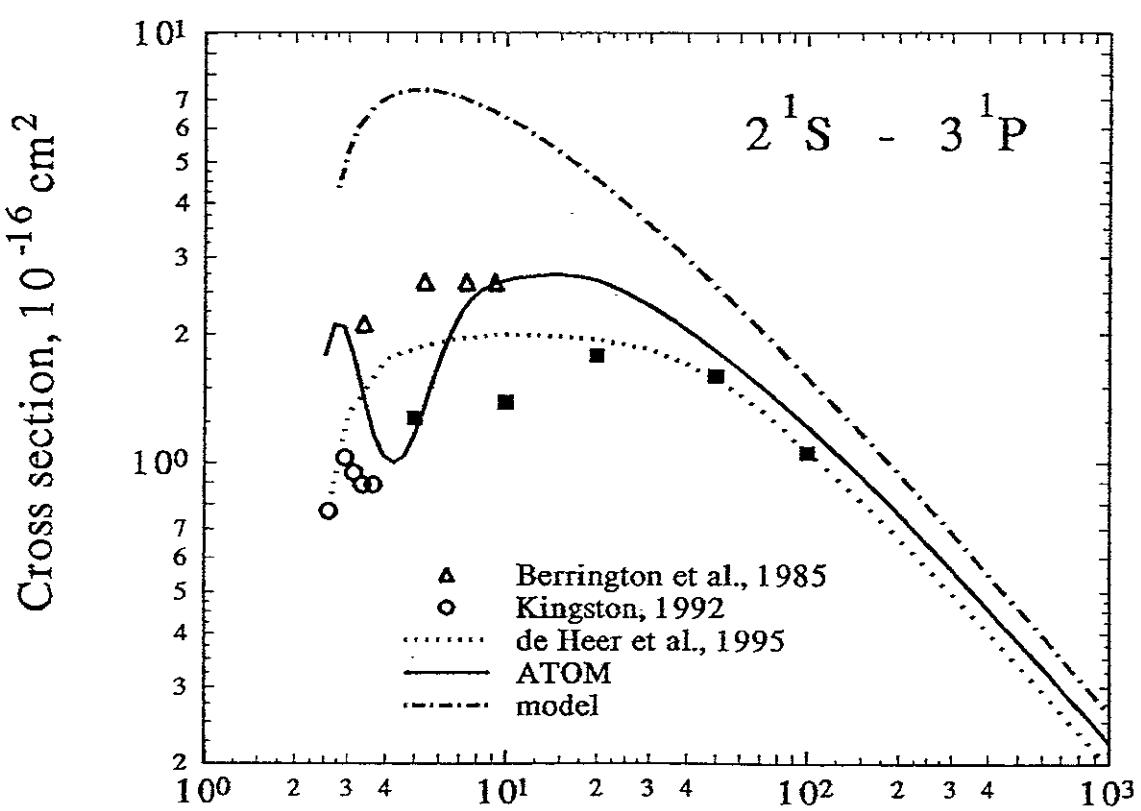


Fig.40 Electron energy, eV

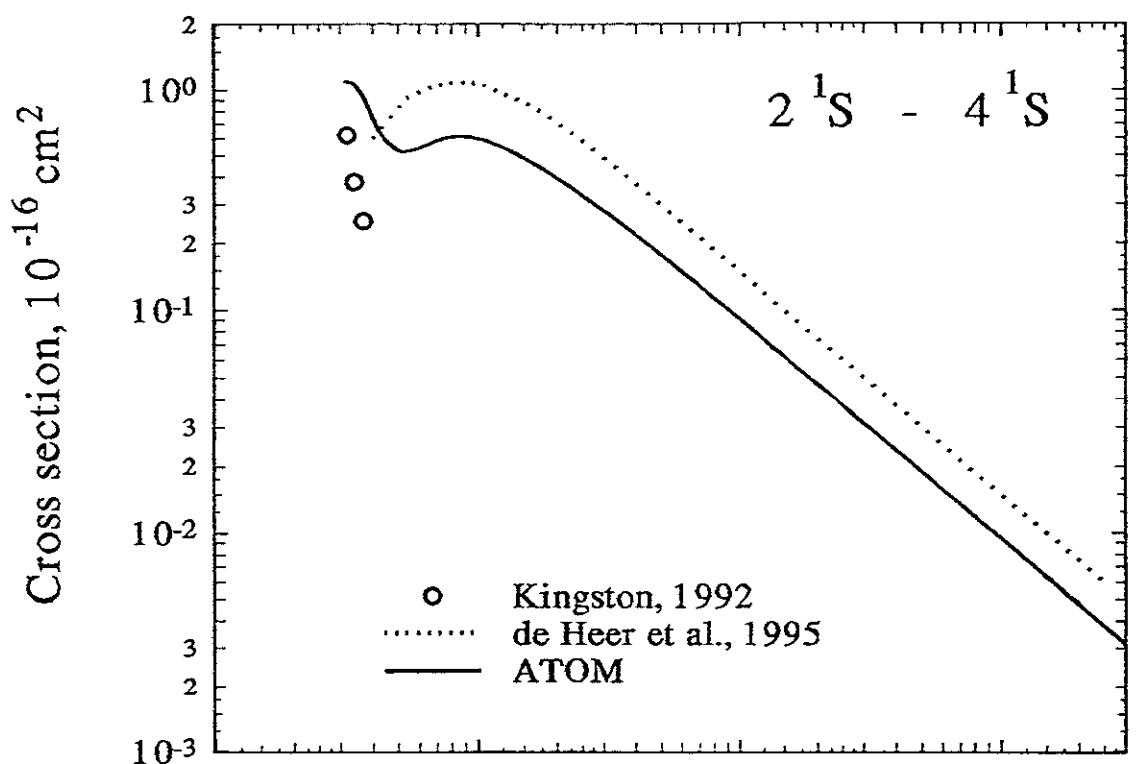


Fig.41 Electron energy, eV

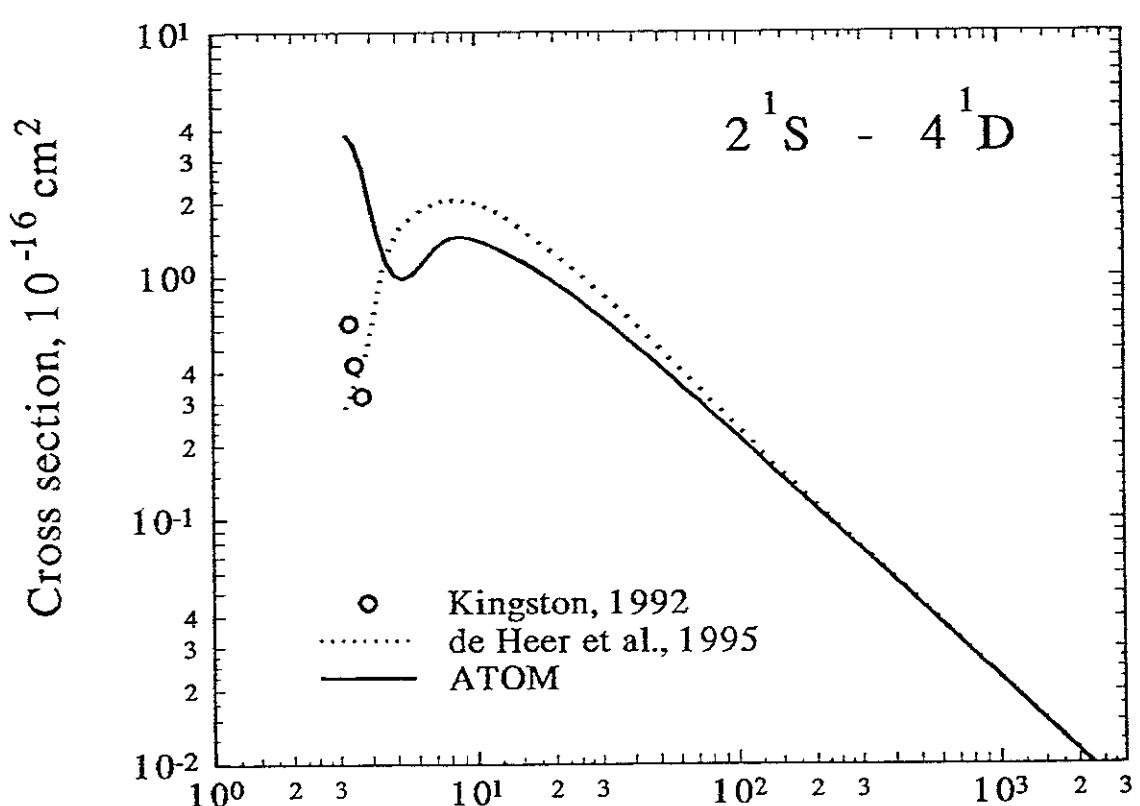
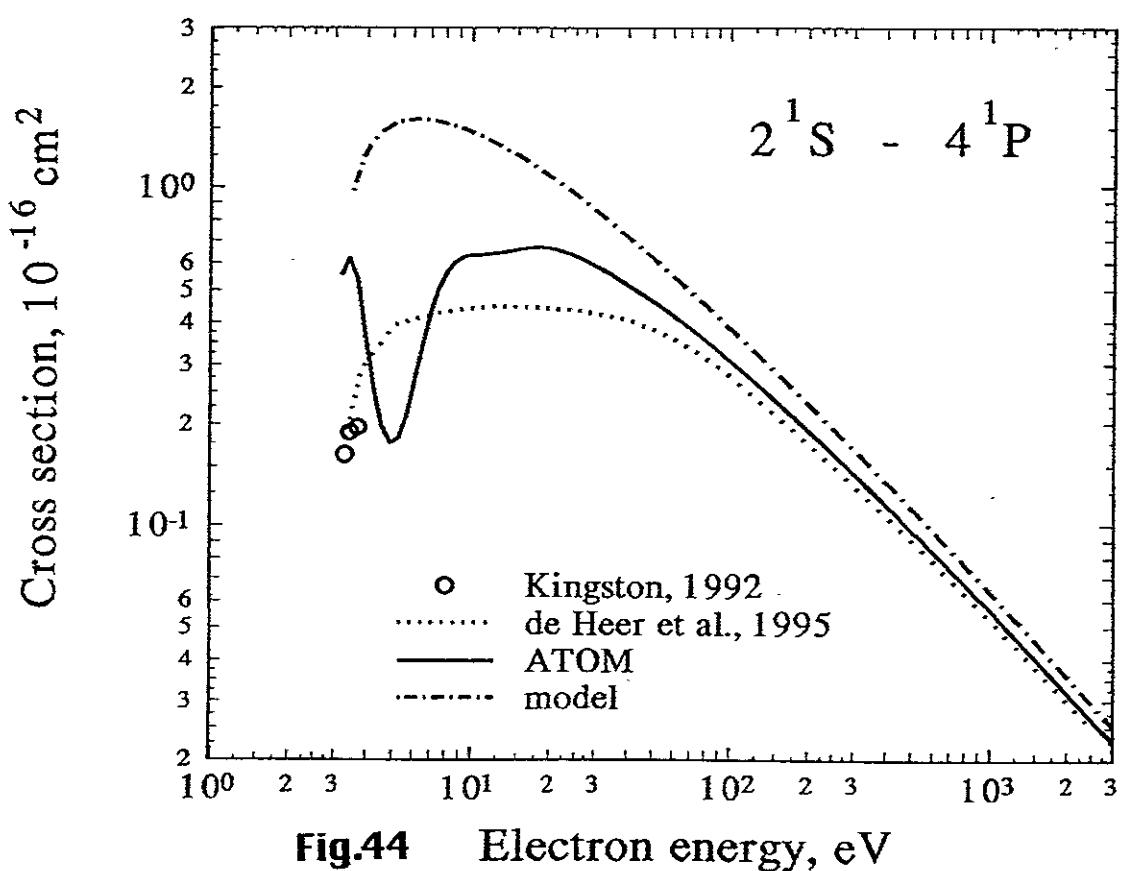
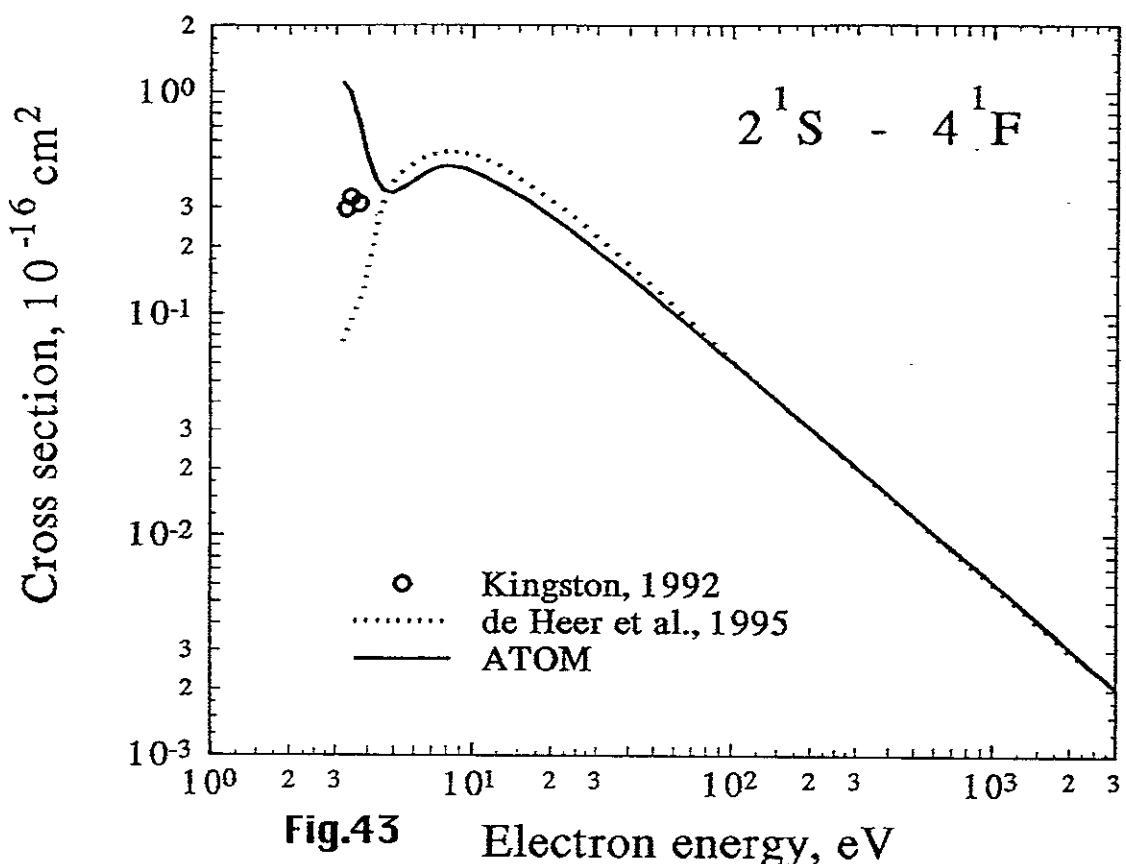
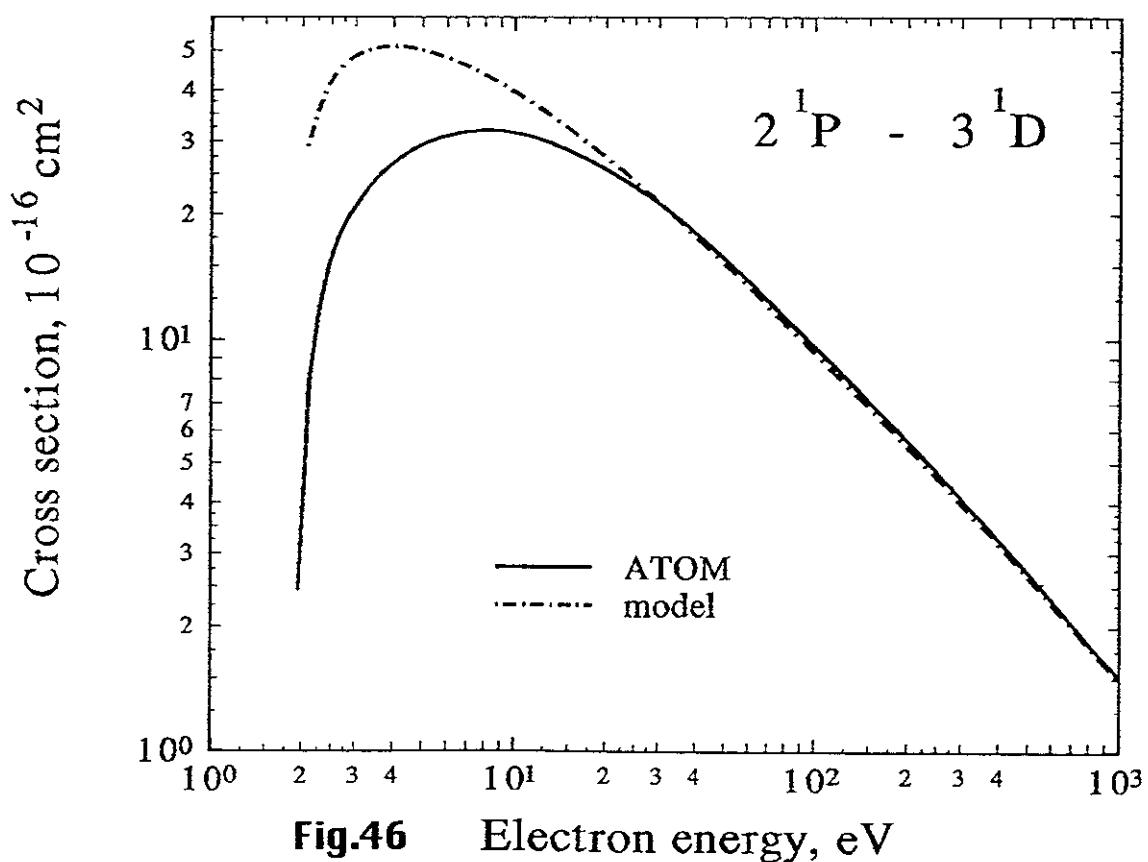
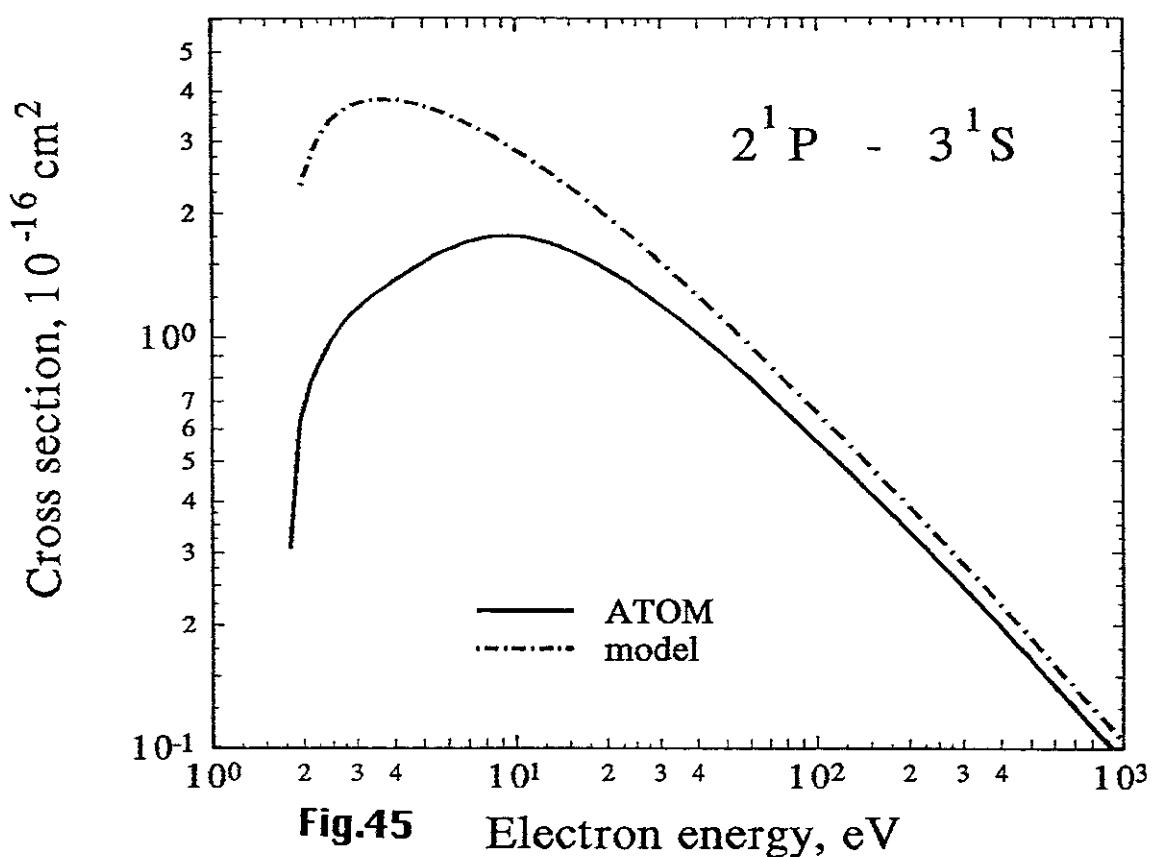


Fig.42 Electron energy, eV





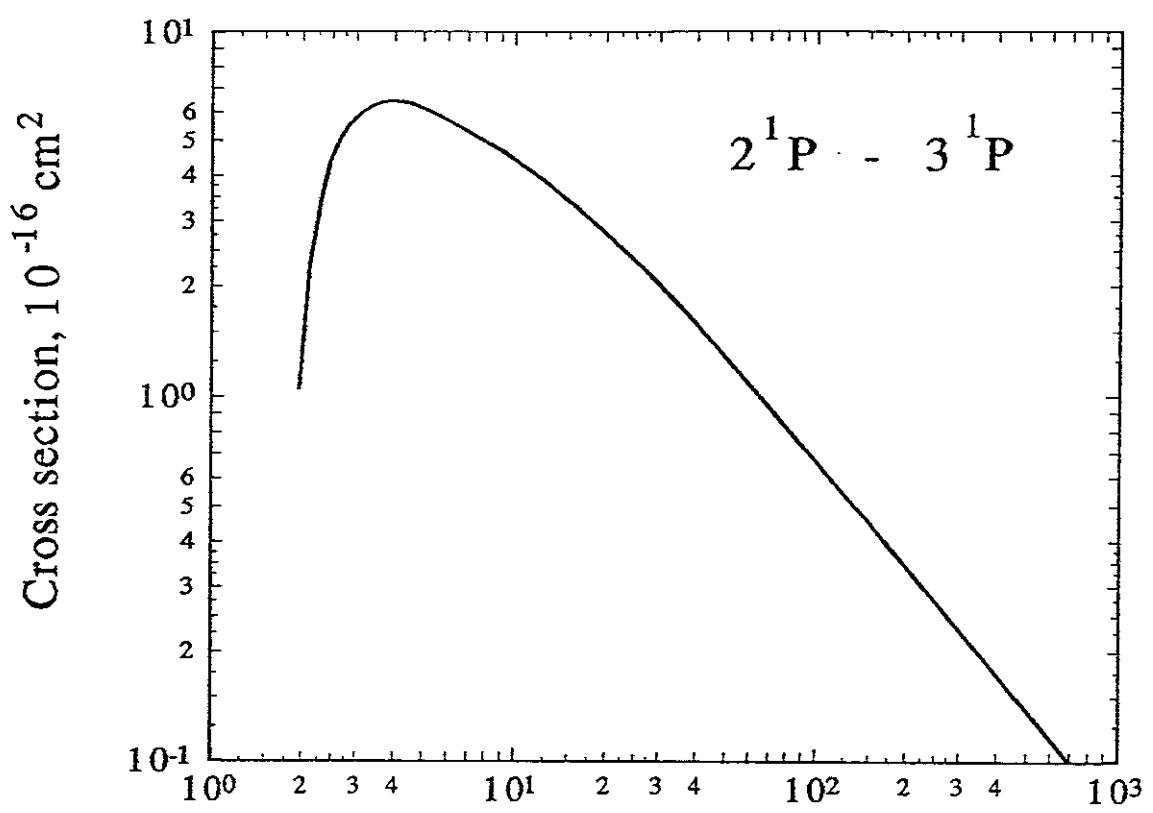


Fig.47 Electron energy, eV

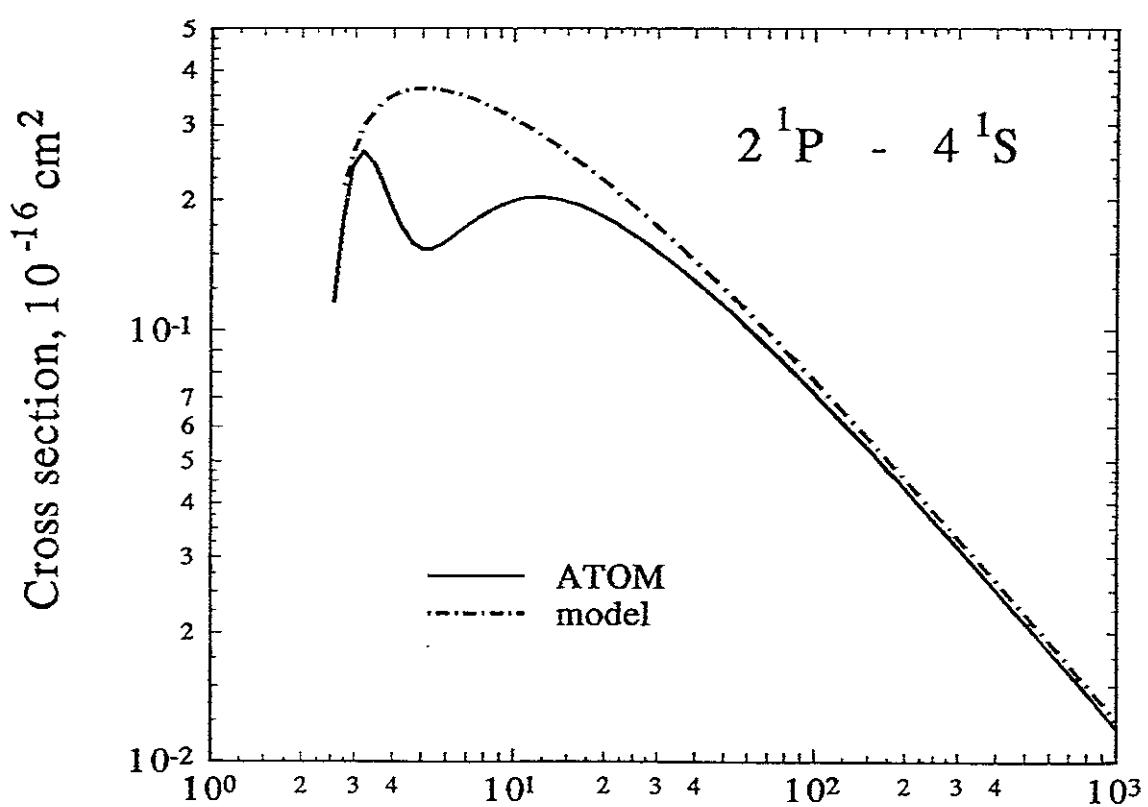


Fig.48 Electron energy, eV

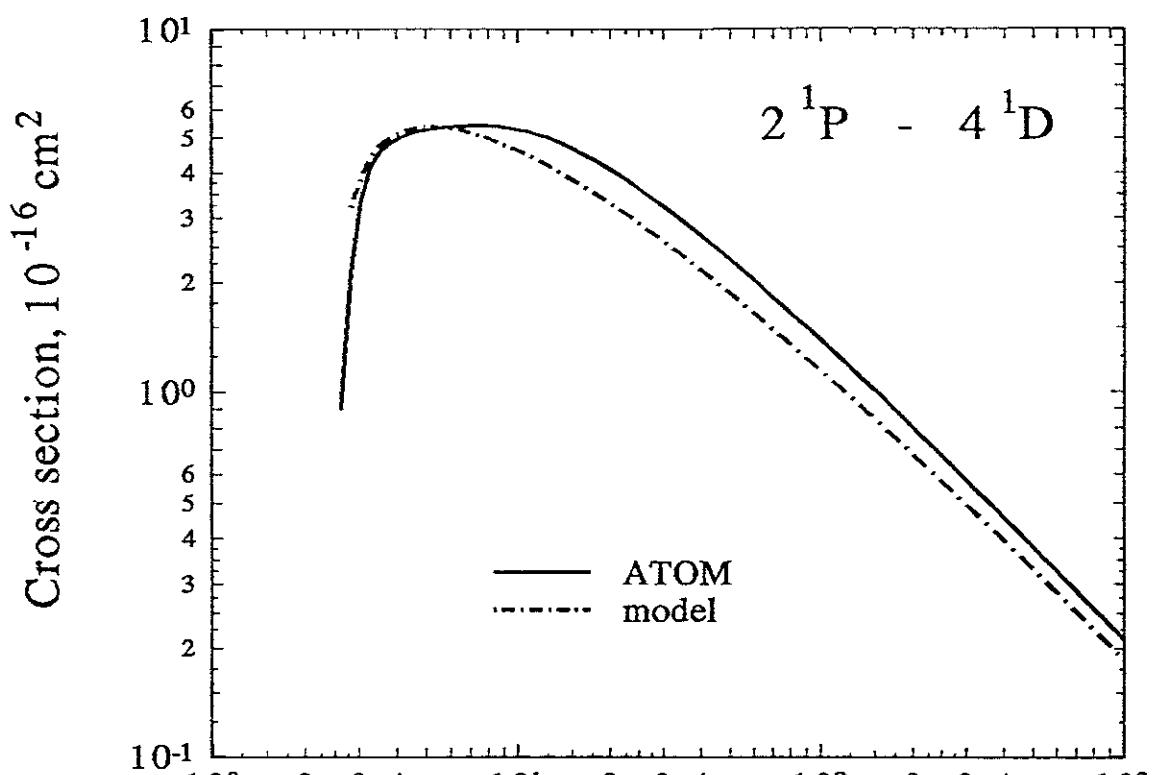


Fig.49 Electron energy, eV

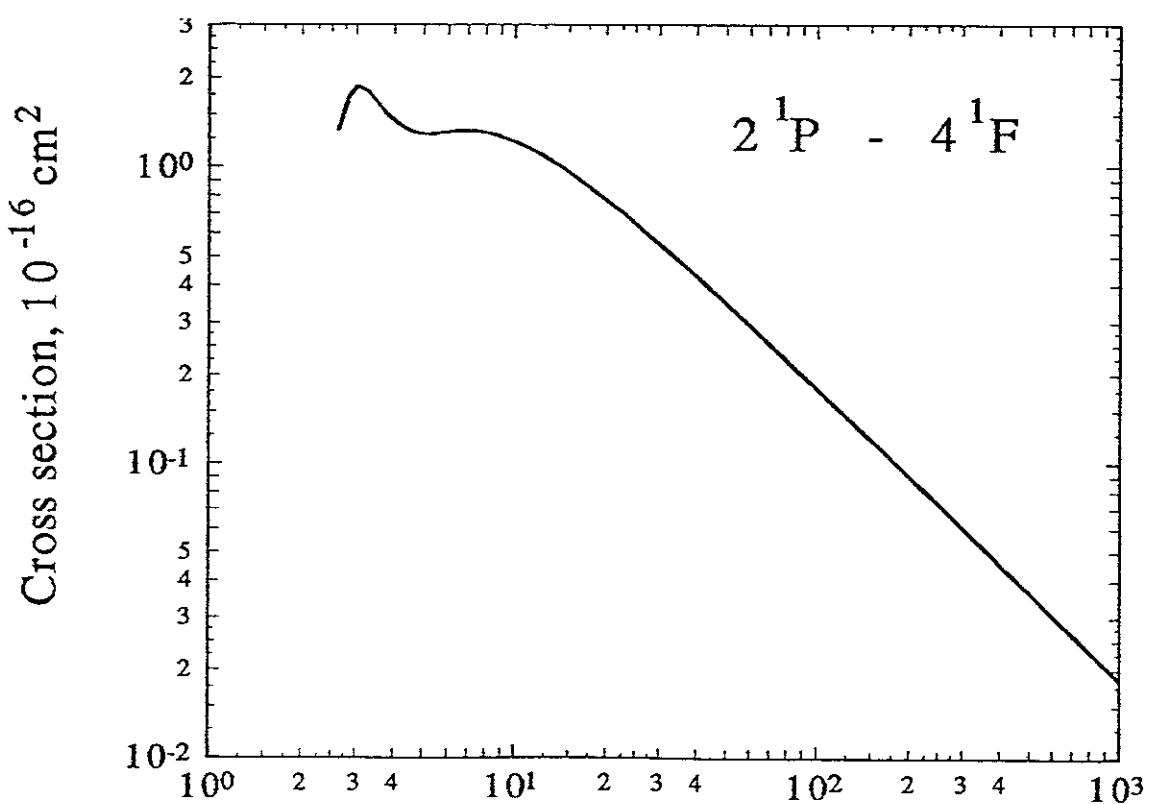
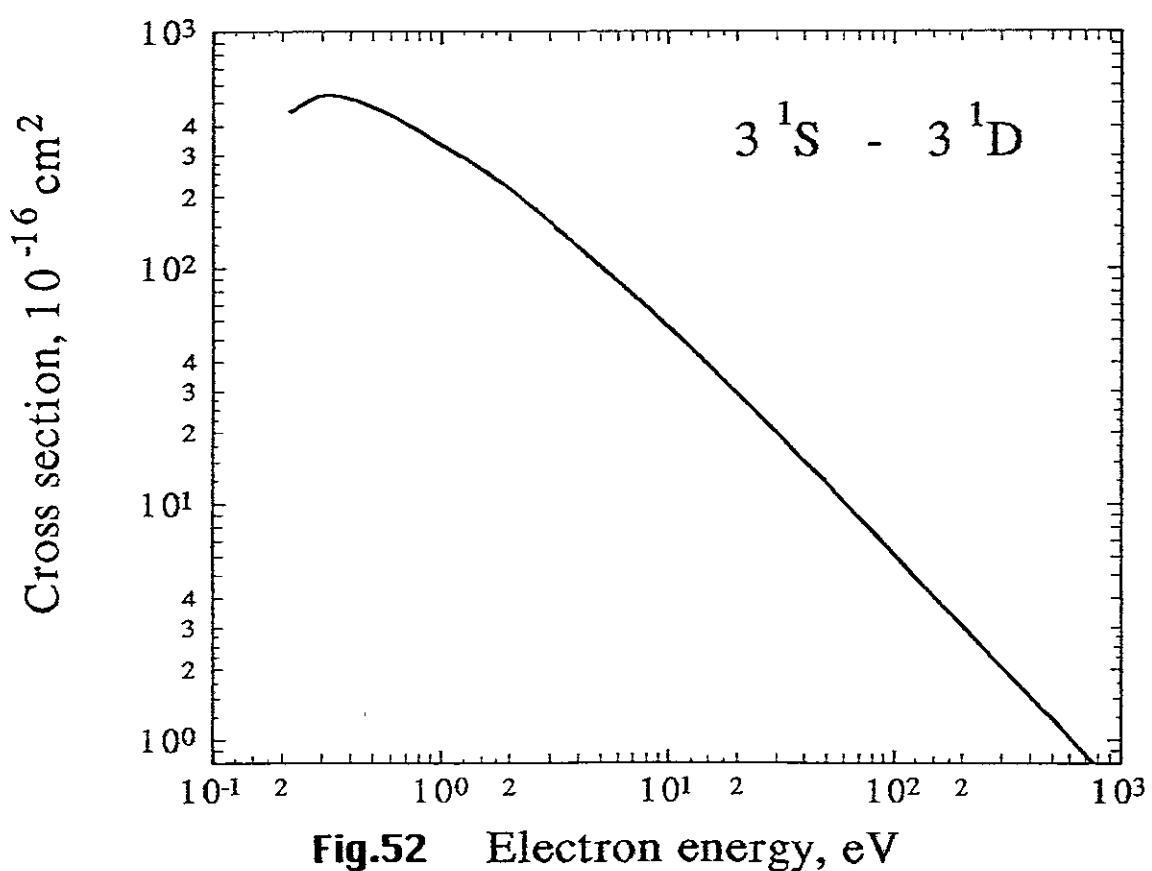
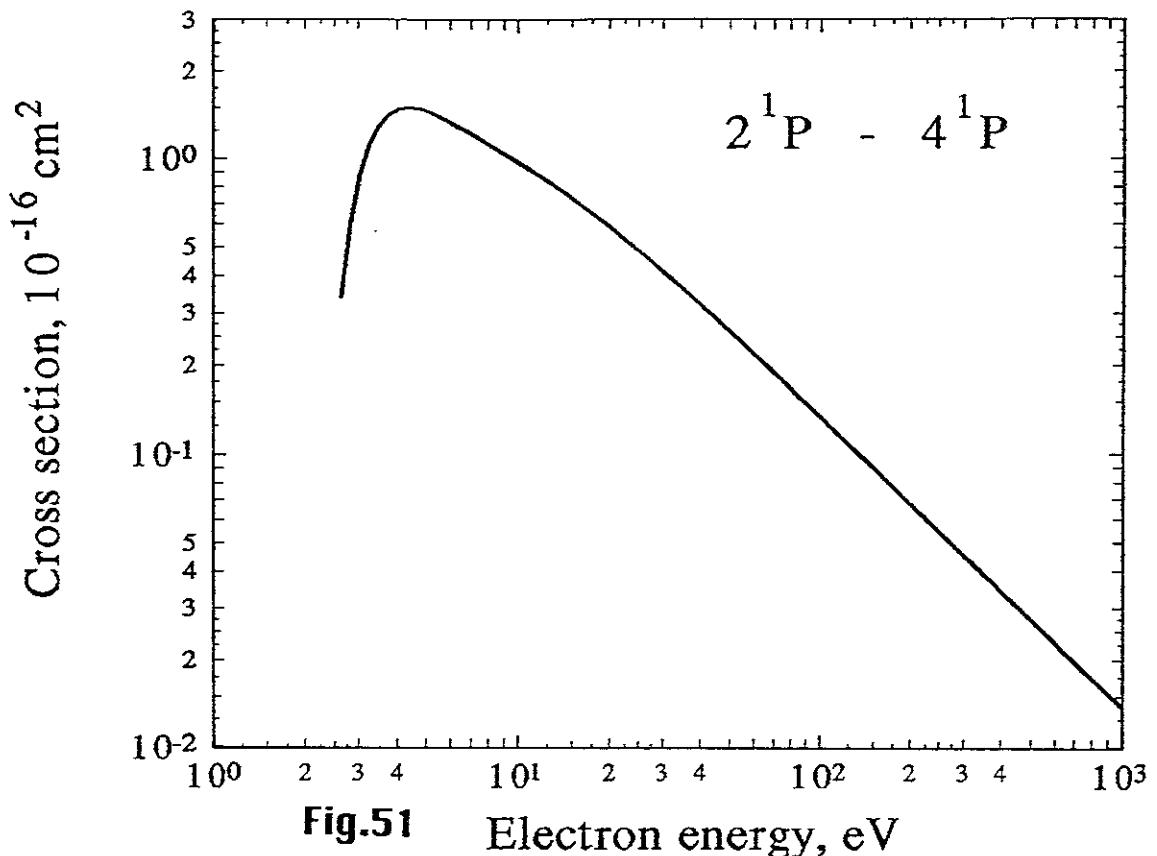


Fig.50 Electron energy, eV



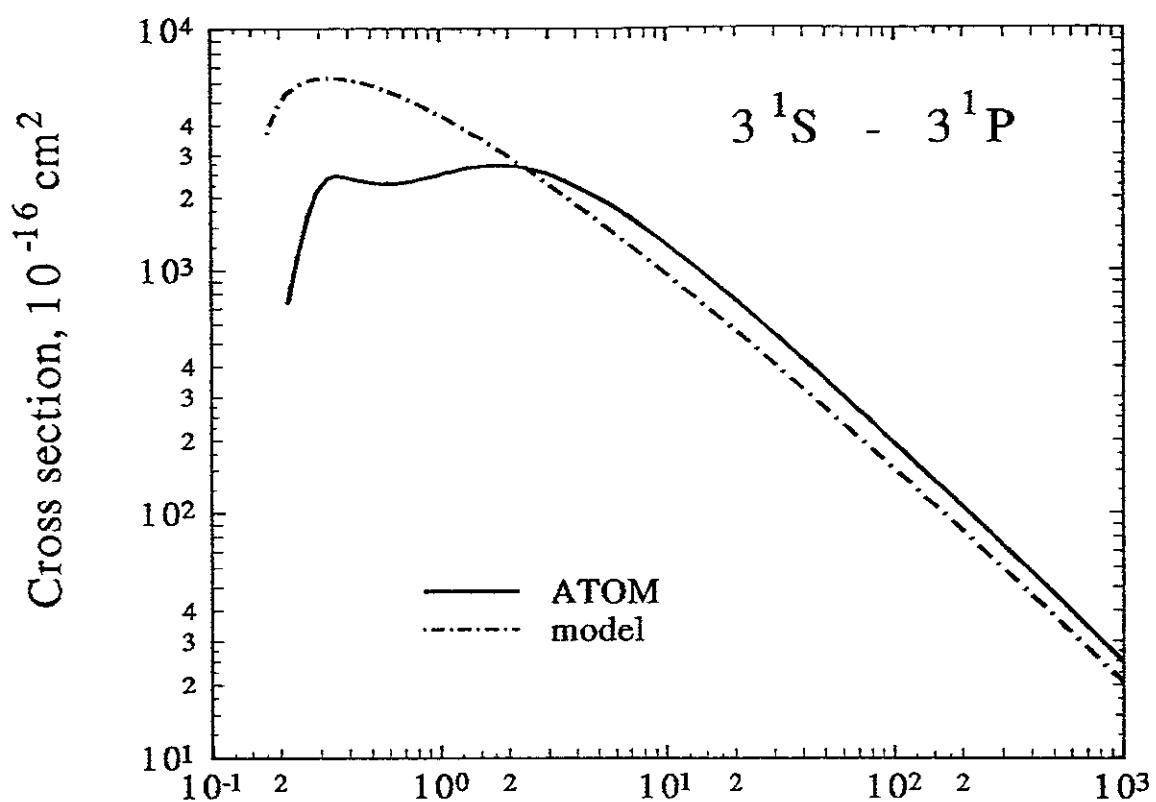


Fig.53 Electron energy, eV

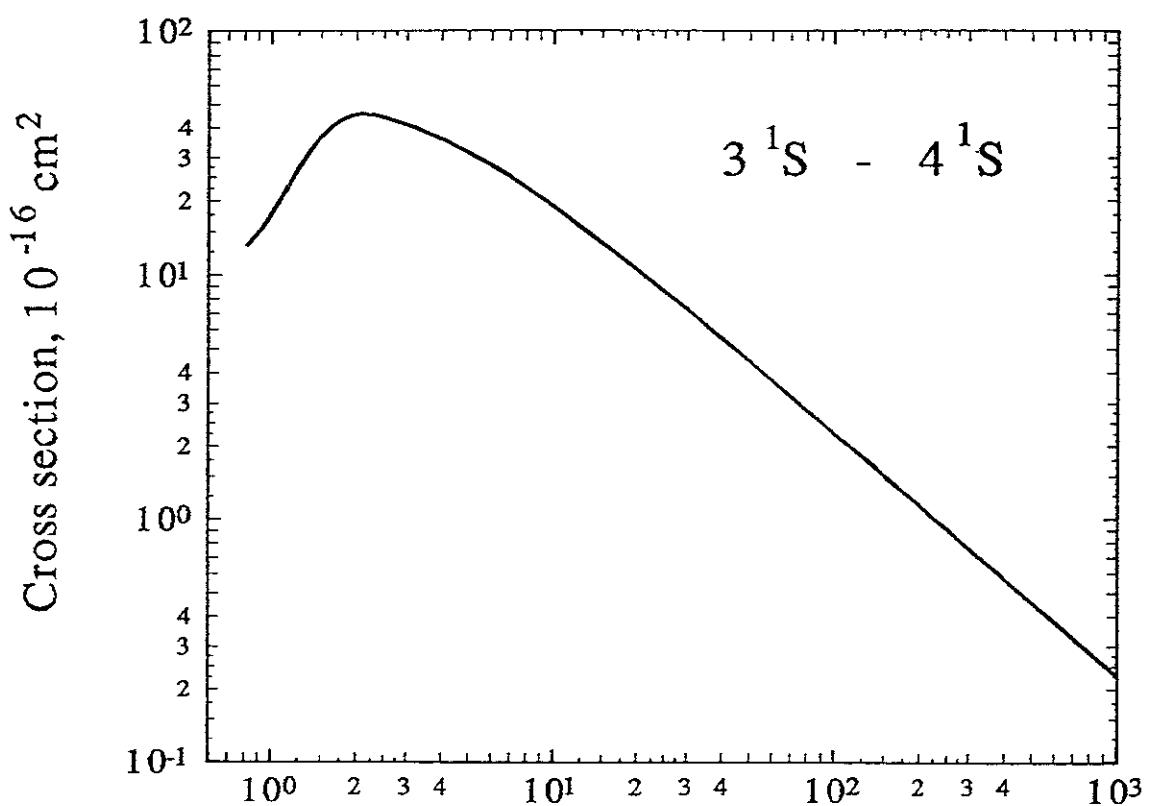


Fig.54 Electron energy, eV

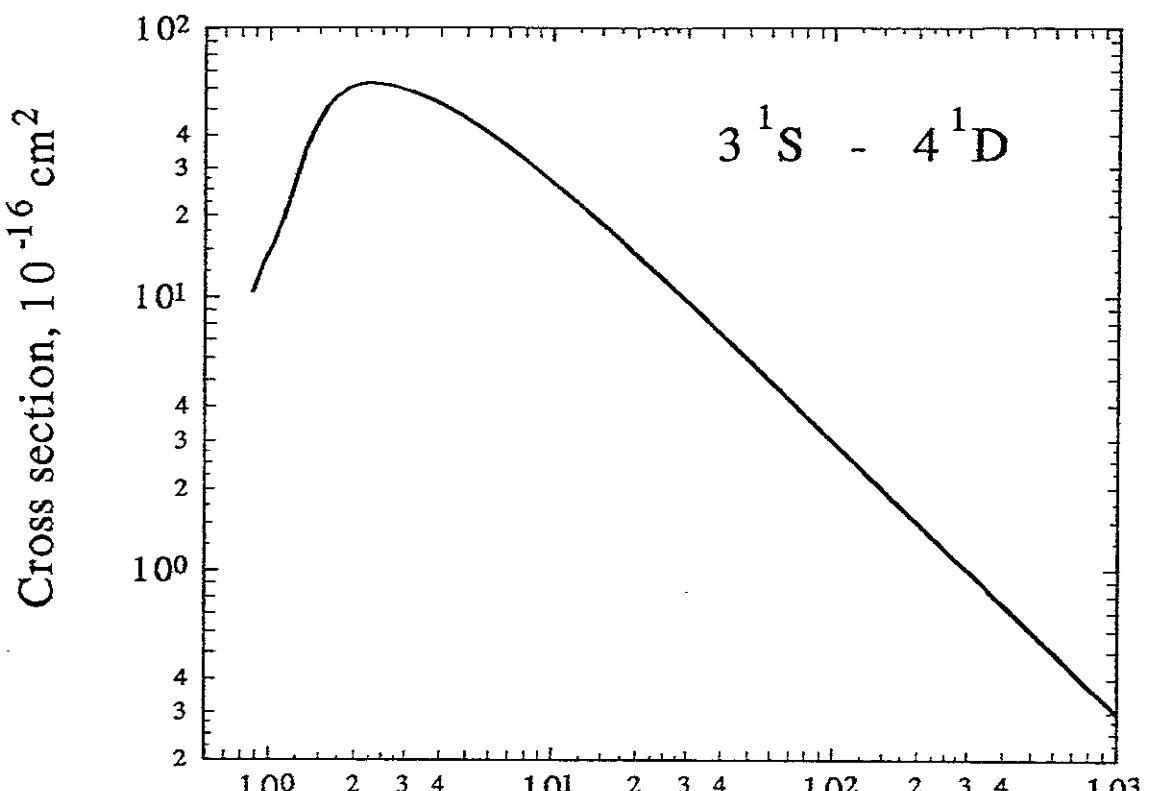


Fig.55 Electron energy, eV

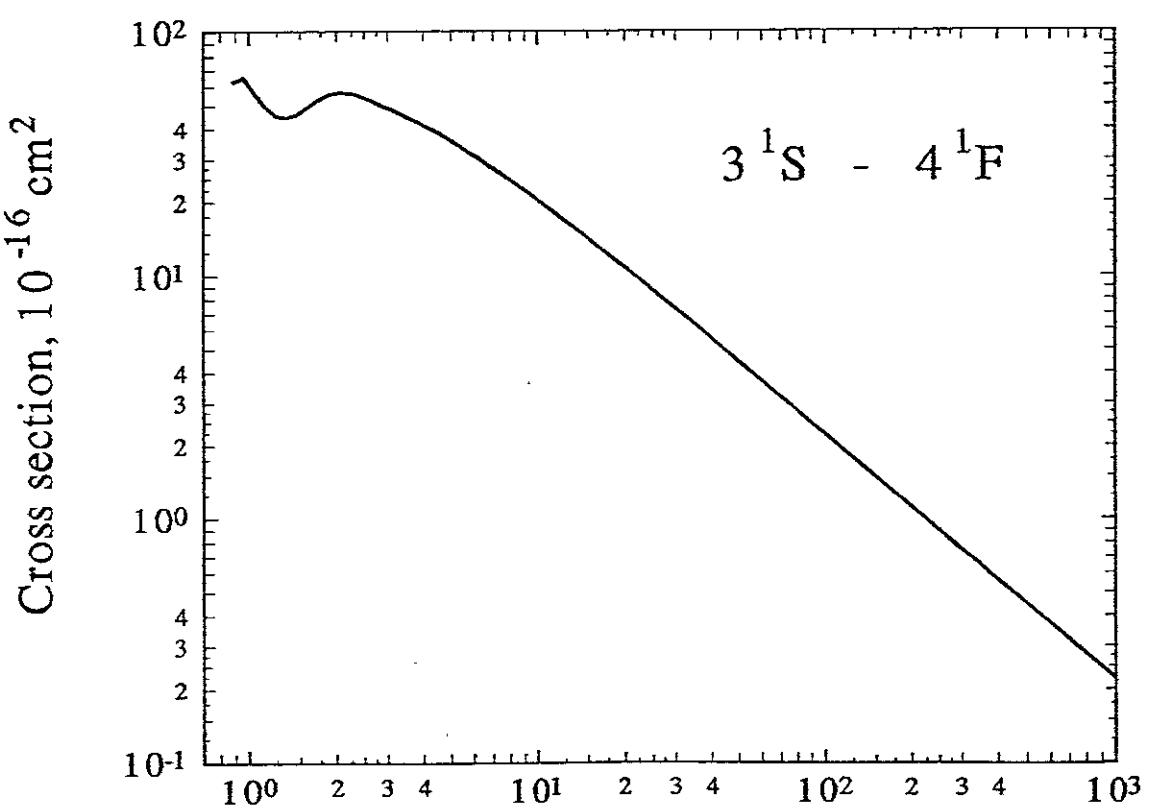
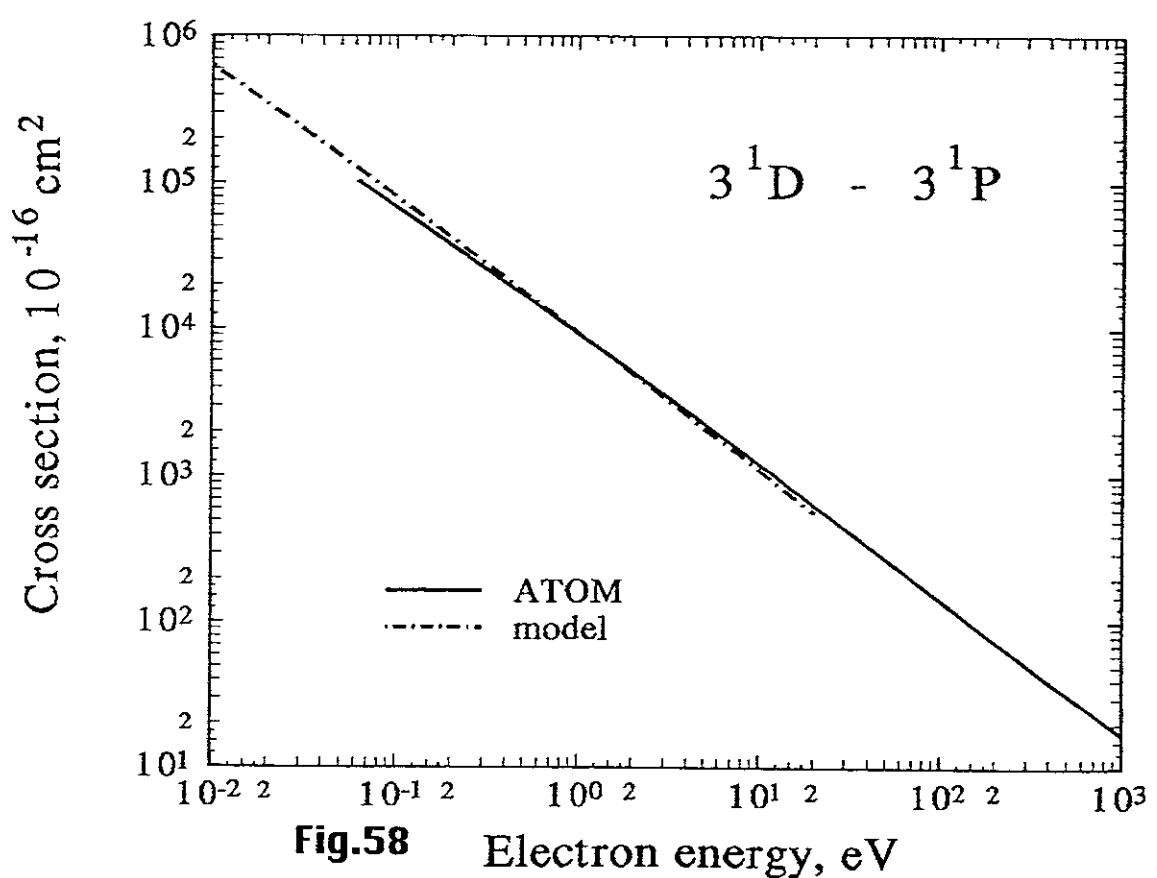
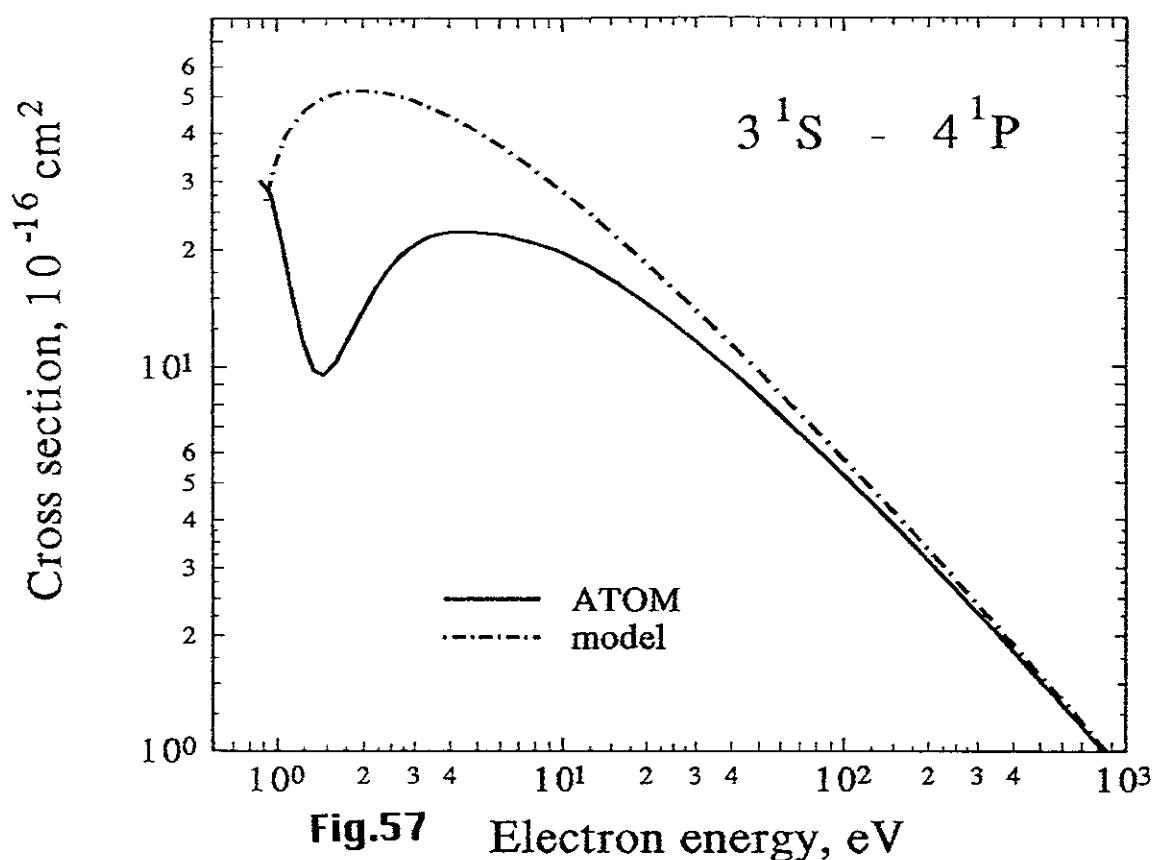


Fig.56 Electron energy, eV



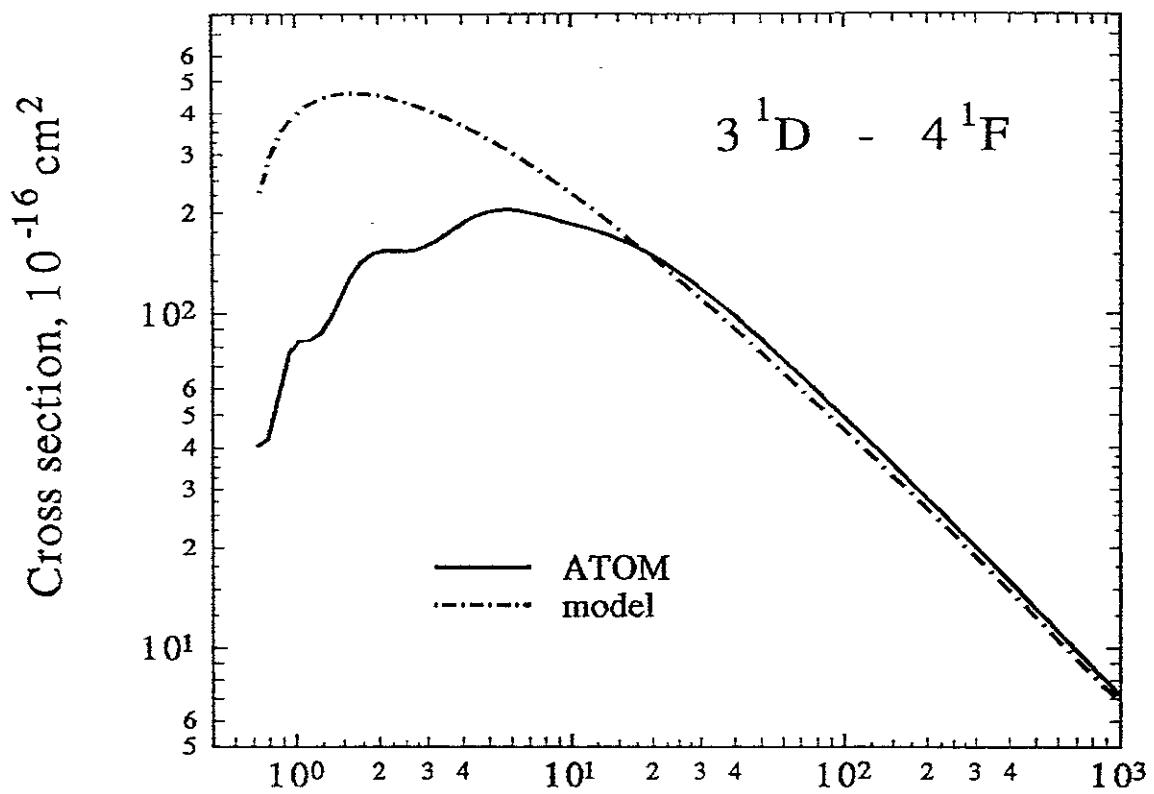


Fig.61 Electron energy, eV

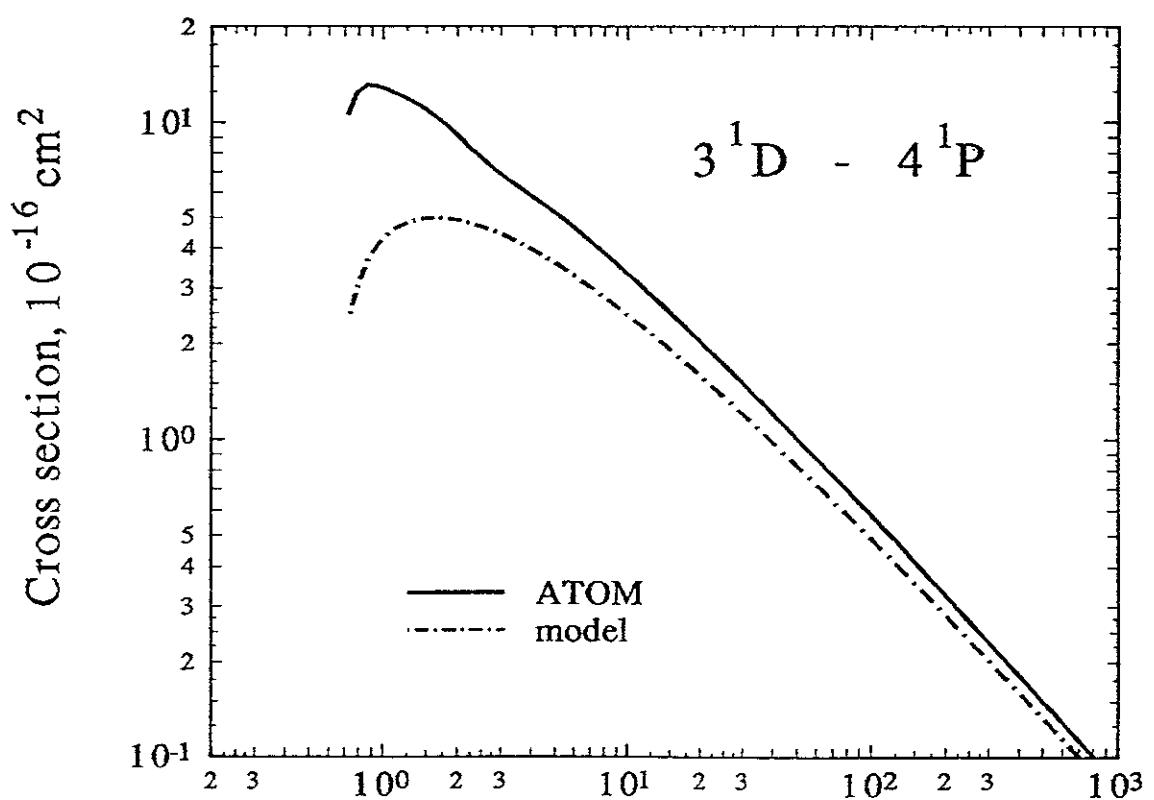


Fig.62 Electron energy, eV

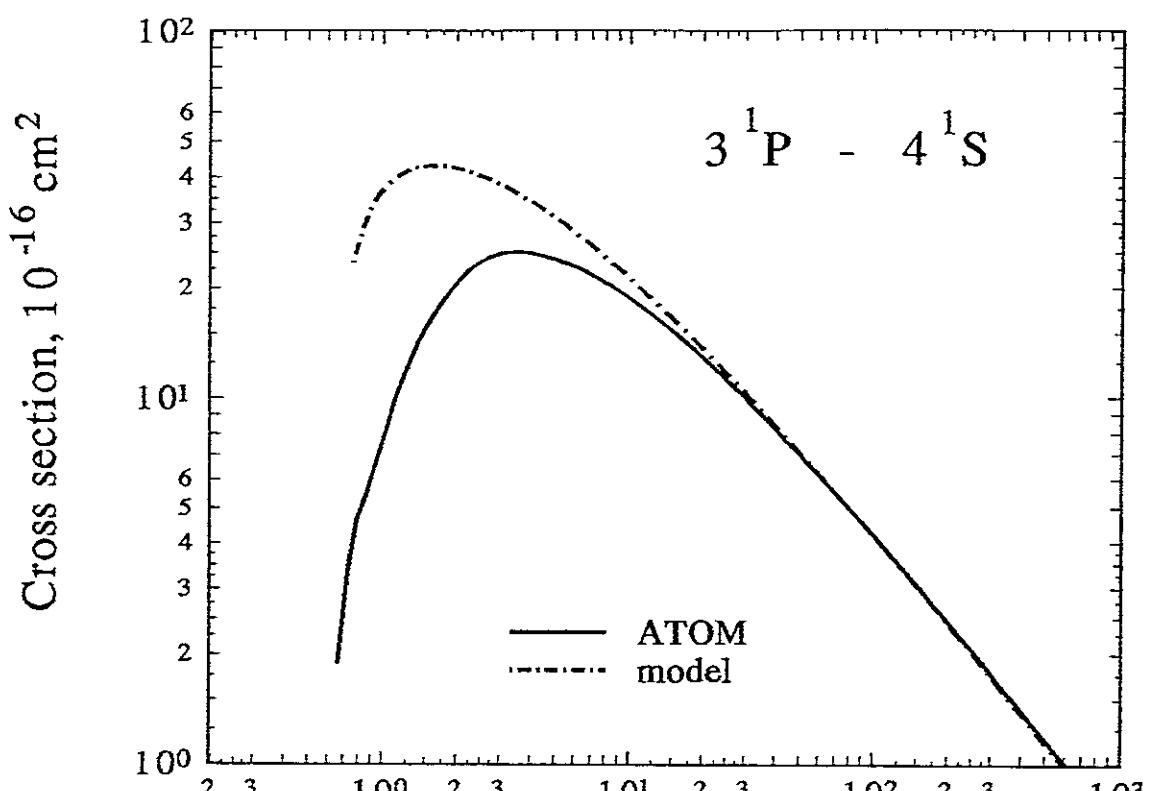


Fig.63 Electron energy, eV

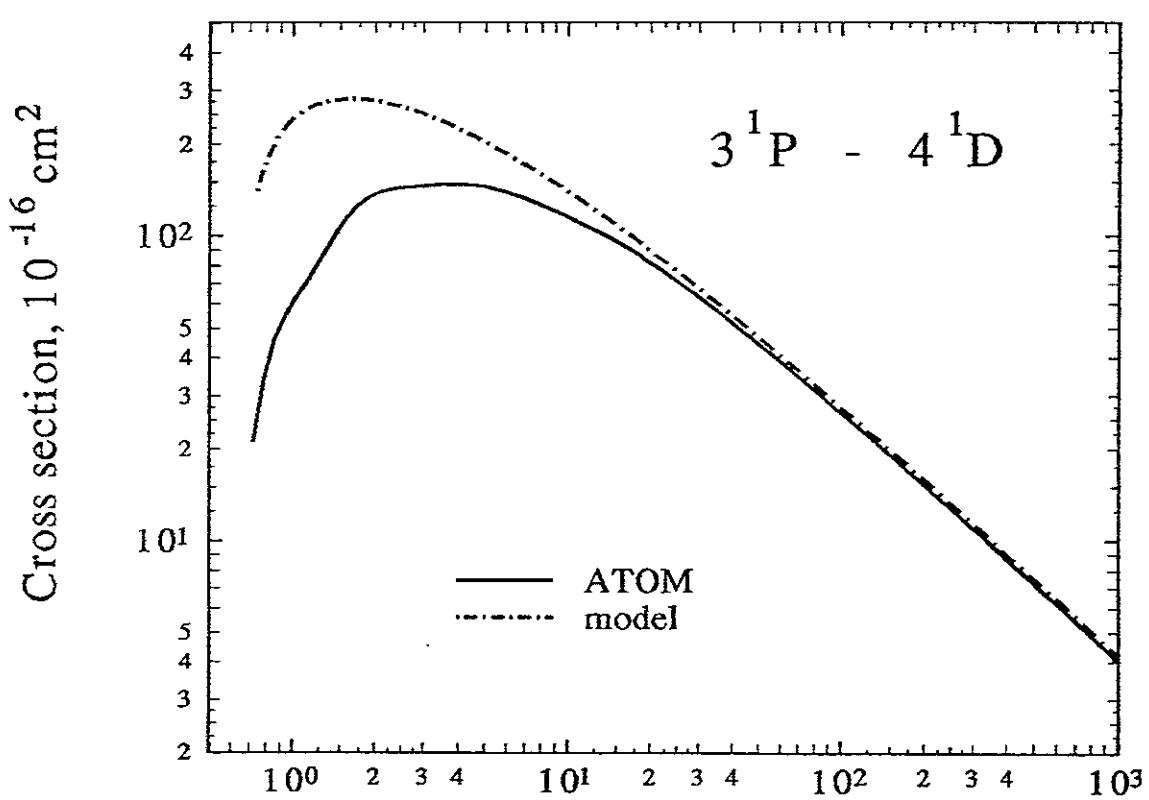


Fig.64 Electron energy, eV

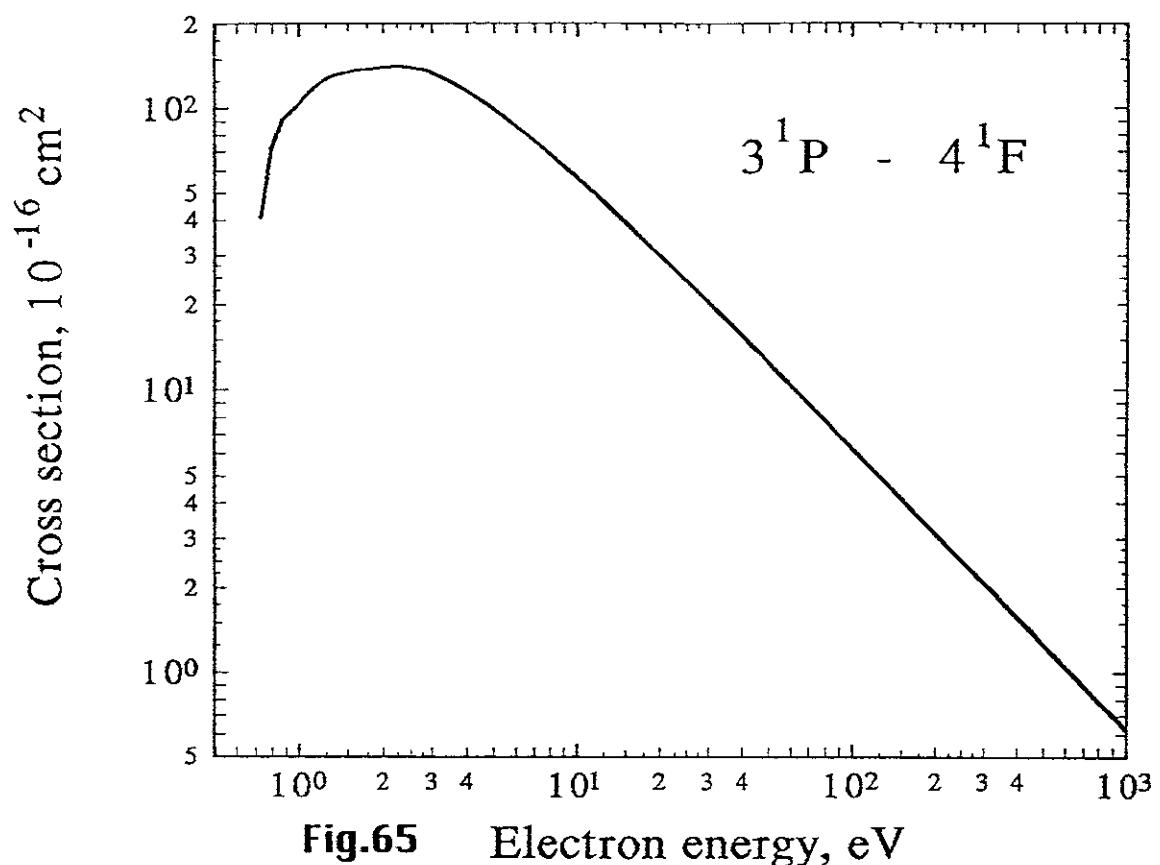


Fig.65 Electron energy, eV

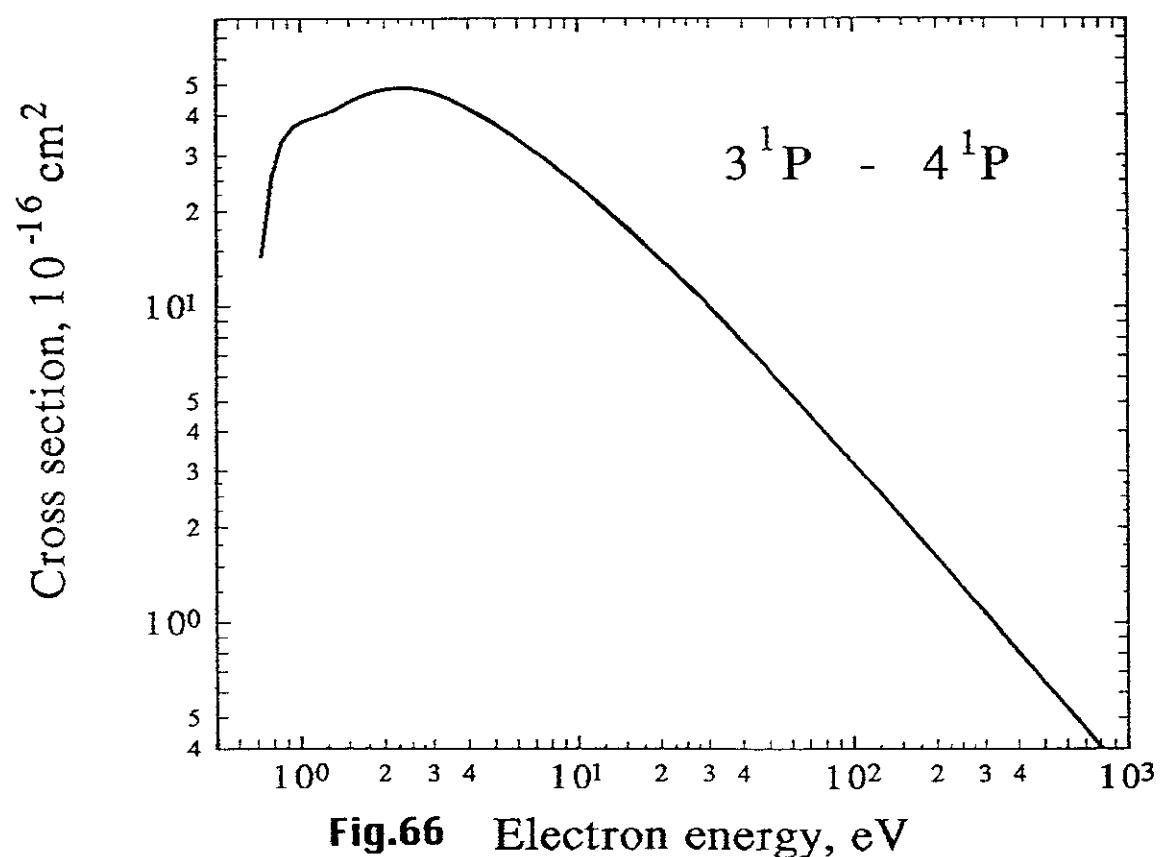


Fig.66 Electron energy, eV

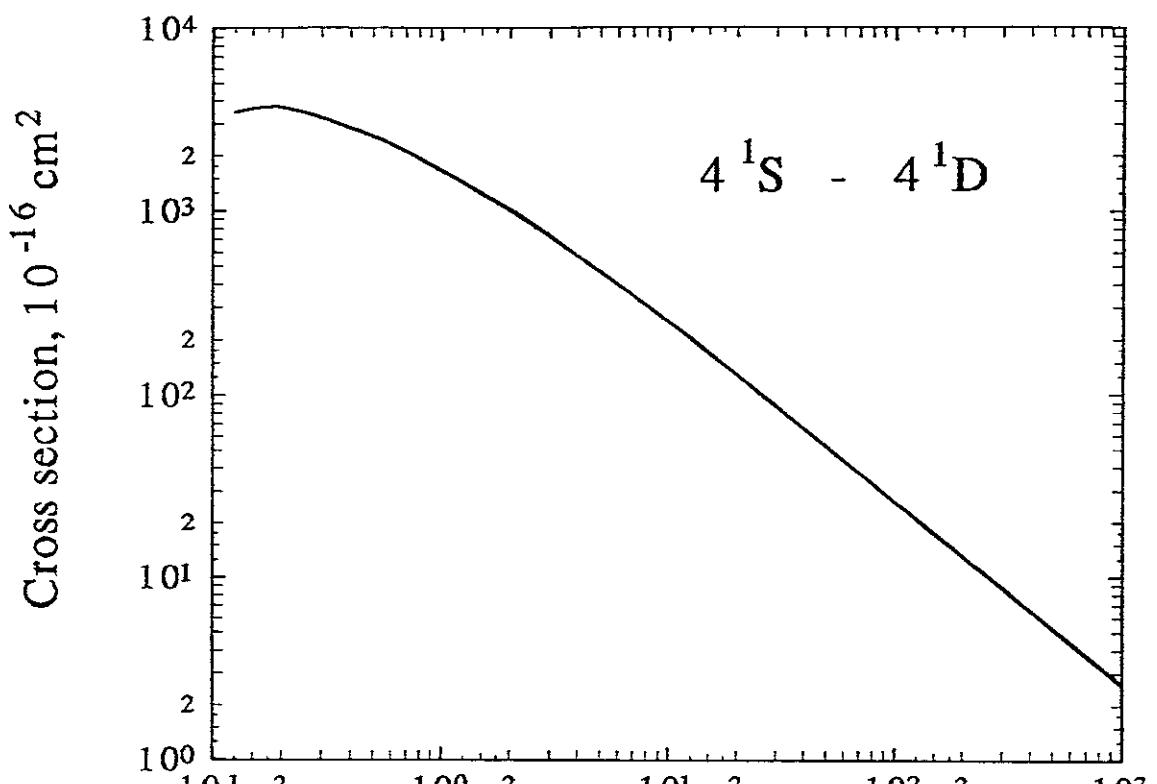


Fig.67 Electron energy, eV

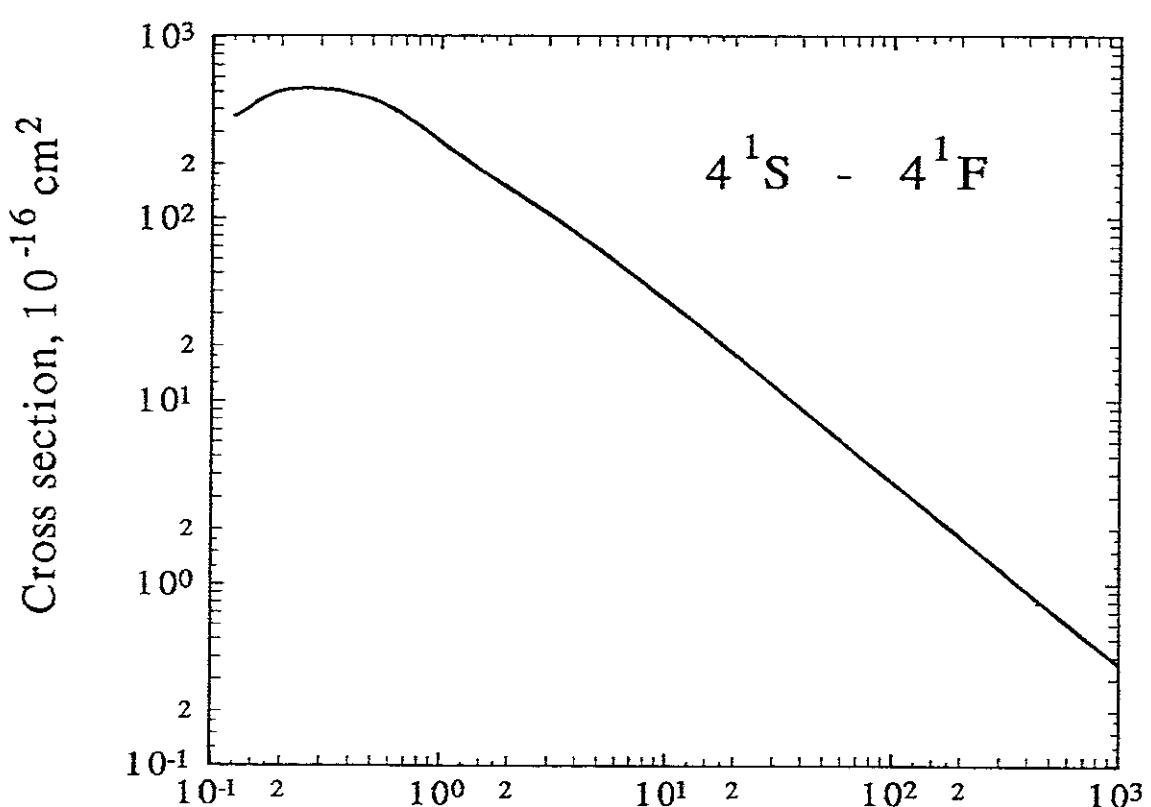


Fig.68 Electron energy, eV

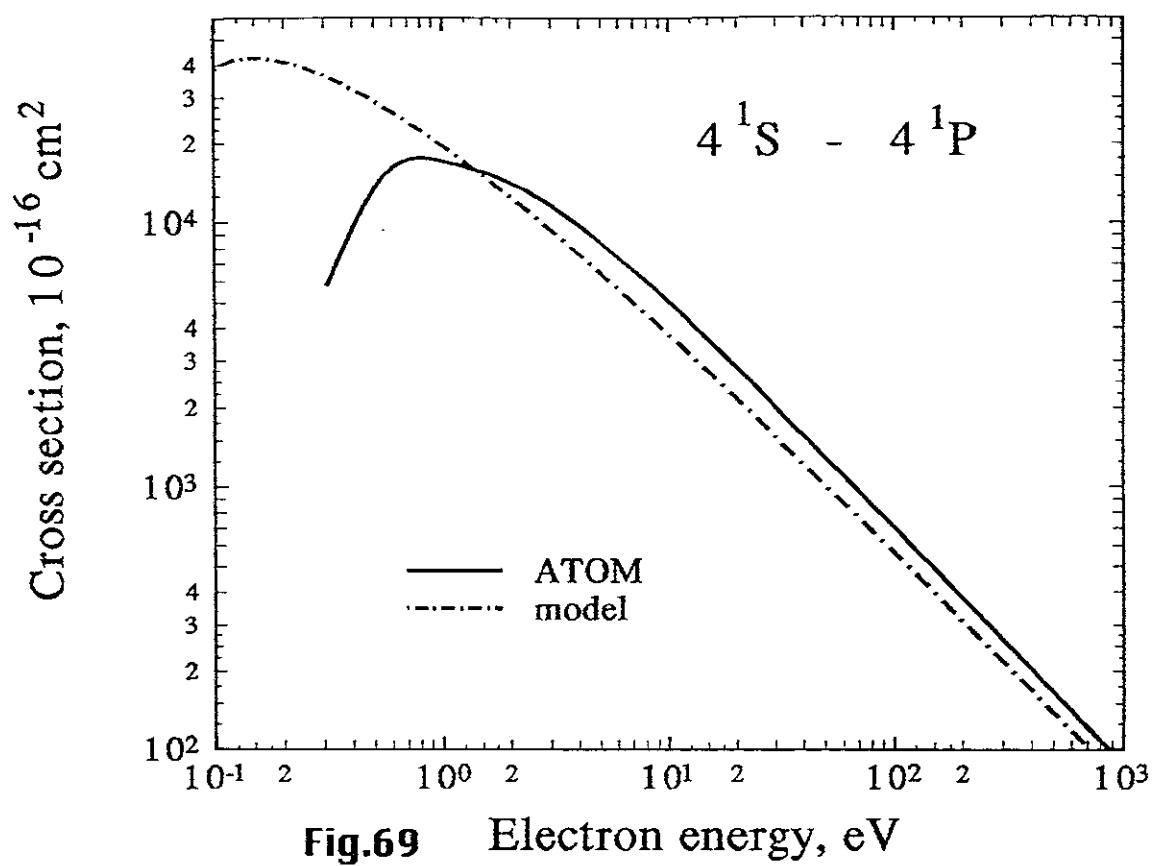


Fig.69 Electron energy, eV

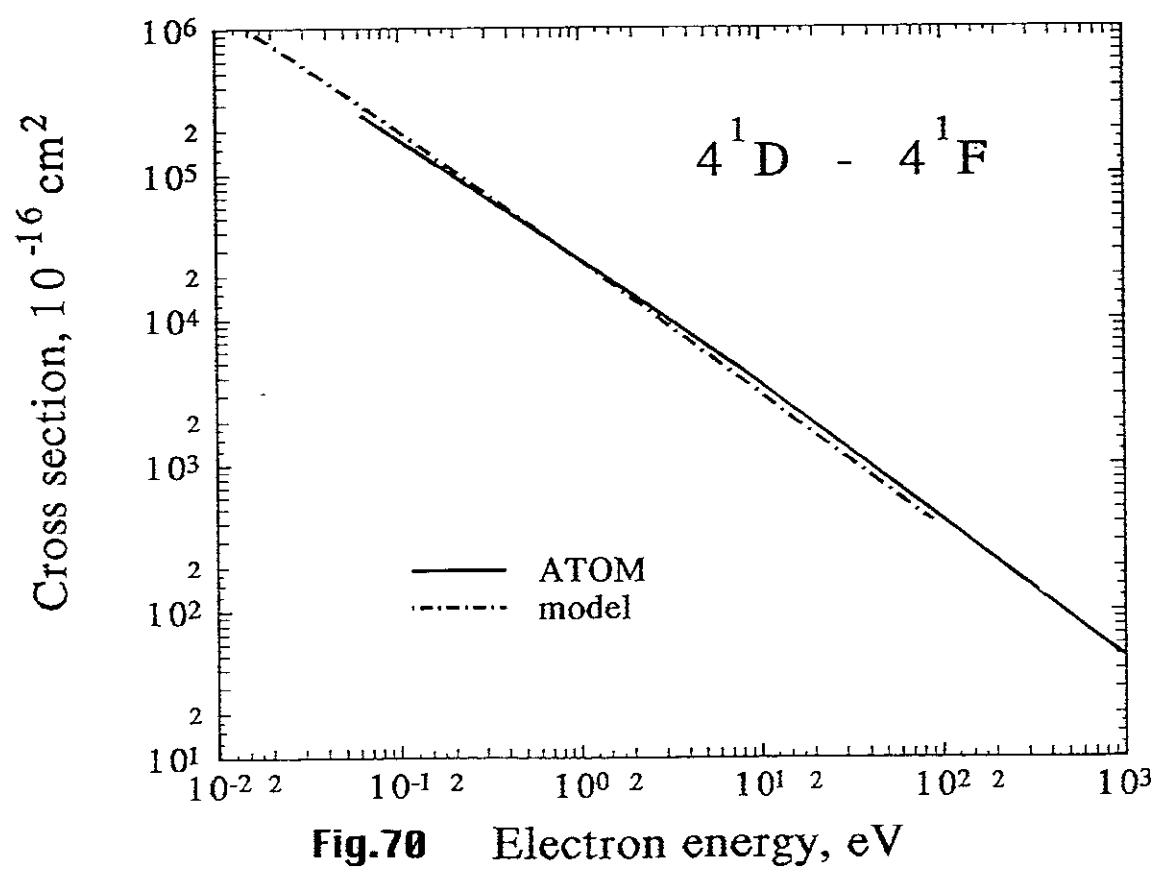


Fig.70 Electron energy, eV

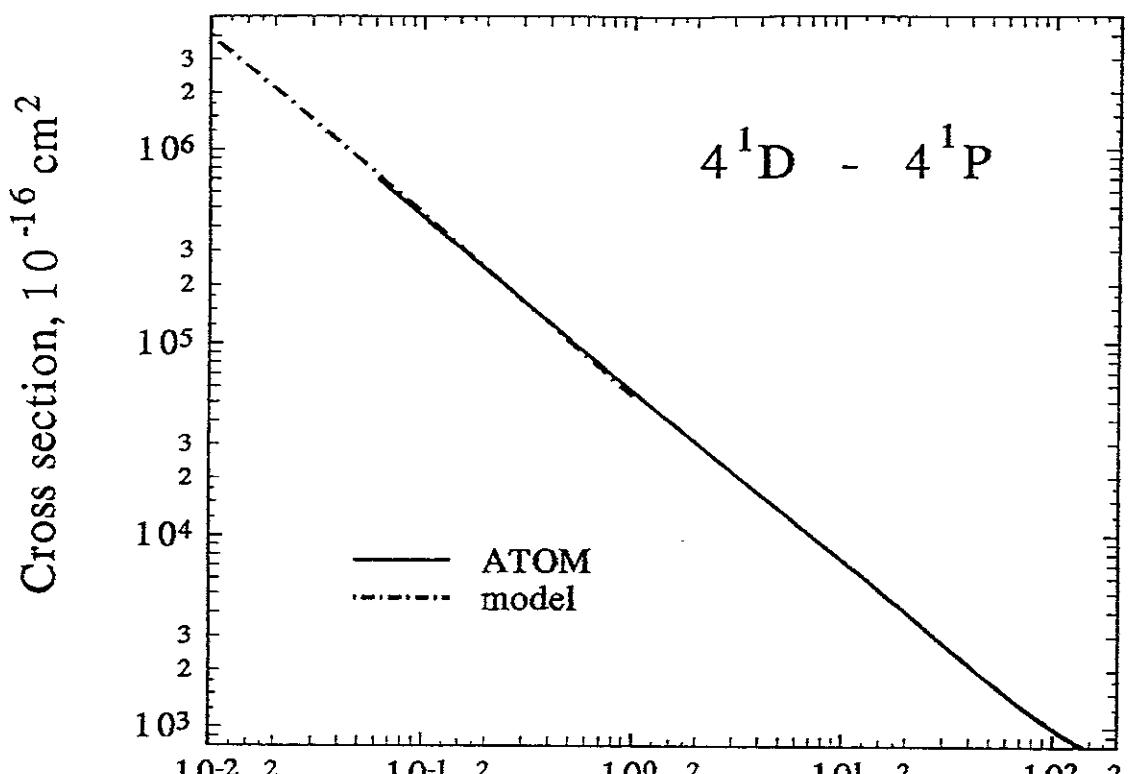


Fig.71 Electron energy, eV

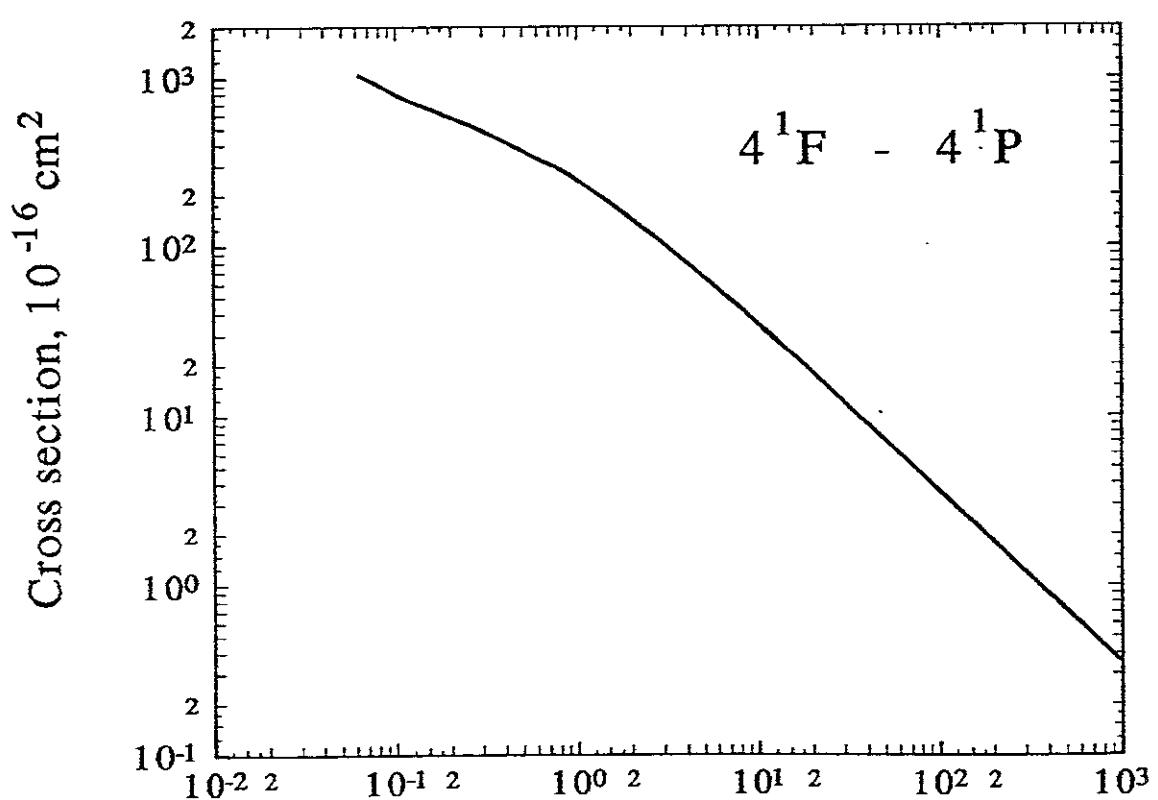


Fig.72 Electron energy, eV

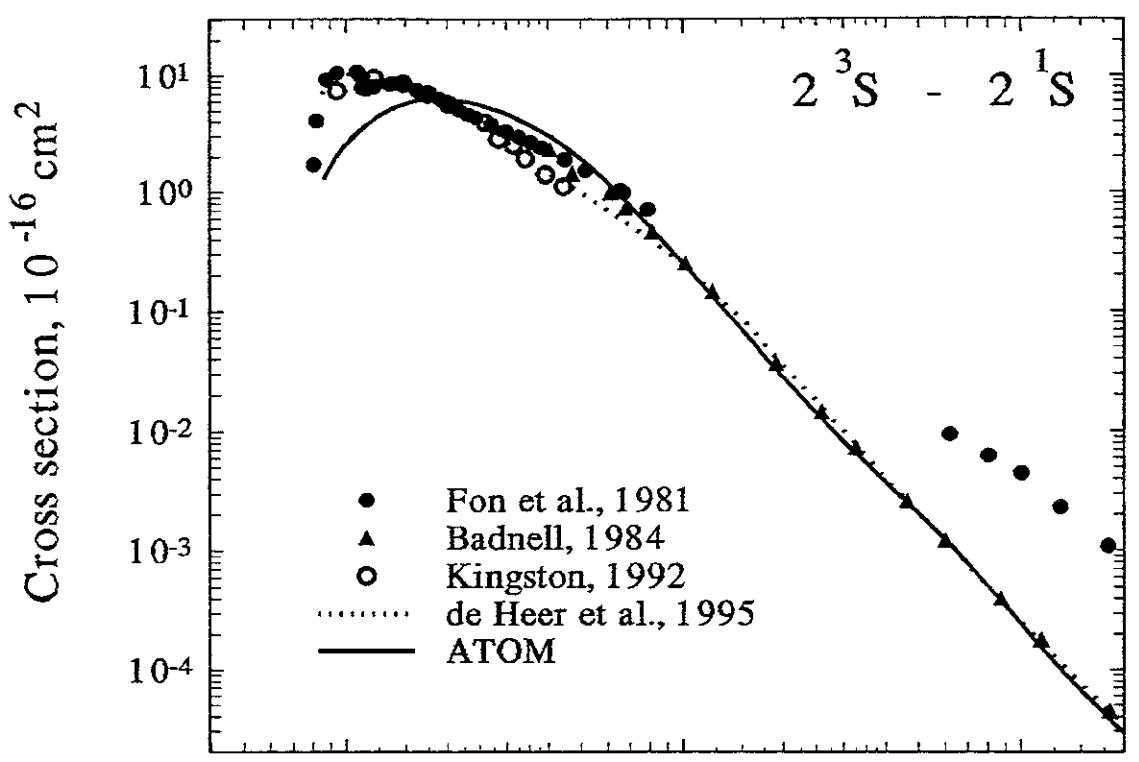


Fig.73 Electron energy, eV

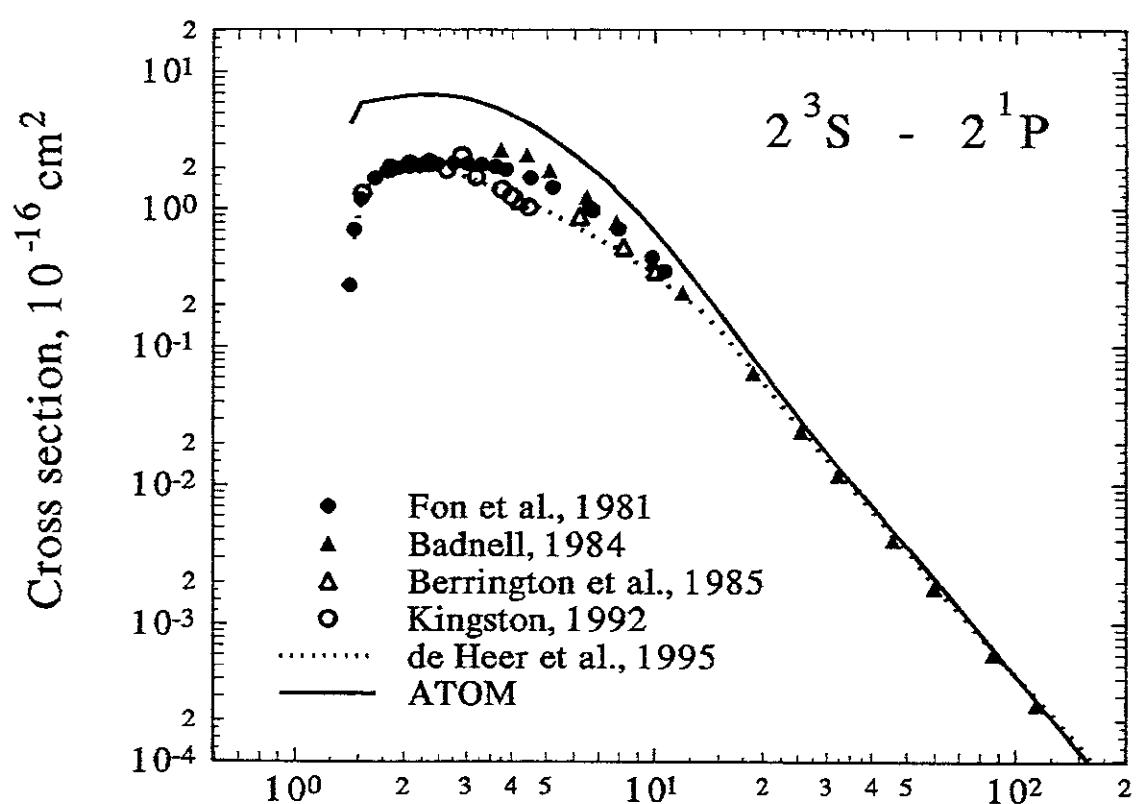


Fig.74 Electron energy, eV

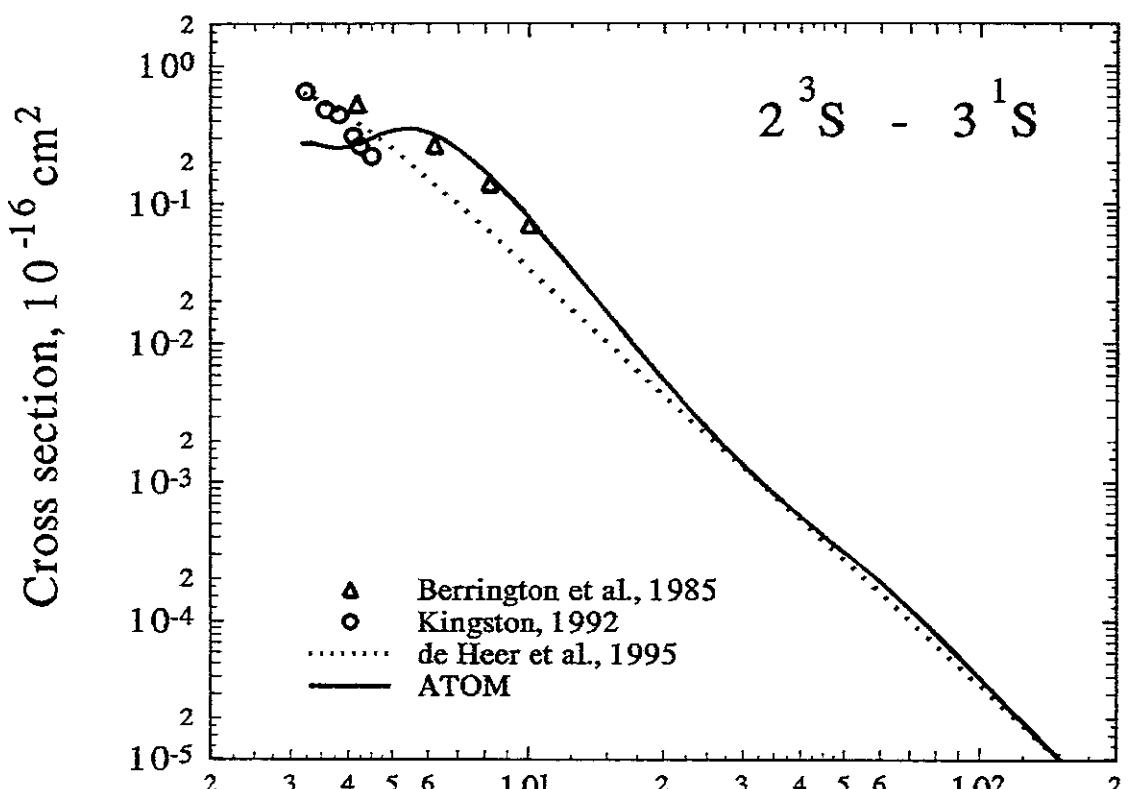


Fig. 75 Electron energy, eV

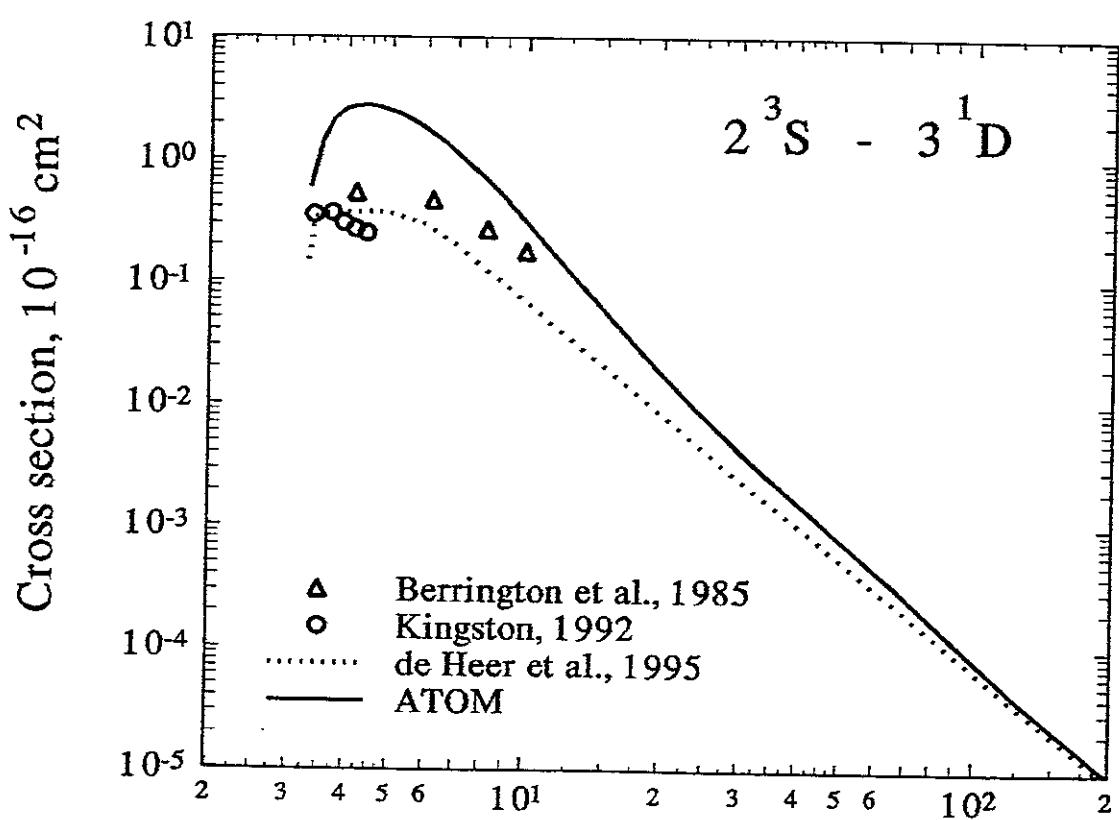


Fig. 76 Electron energy, eV

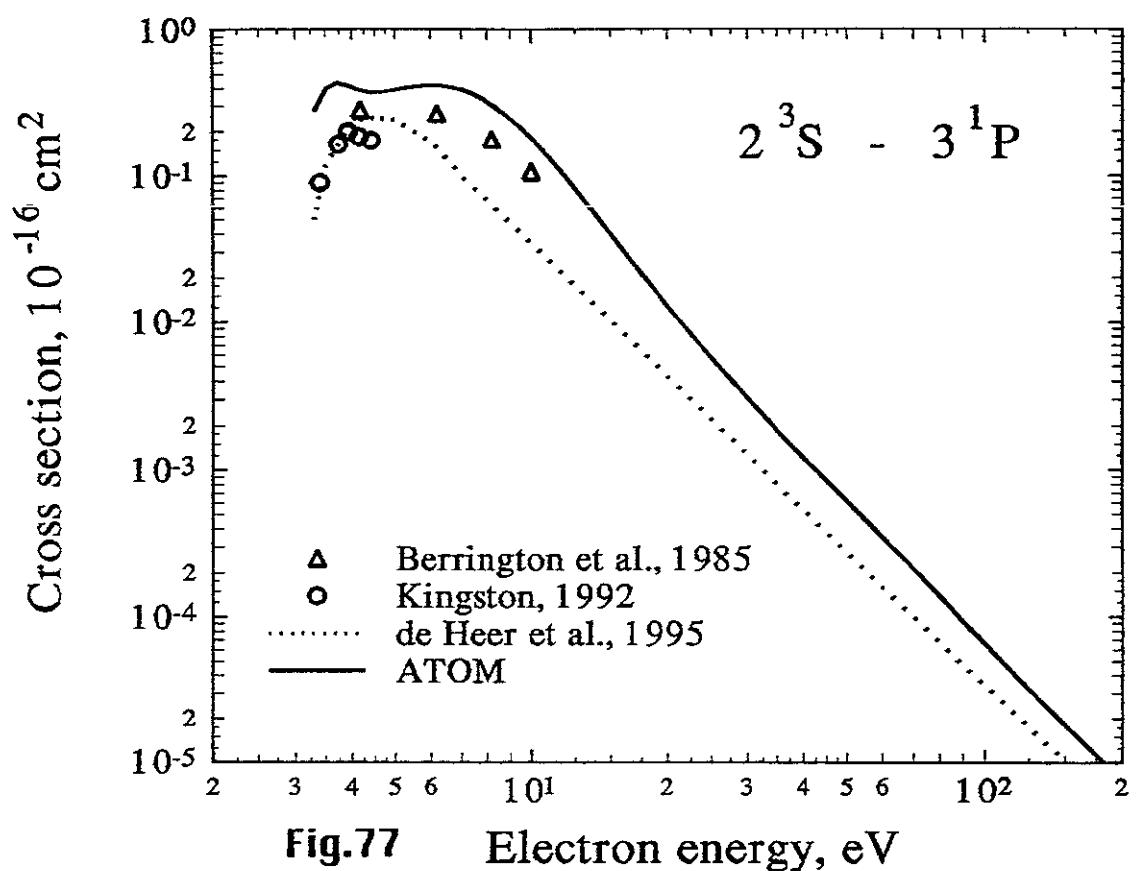


Fig.77 Electron energy, eV

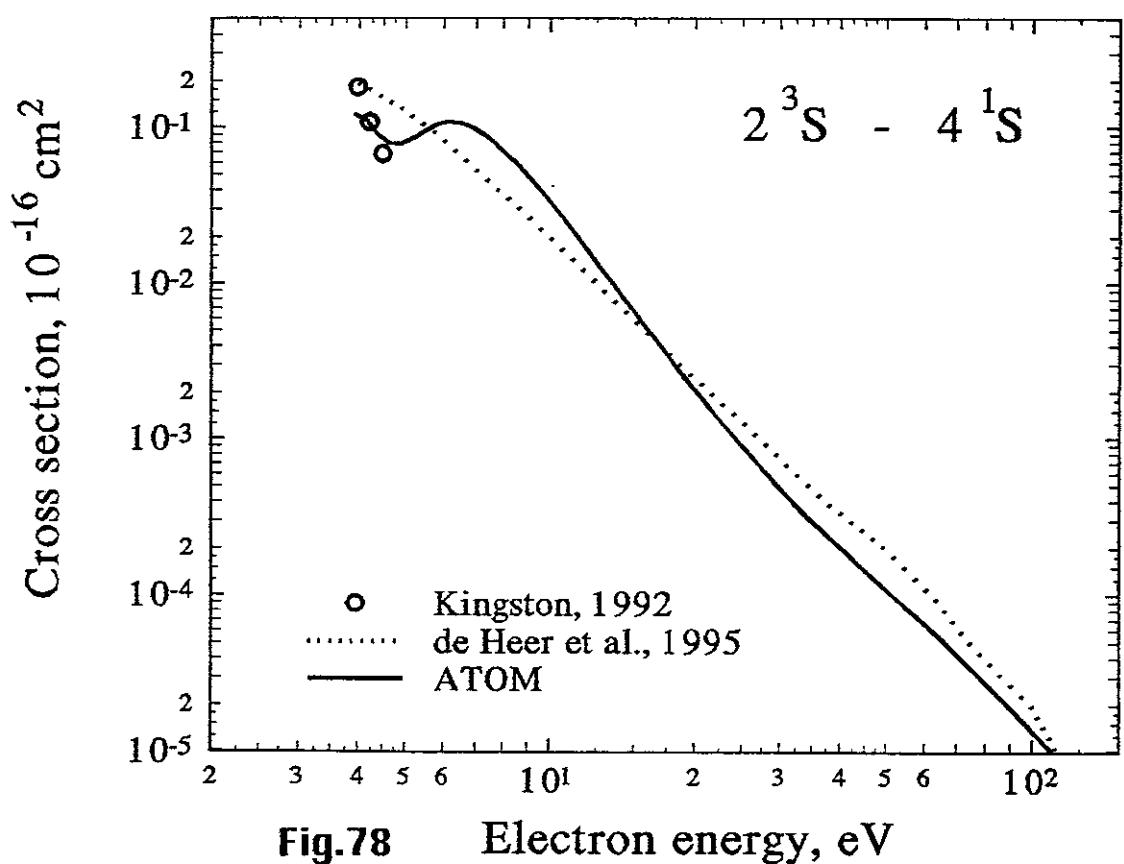


Fig.78 Electron energy, eV

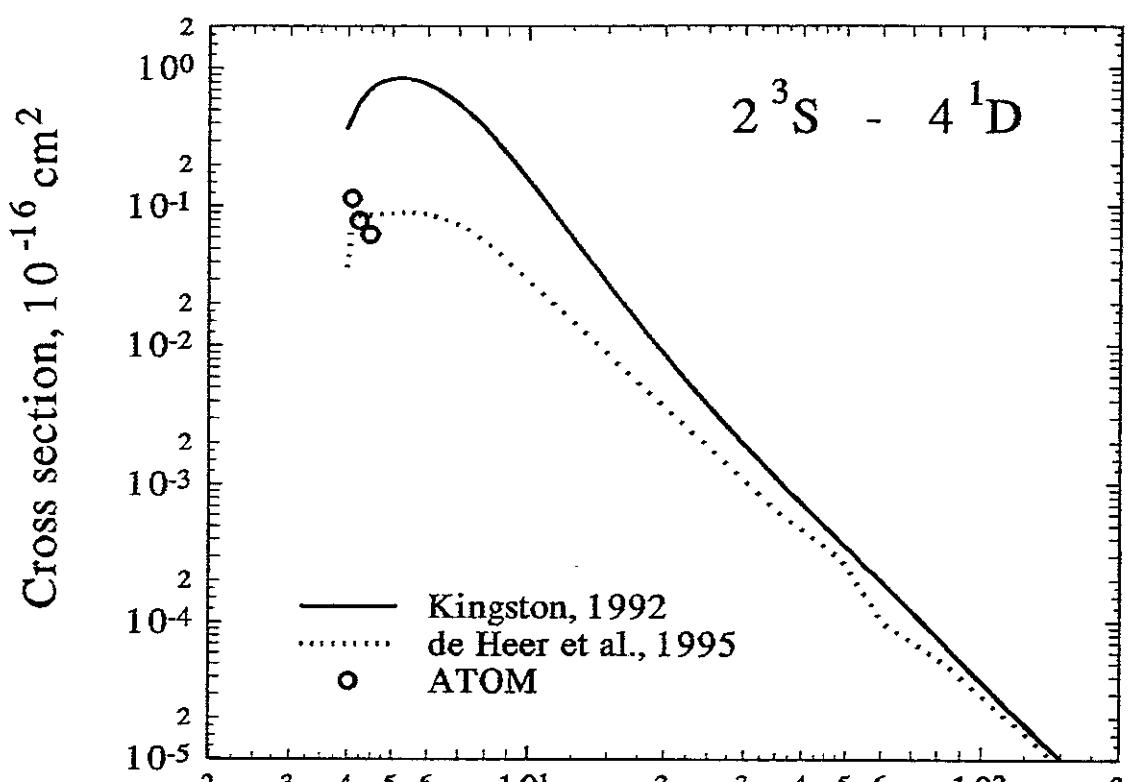


Fig.79 Electron energy, eV

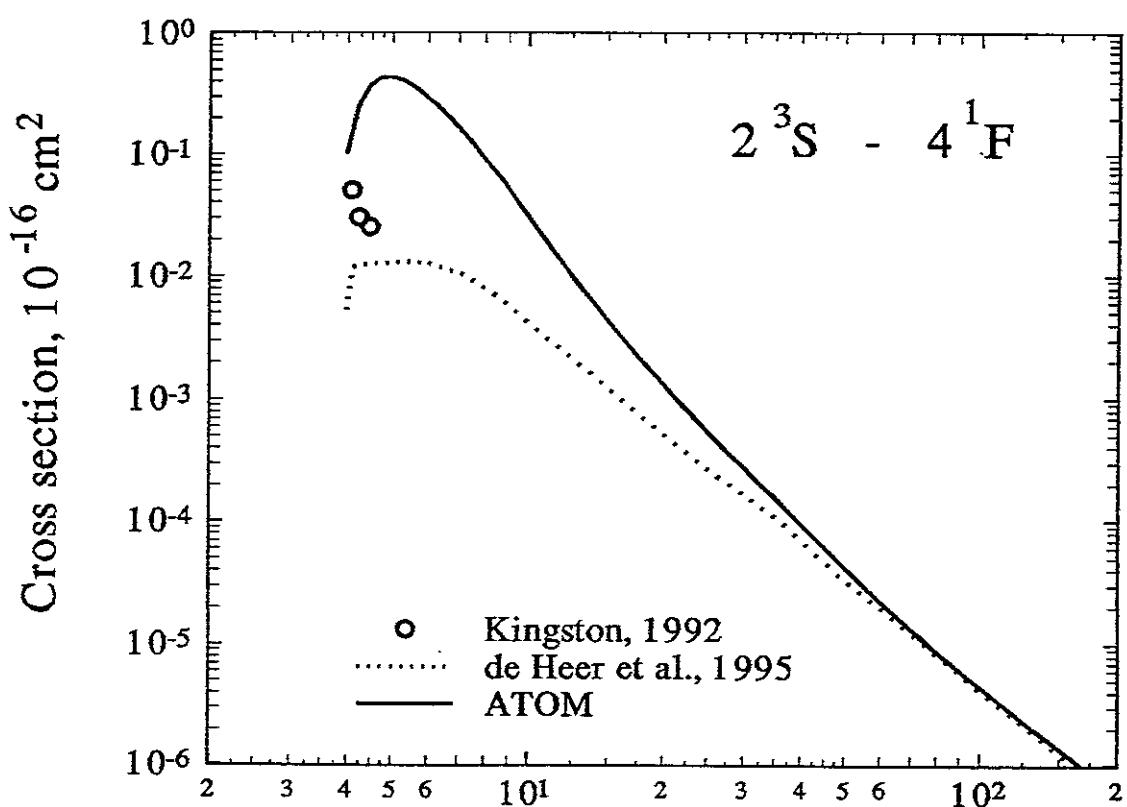


Fig.80 Electron energy, eV

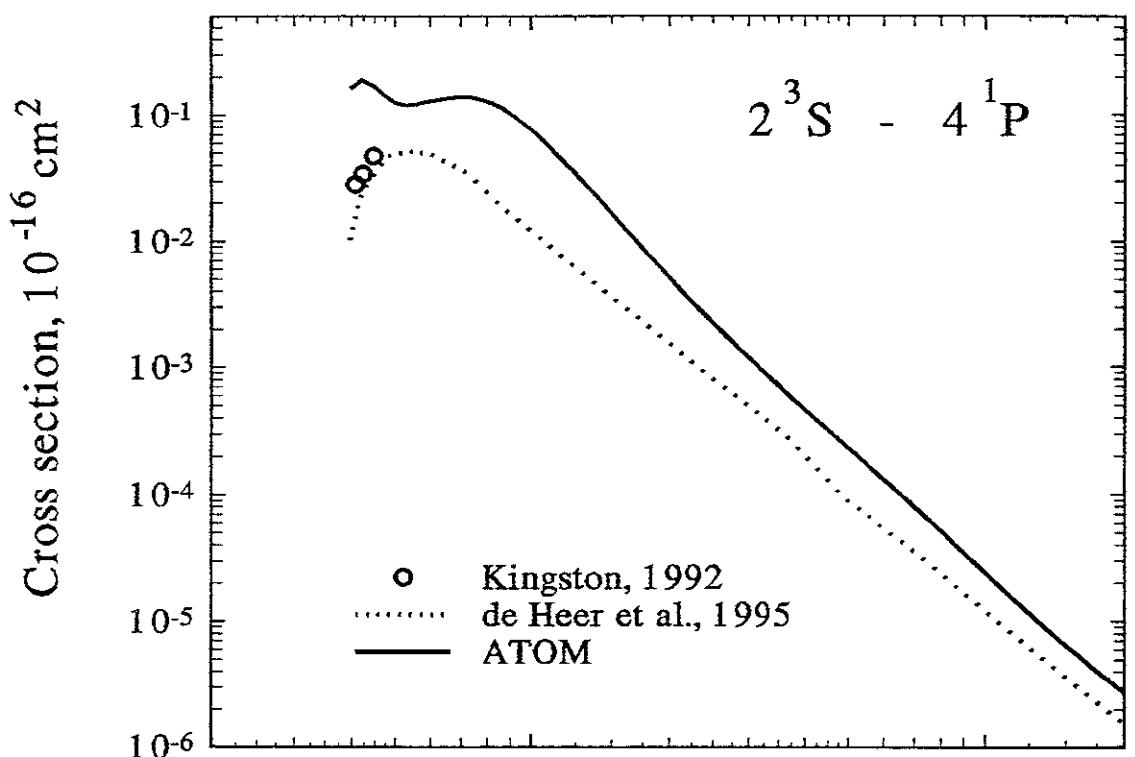


Fig.81 Electron energy, eV

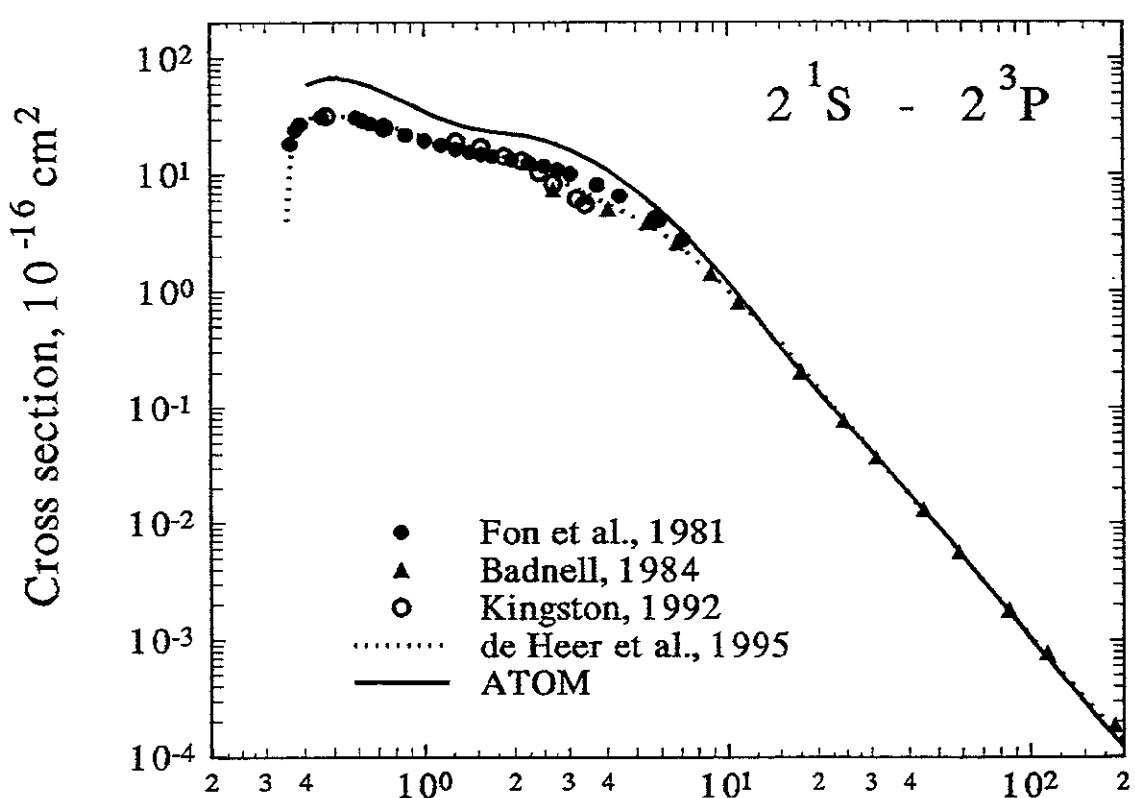


Fig.82 Electron energy, eV

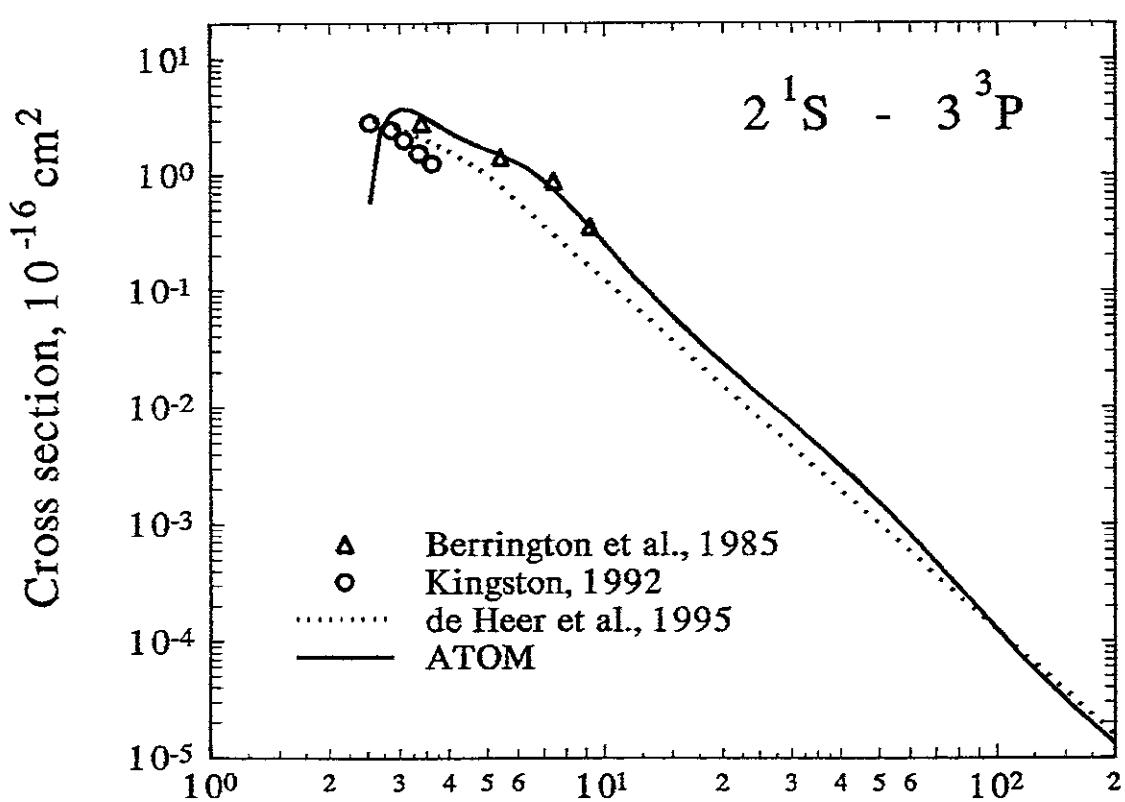
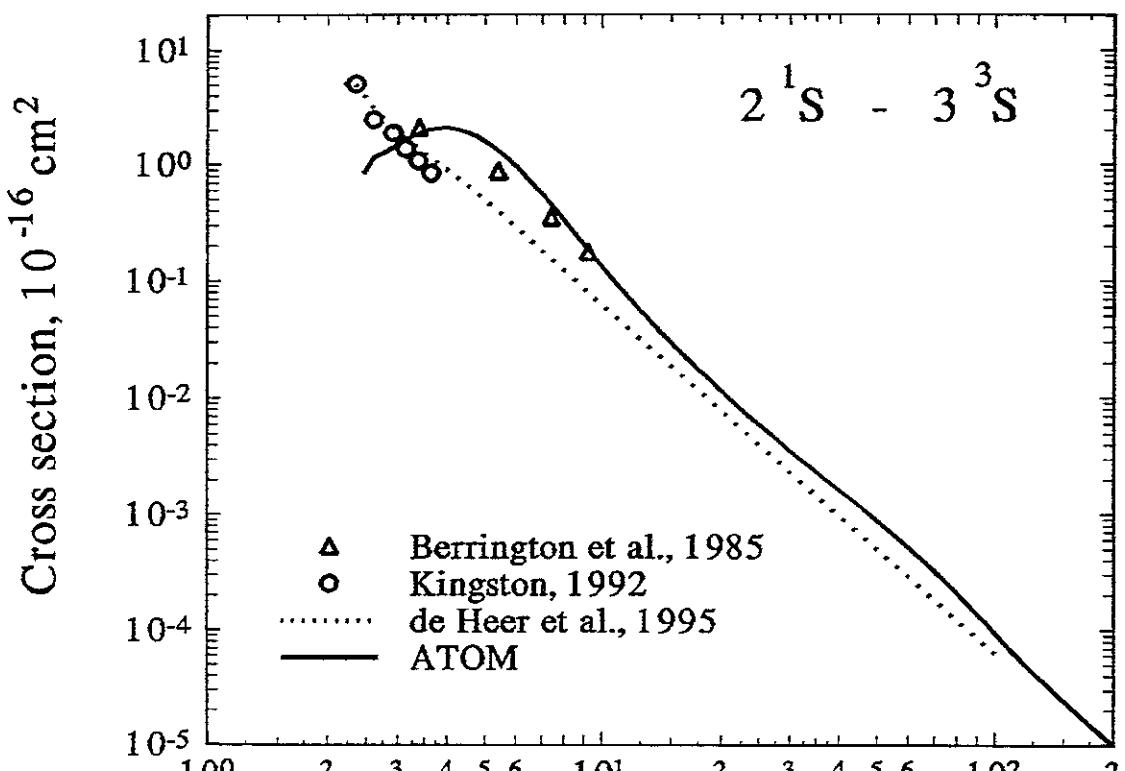


Fig.83 Electron energy, eV

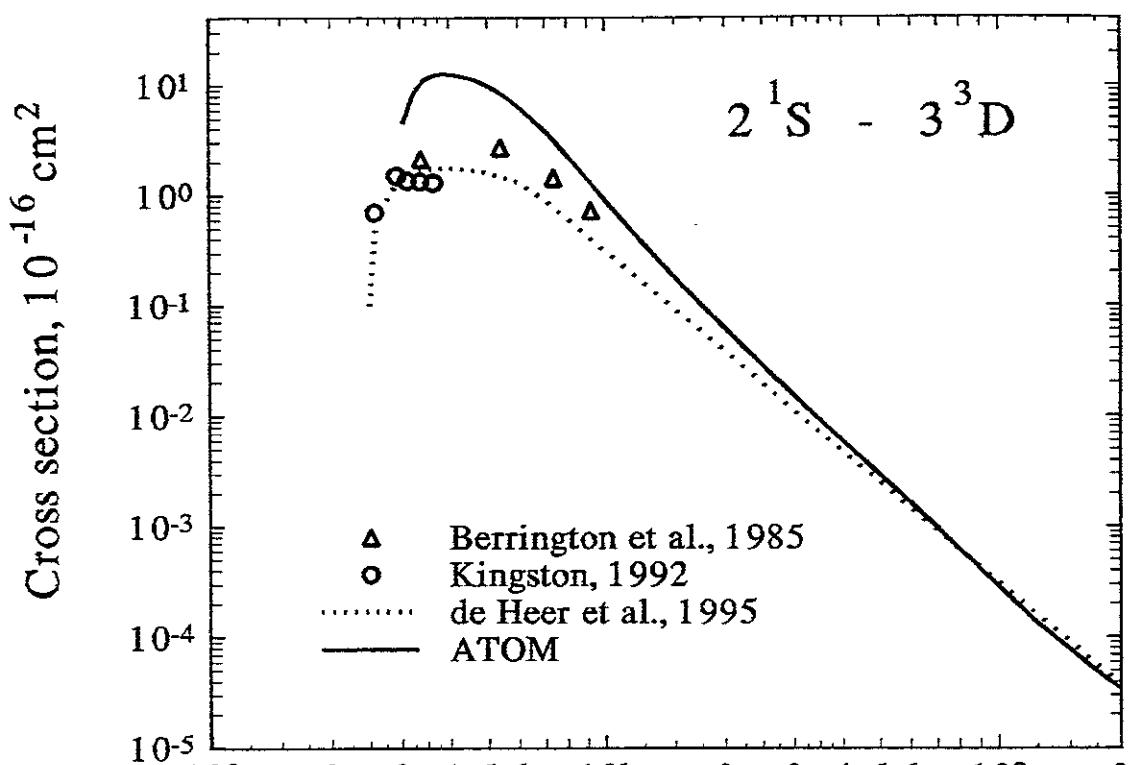


Fig.85 Electron energy, eV

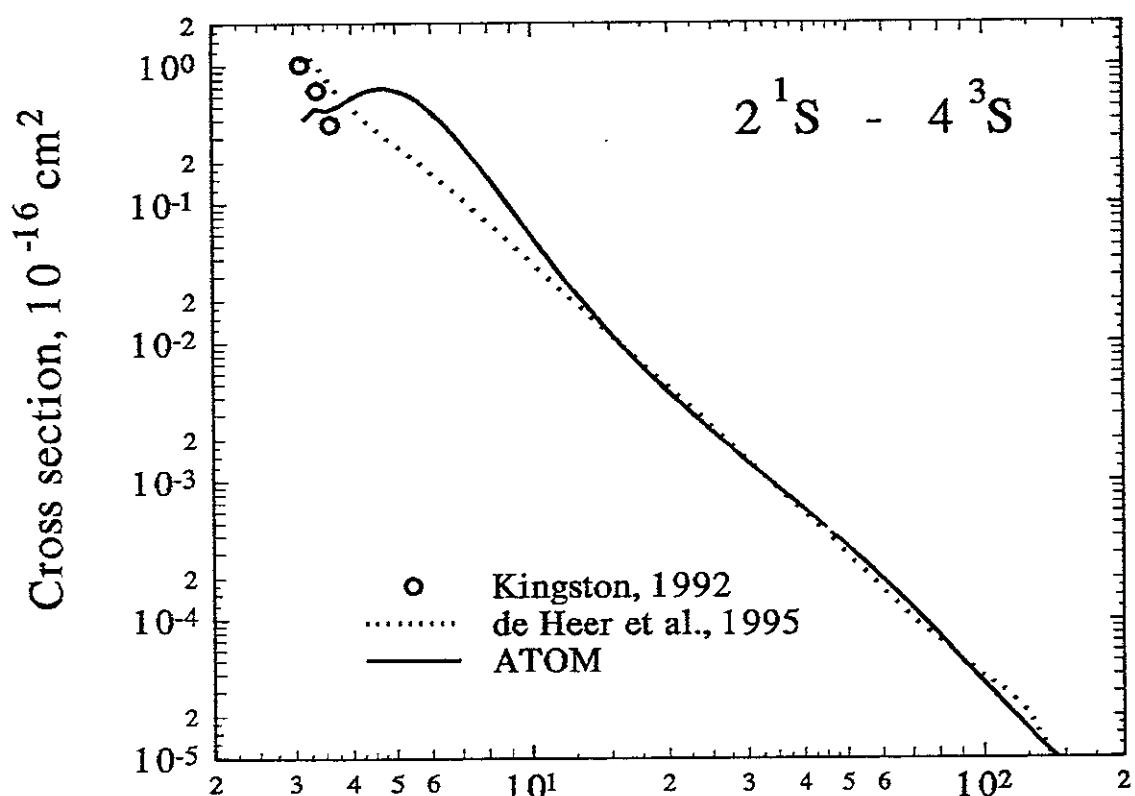


Fig.86 Electron energy, eV

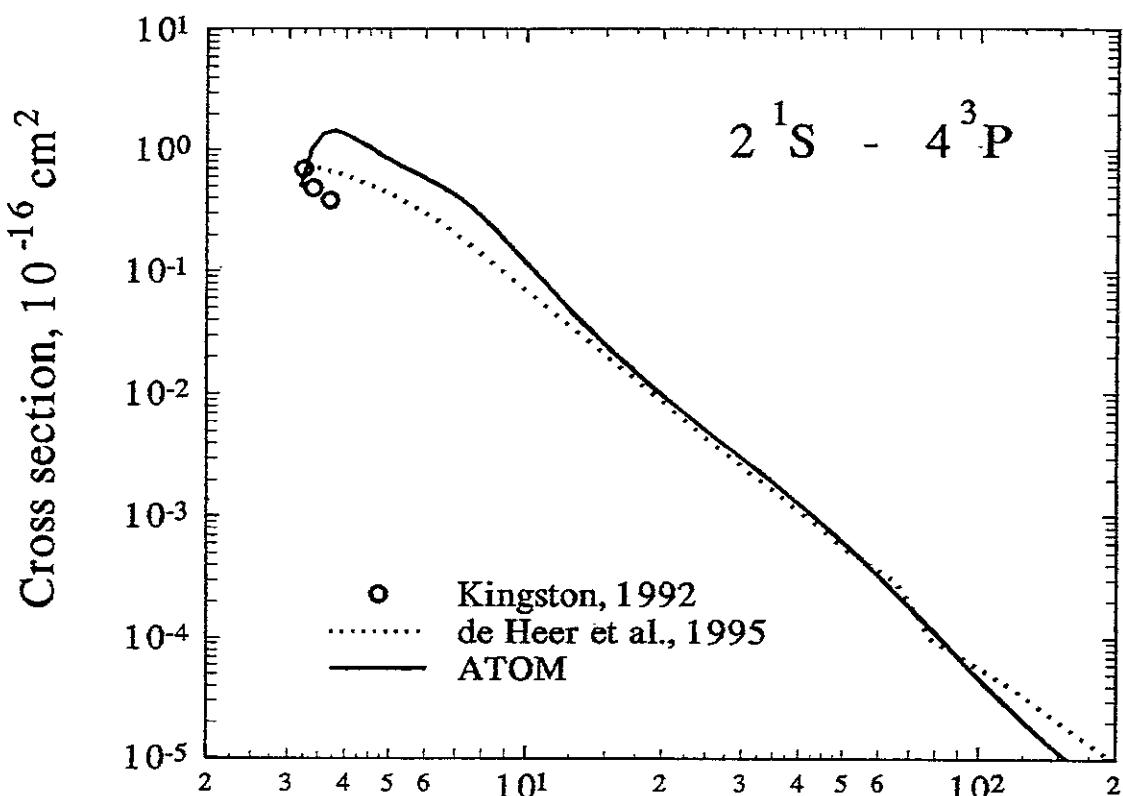


Fig.87 Electron energy, eV

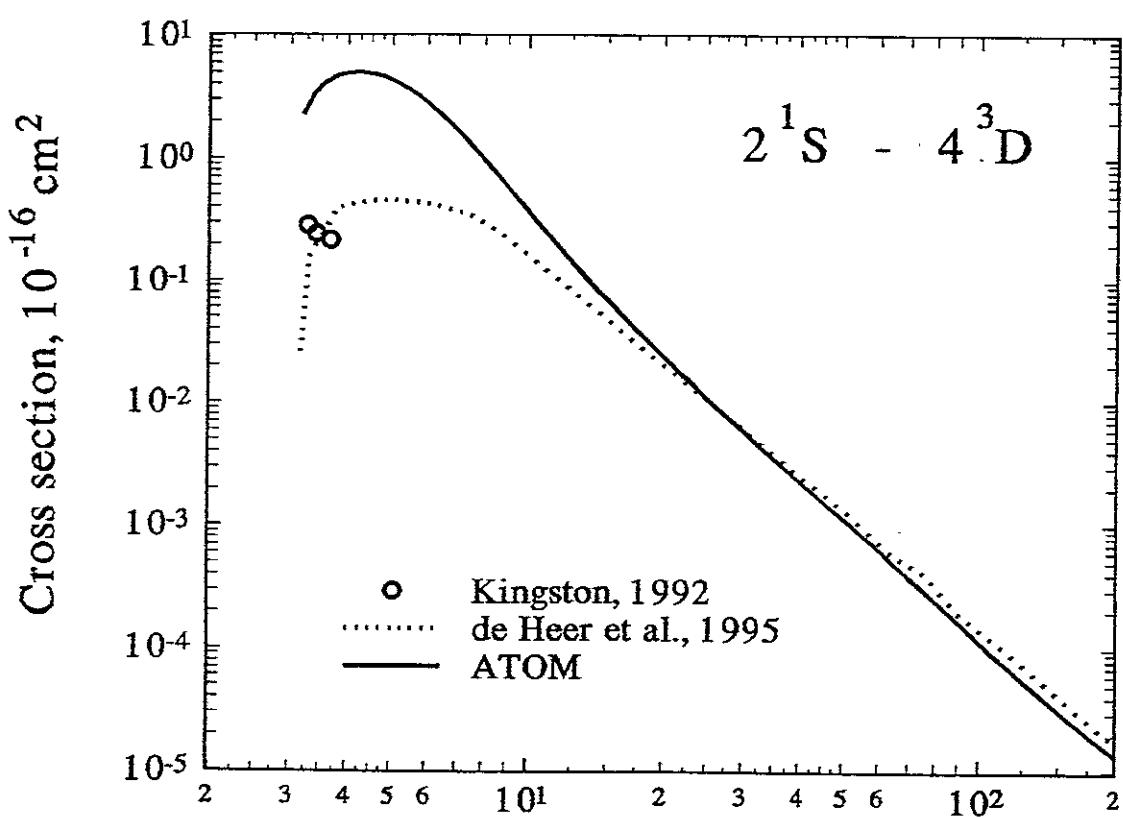


Fig.88 Electron energy, eV

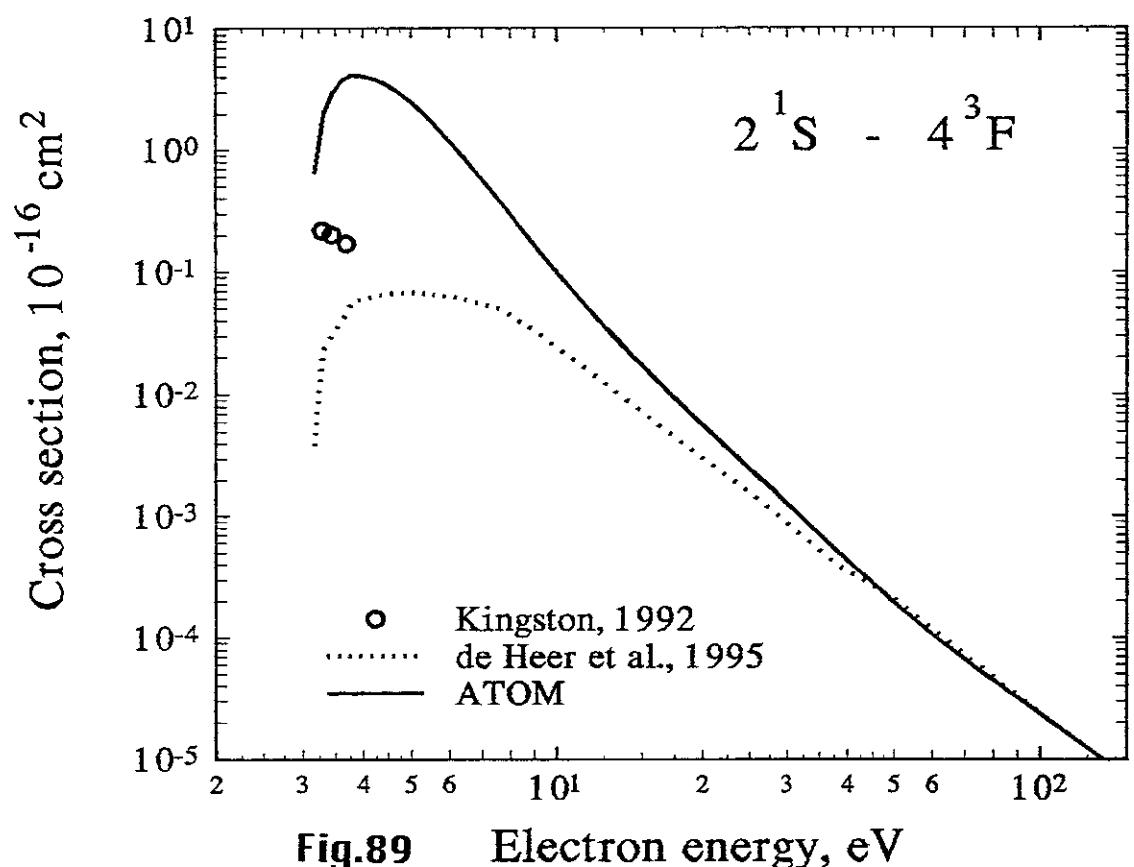


Fig.89 Electron energy, eV

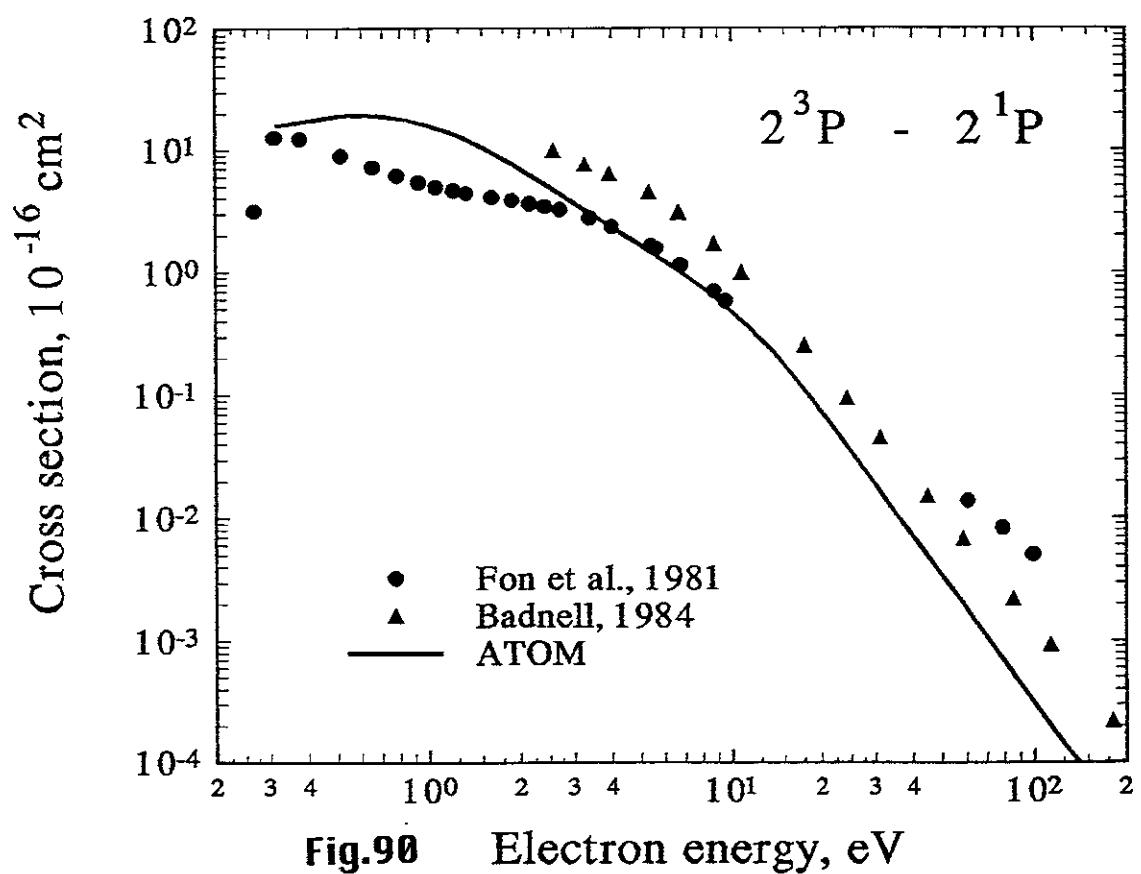


Fig.90 Electron energy, eV

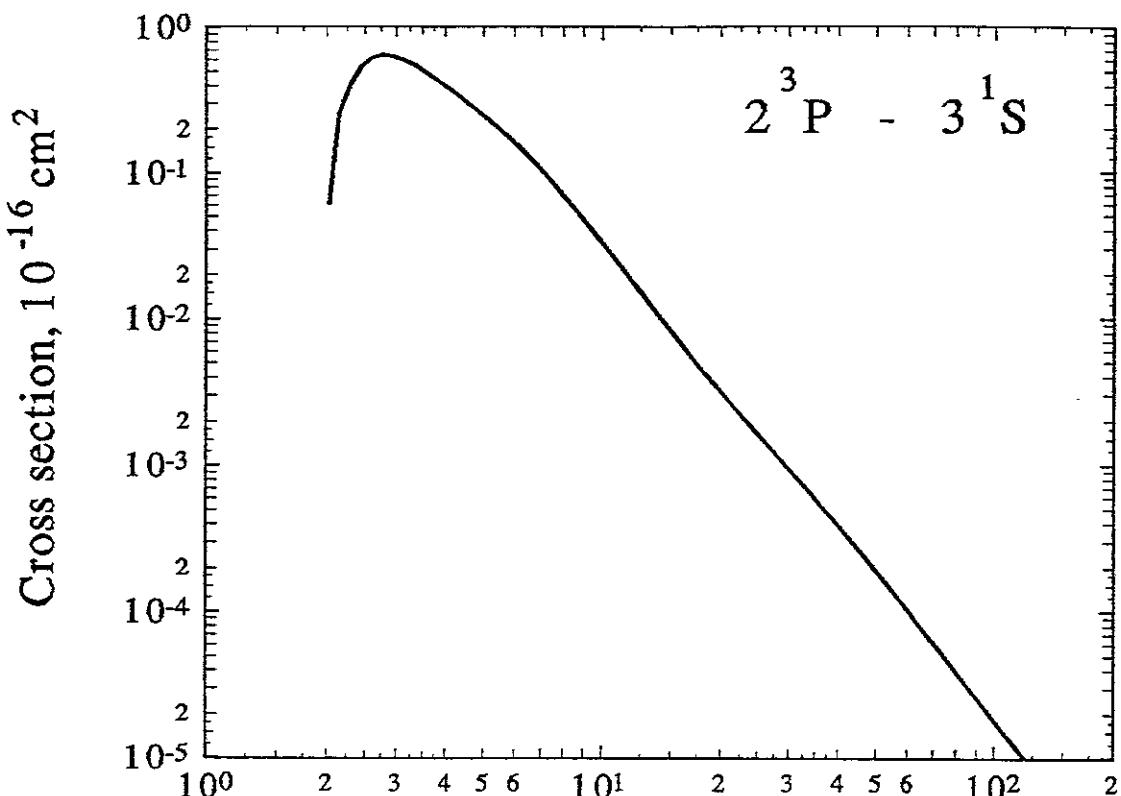


Fig.91 Electron energy, eV

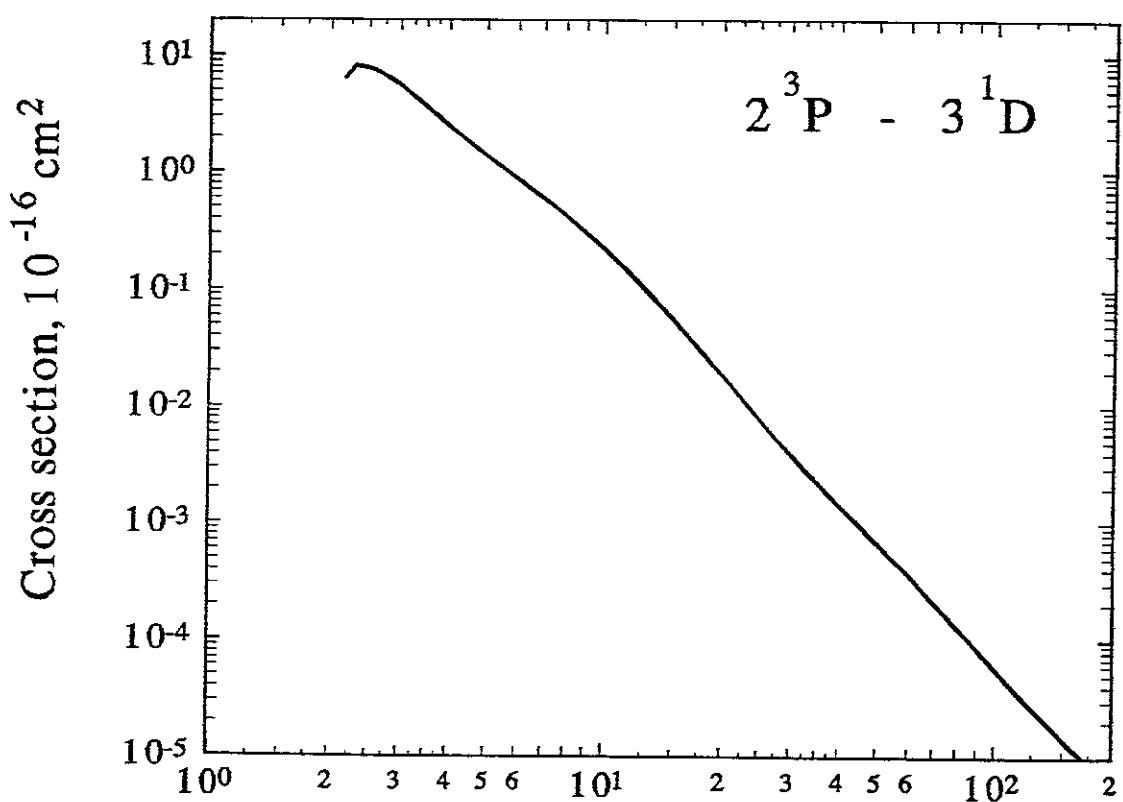


Fig.92 Electron energy, eV

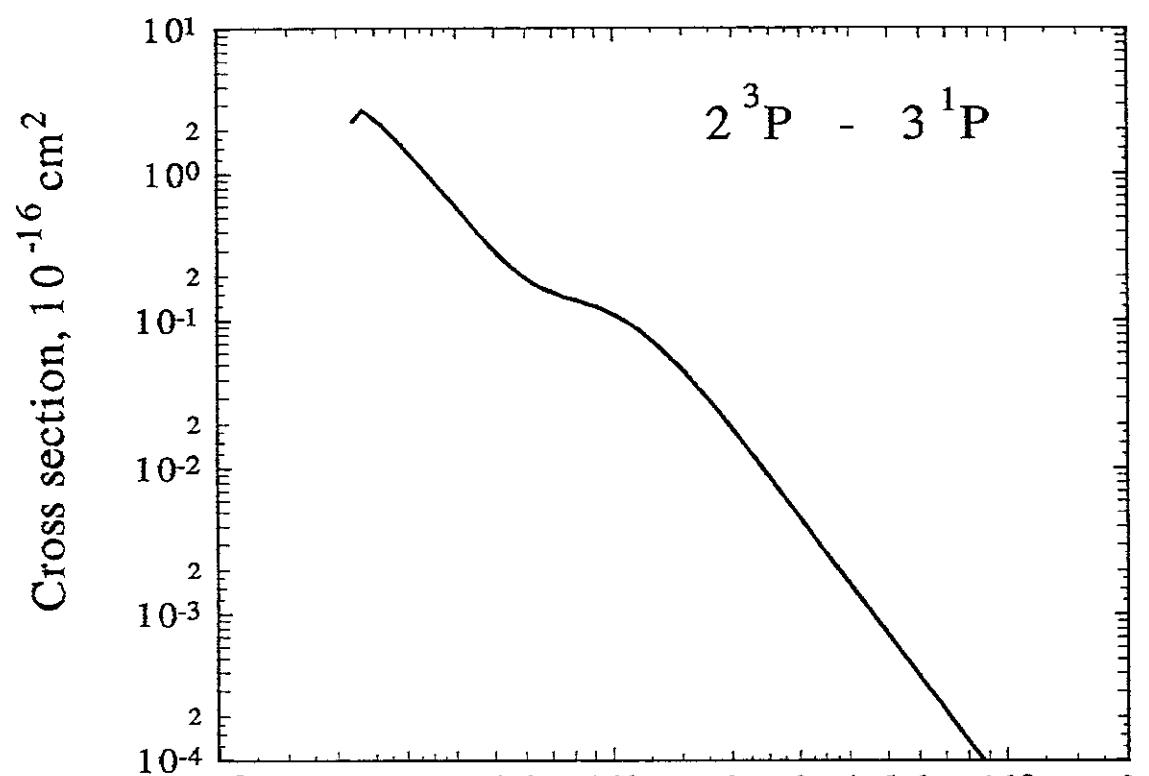


Fig.93 Electron energy, eV

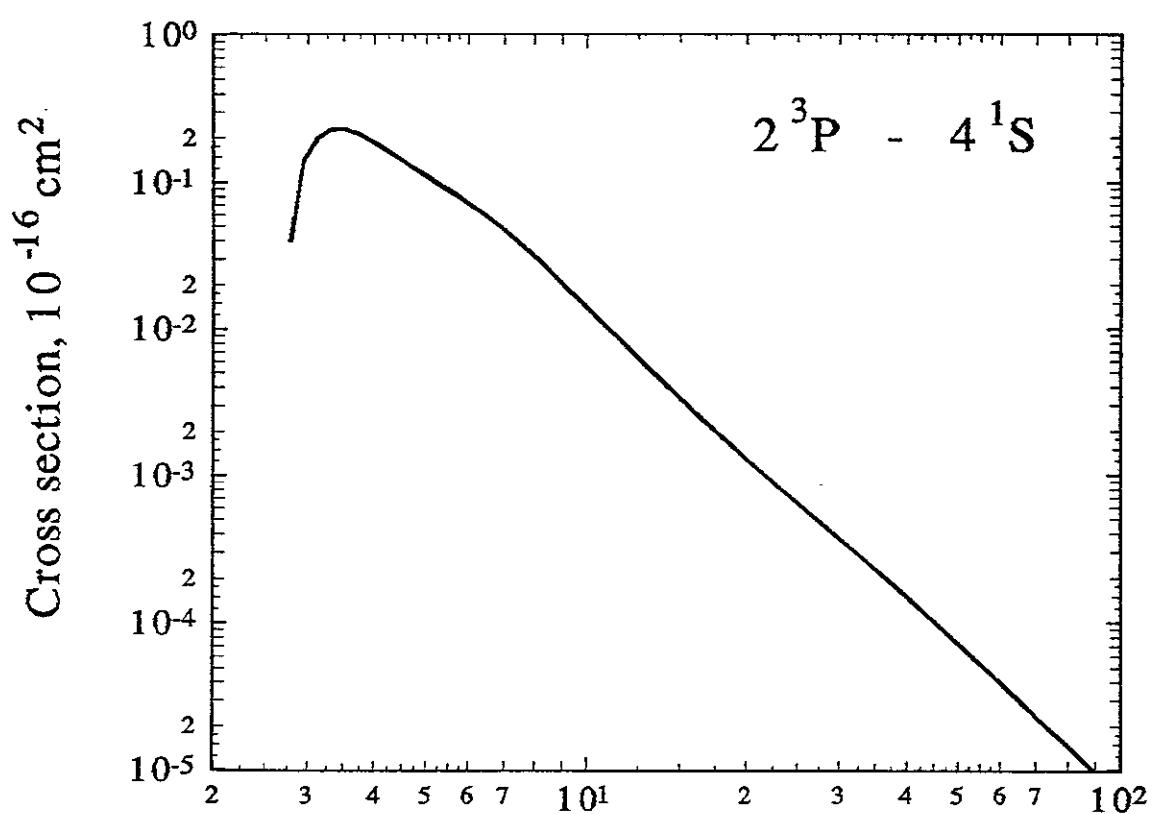


Fig.94 Electron energy, eV

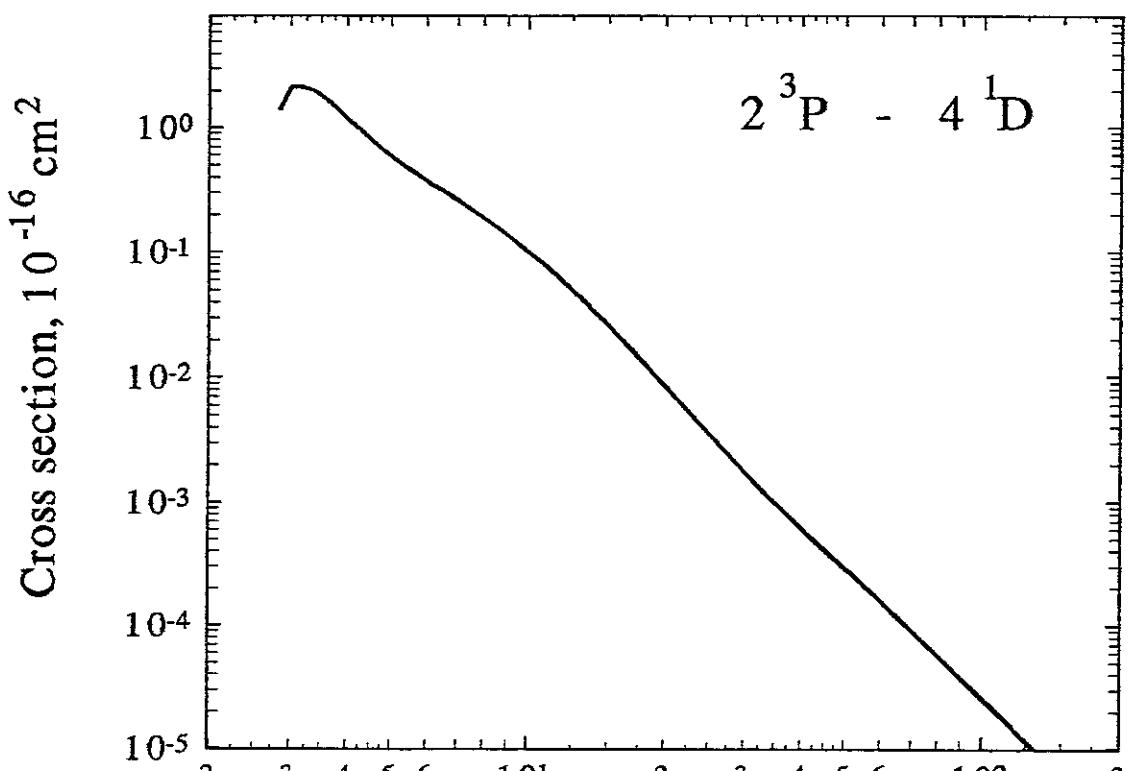


Fig.95 Electron energy, eV

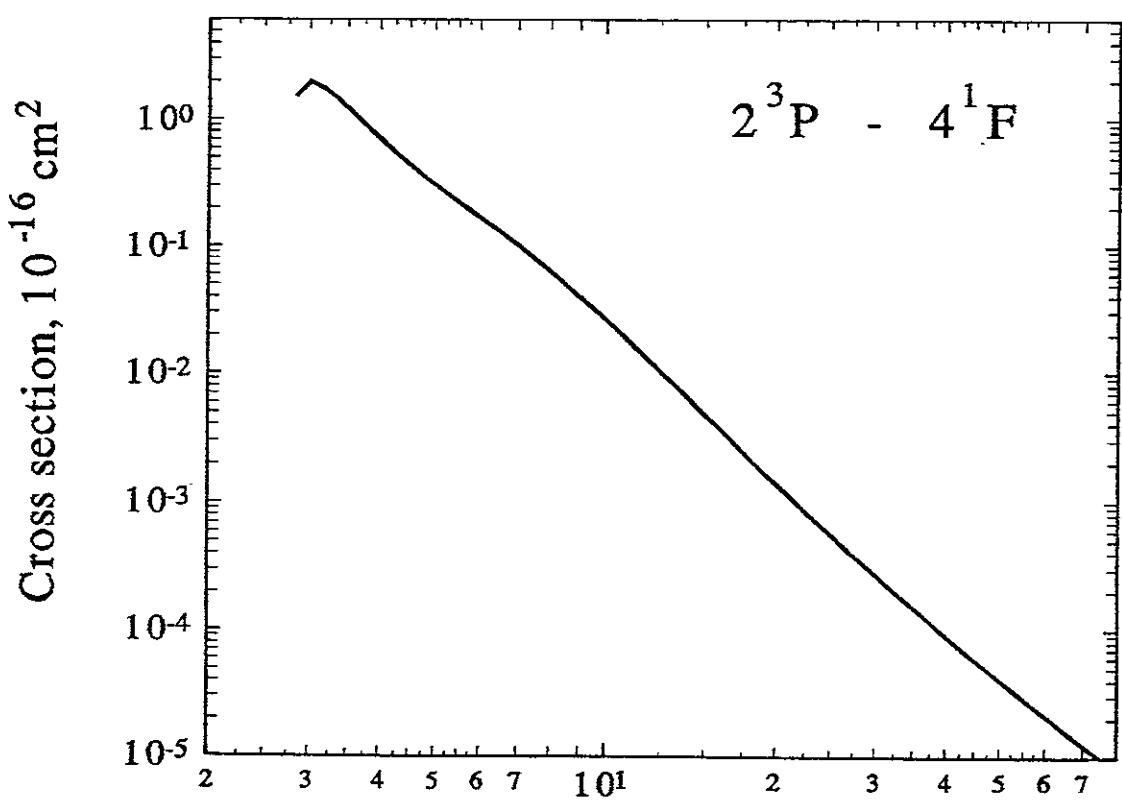


Fig.96 Electron energy, eV

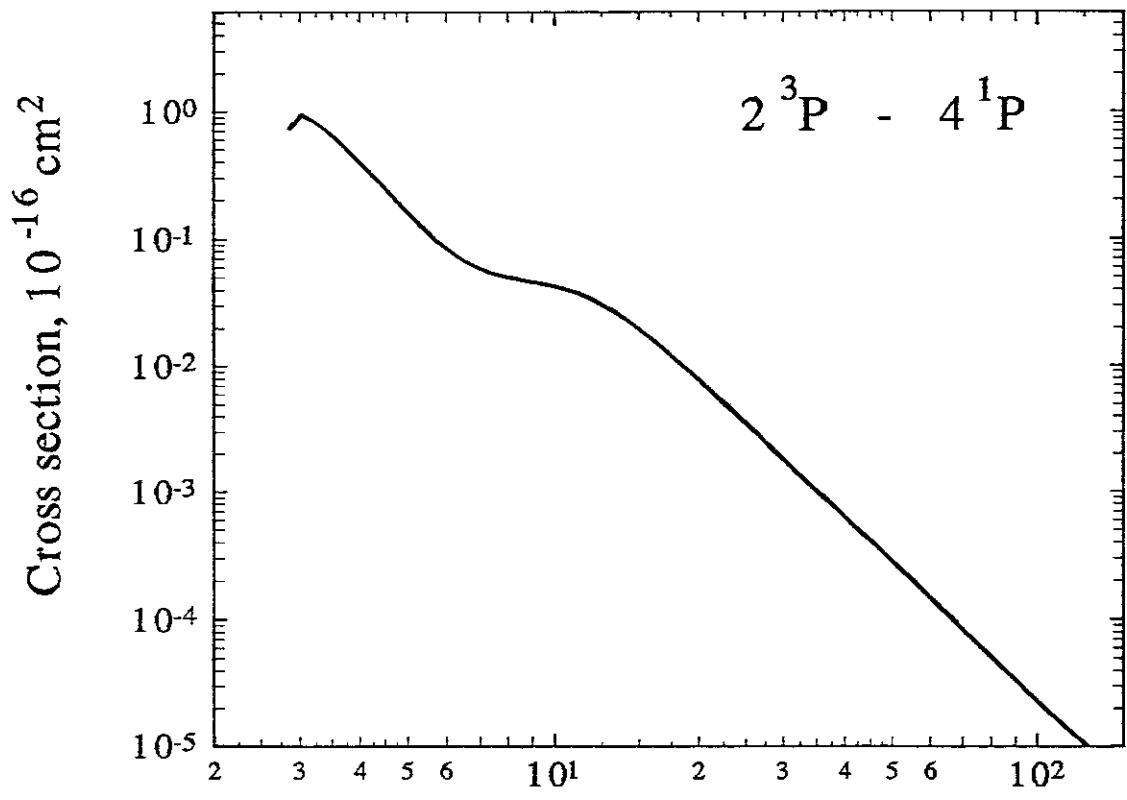


Fig.97 Electron energy, eV

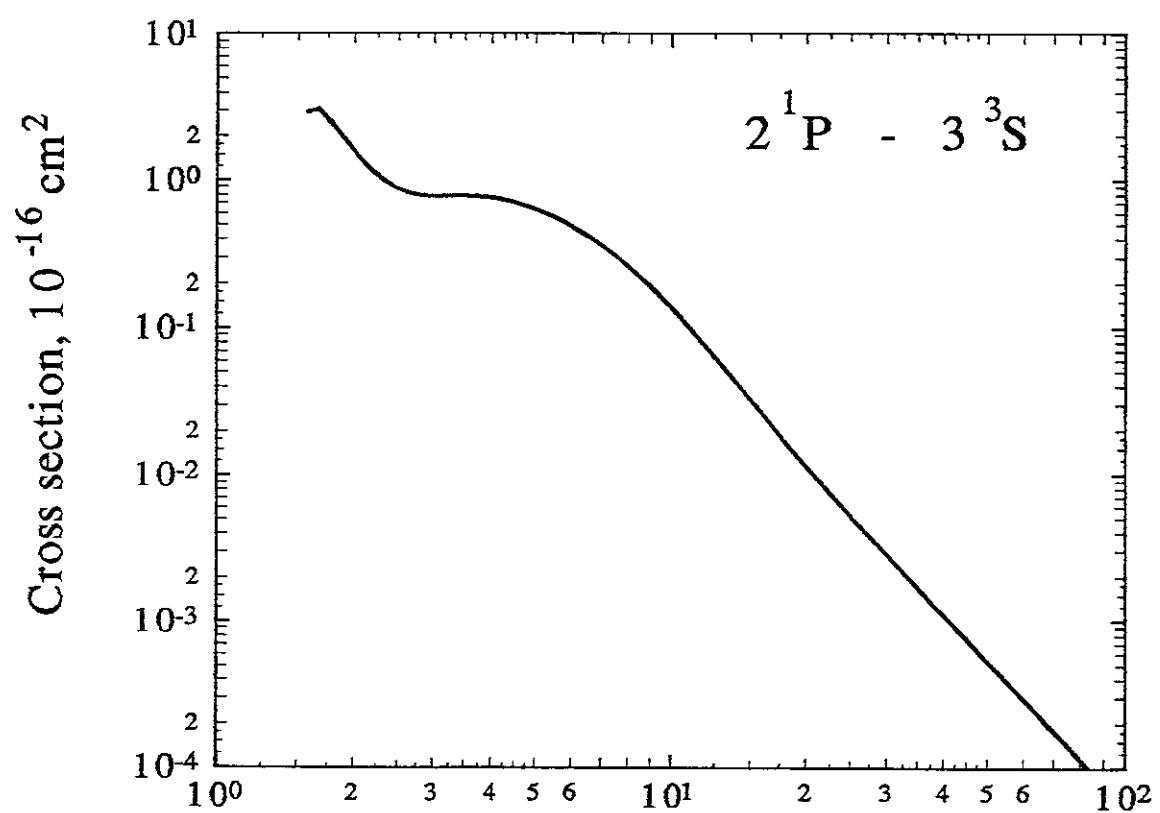


Fig.98 Electron energy, eV

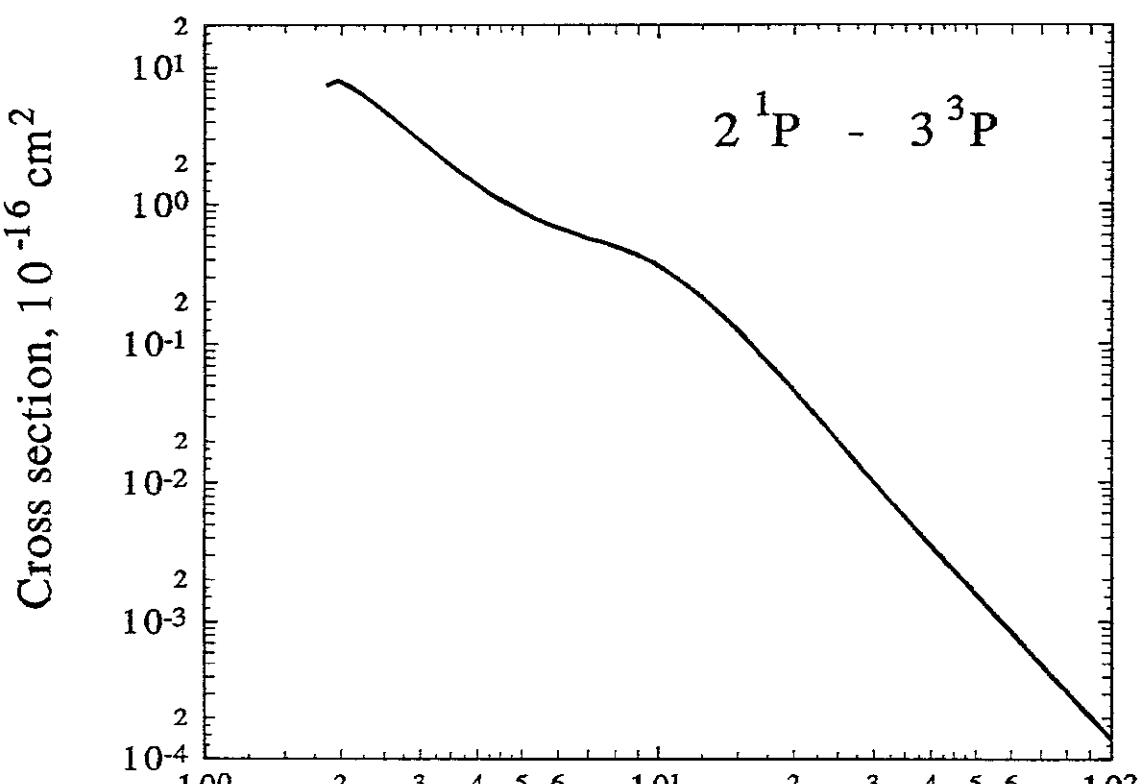


Fig.99 Electron energy, eV

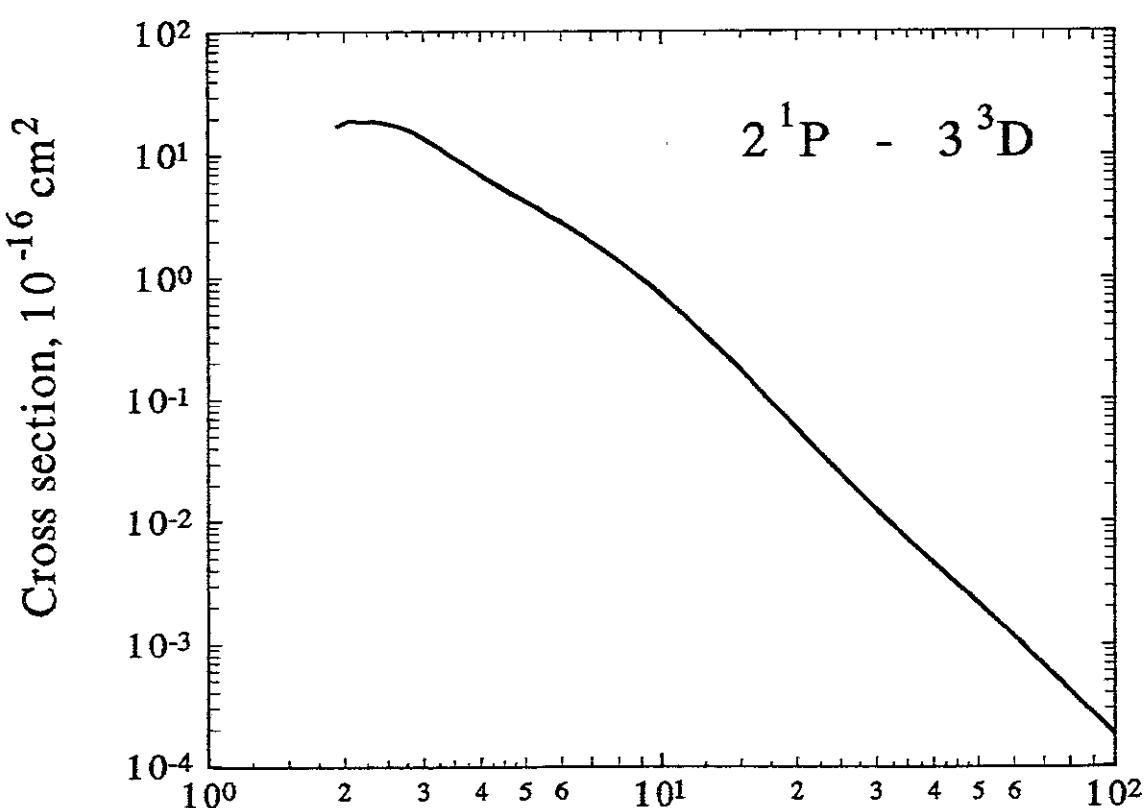


Fig.100 Electron energy, eV

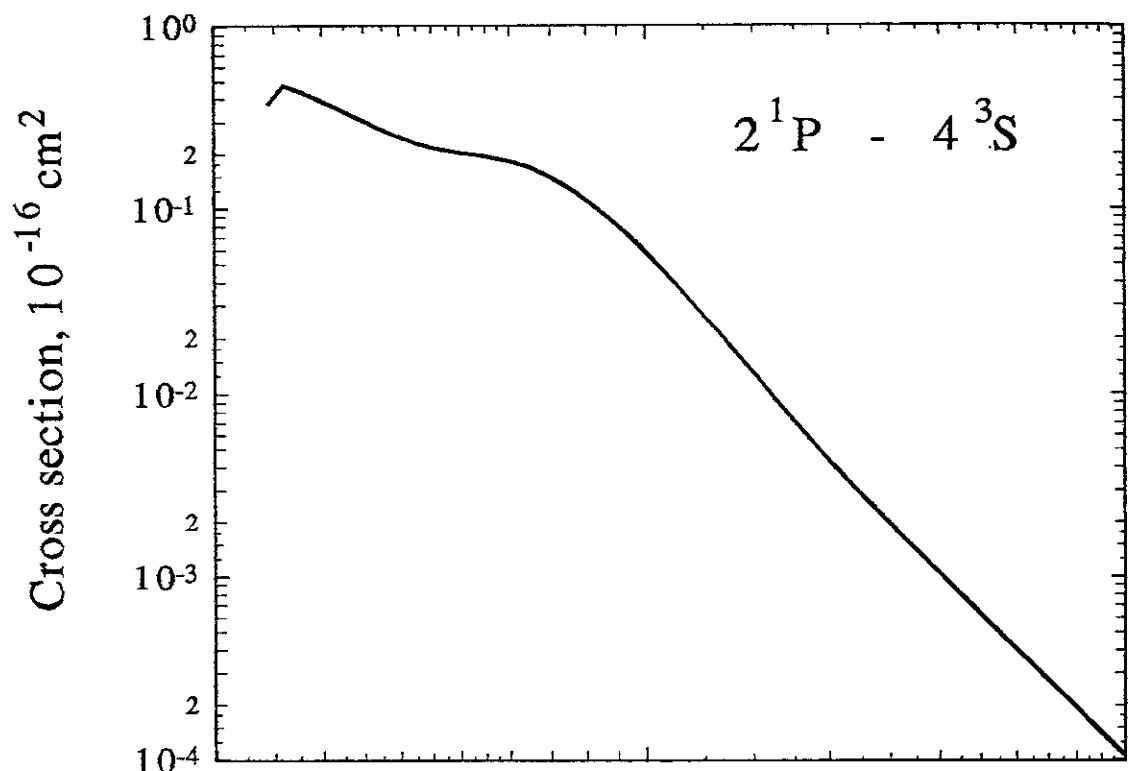


Fig.101 Electron energy, eV

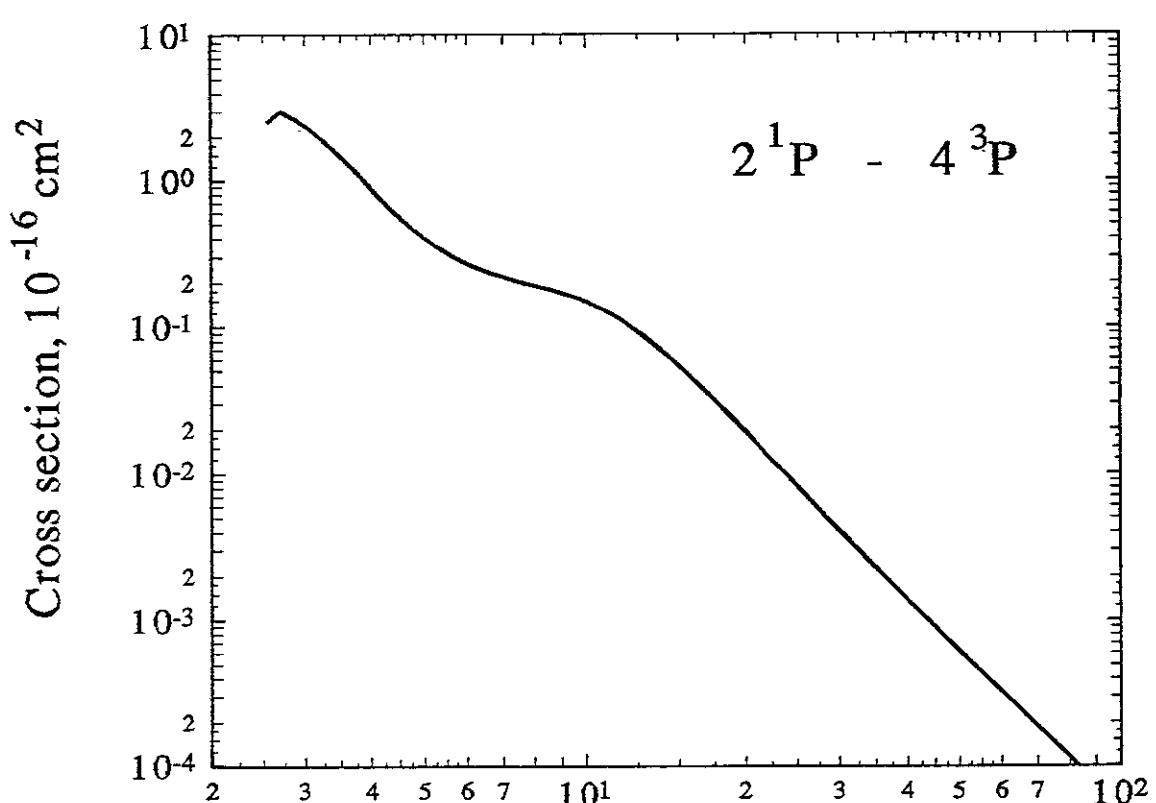


Fig.102 Electron energy, eV

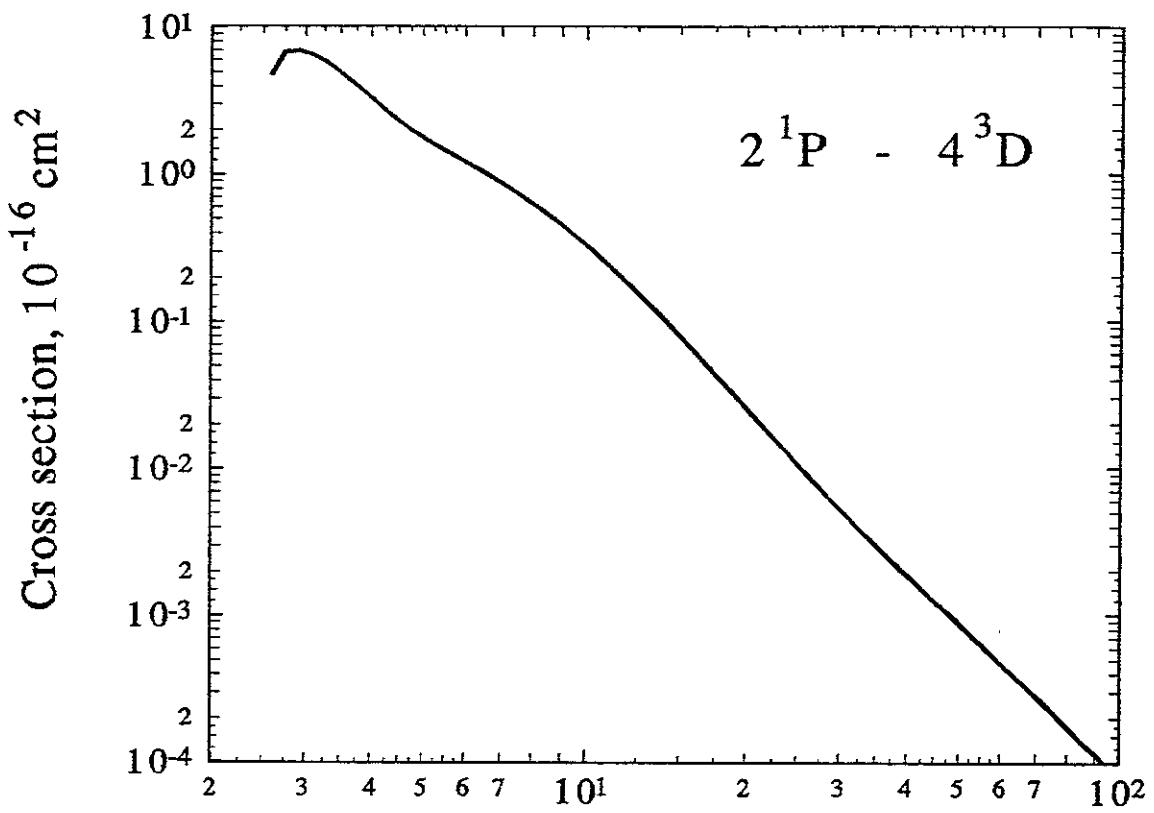


Fig.103 Electron energy, eV

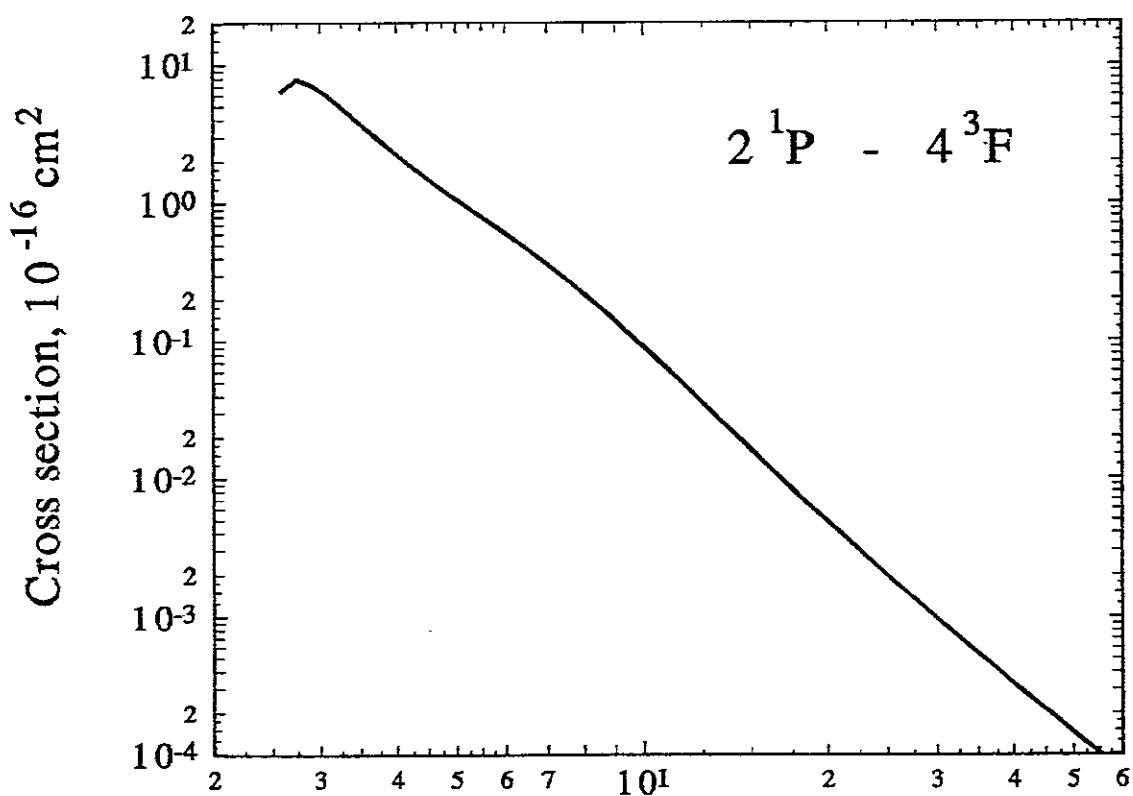


Fig.104 Electron energy, eV

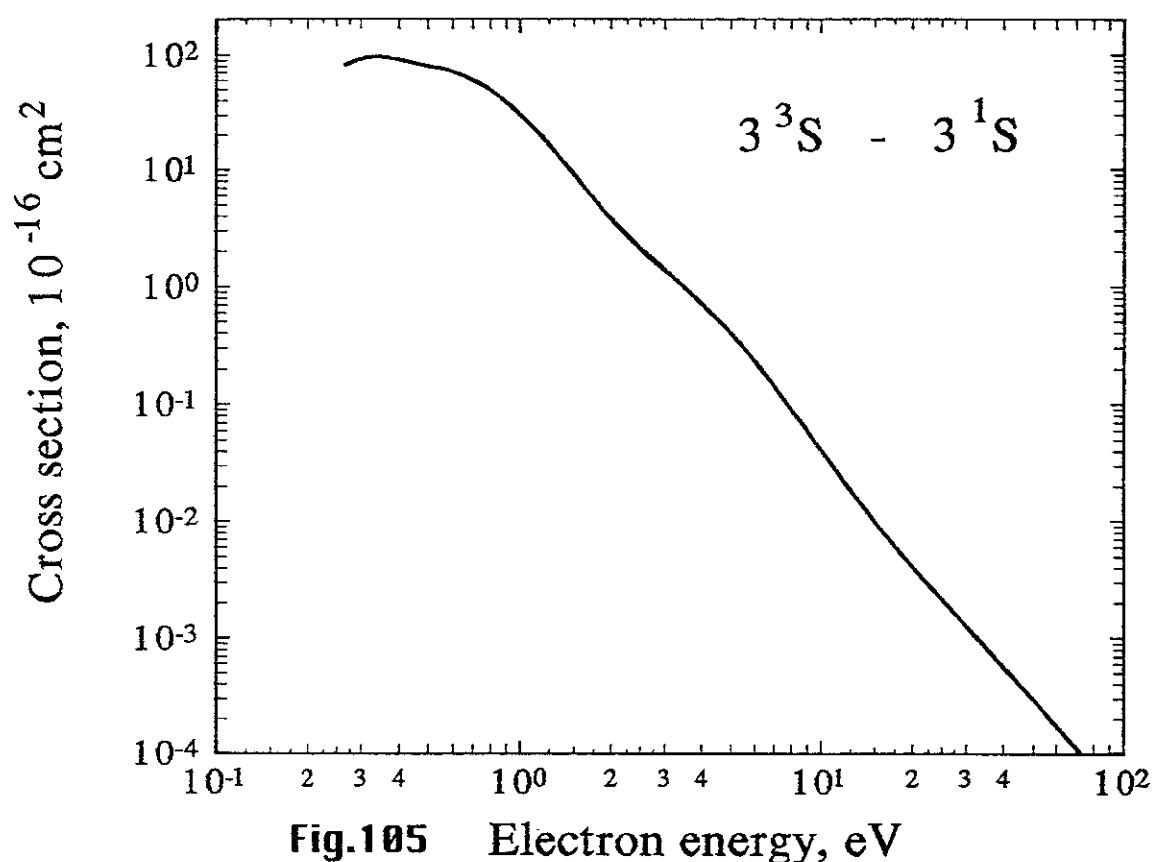


Fig.105 Electron energy, eV

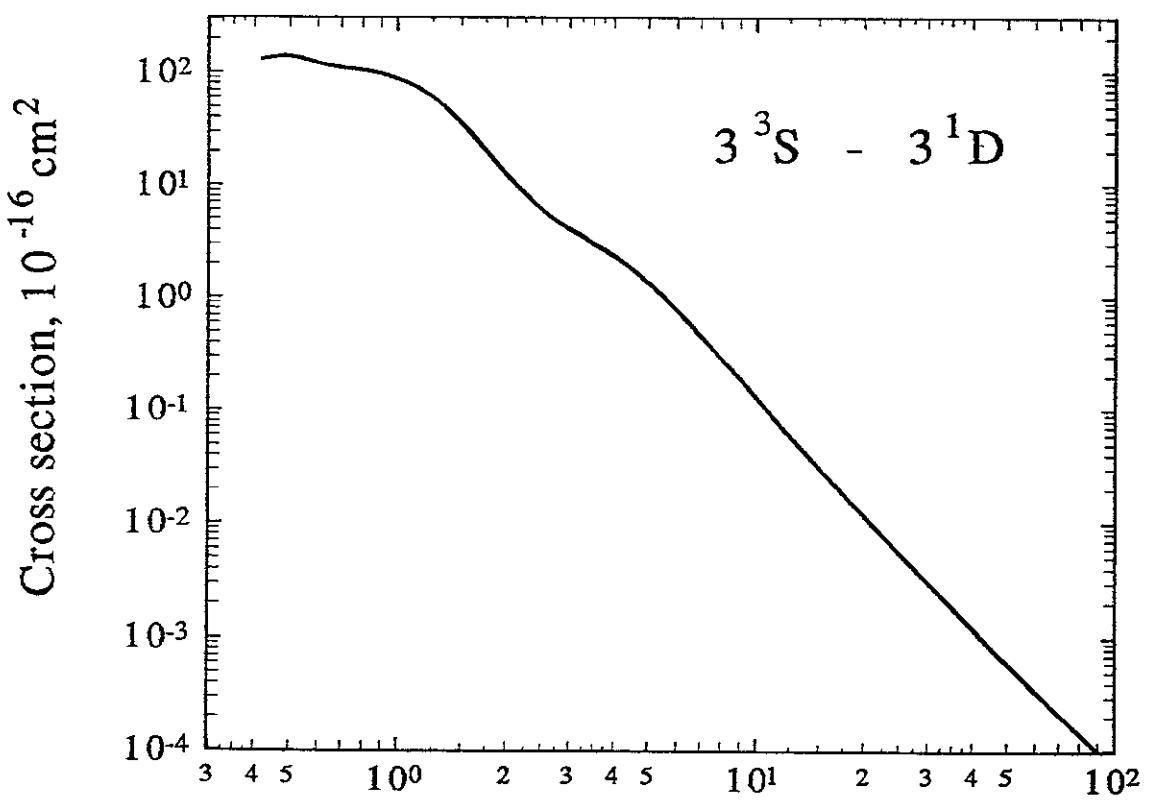


Fig.106 Electron energy, eV

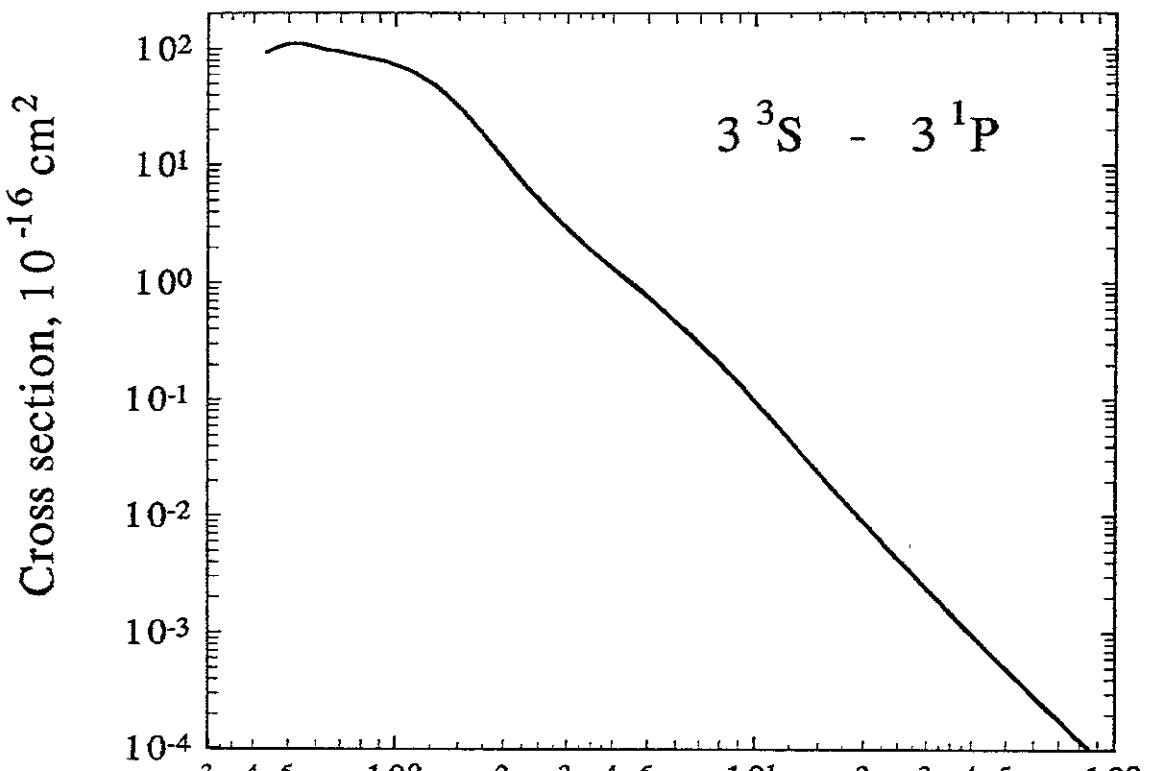


Fig.107 Electron energy, eV

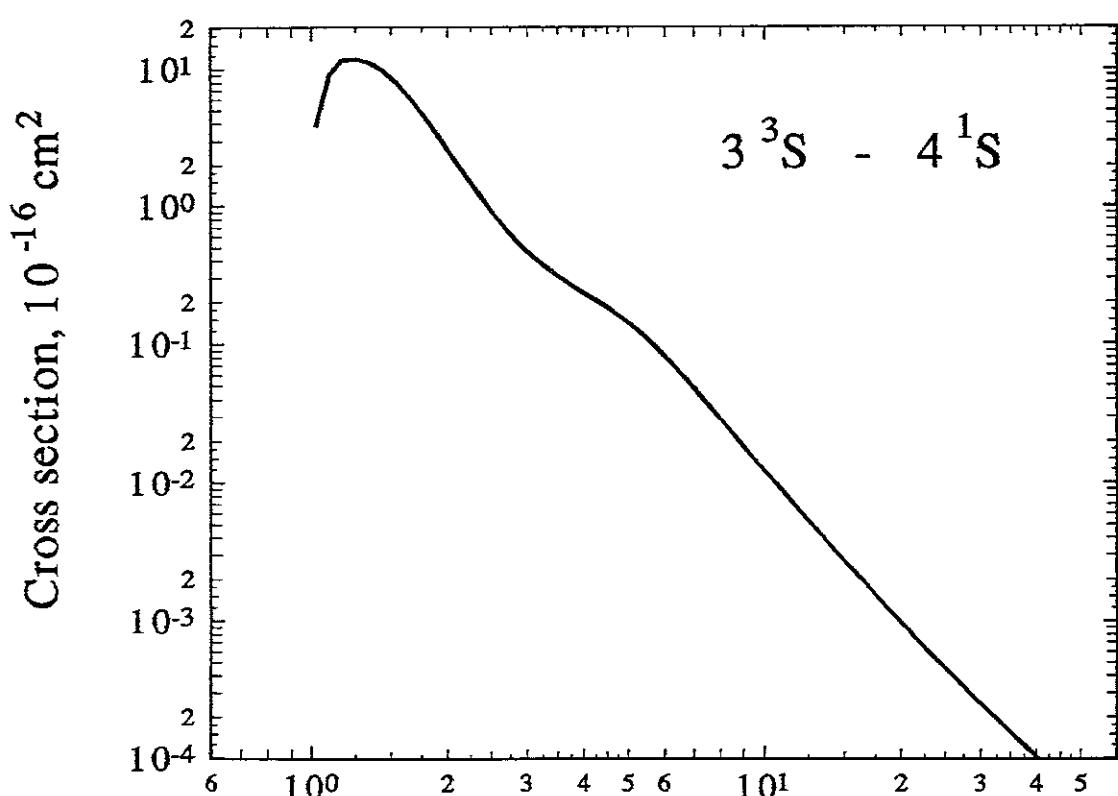


Fig.108 Electron energy, eV

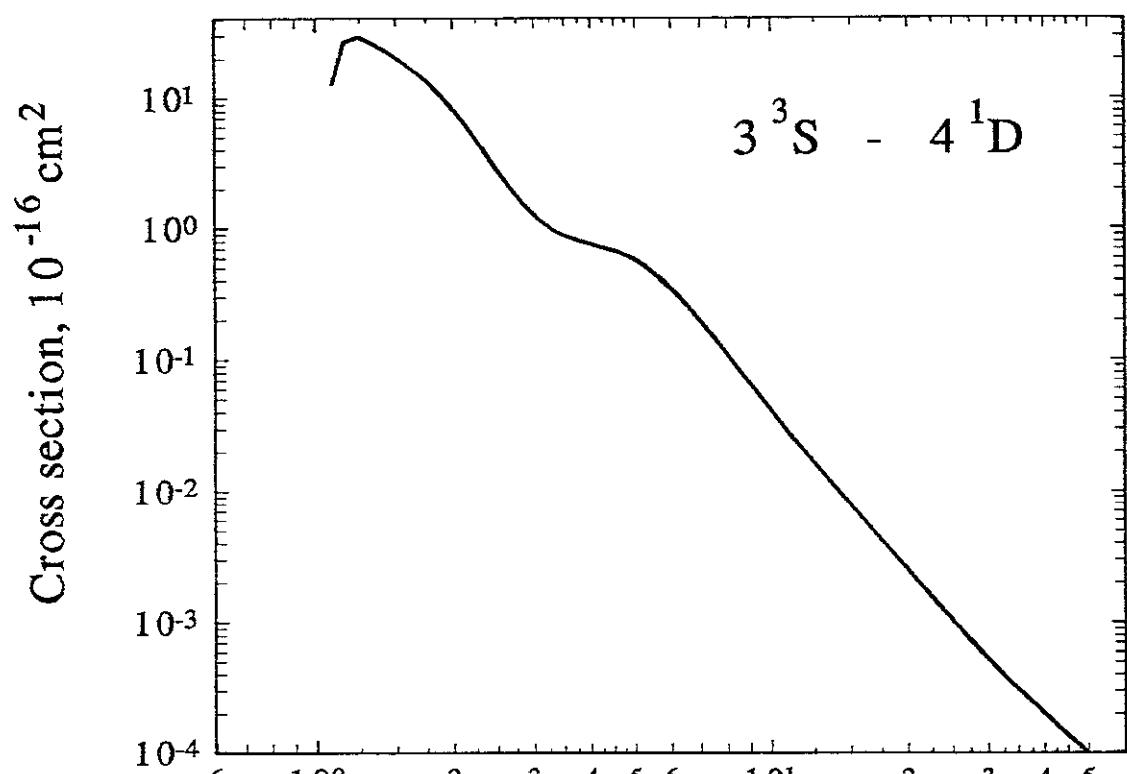


Fig.109 Electron energy, eV

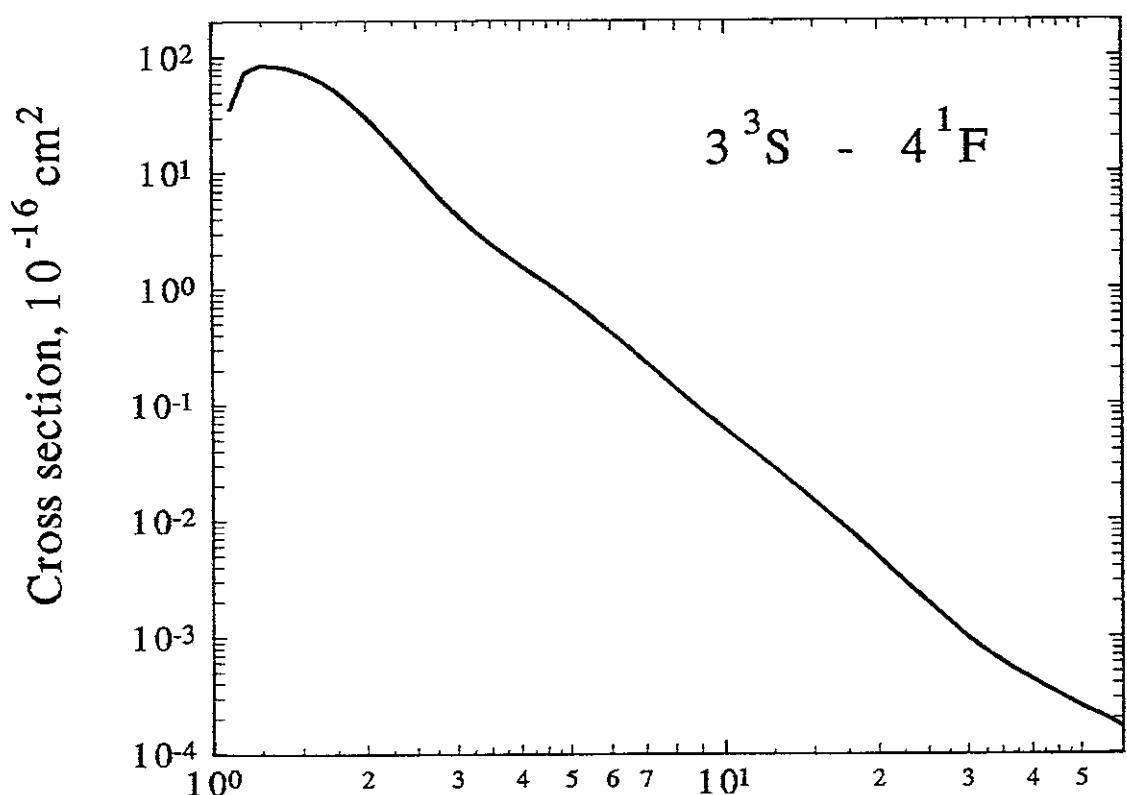


Fig.110 Electron energy, eV

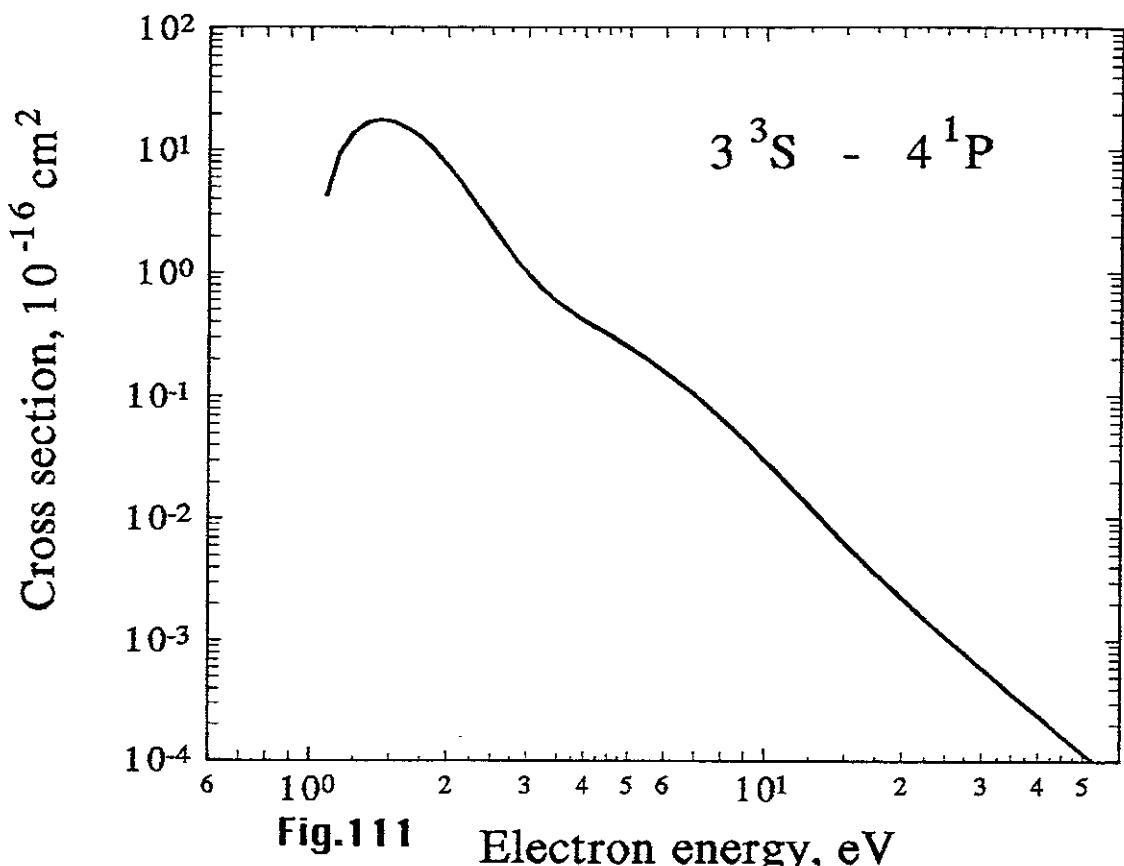


Fig.111 Electron energy, eV

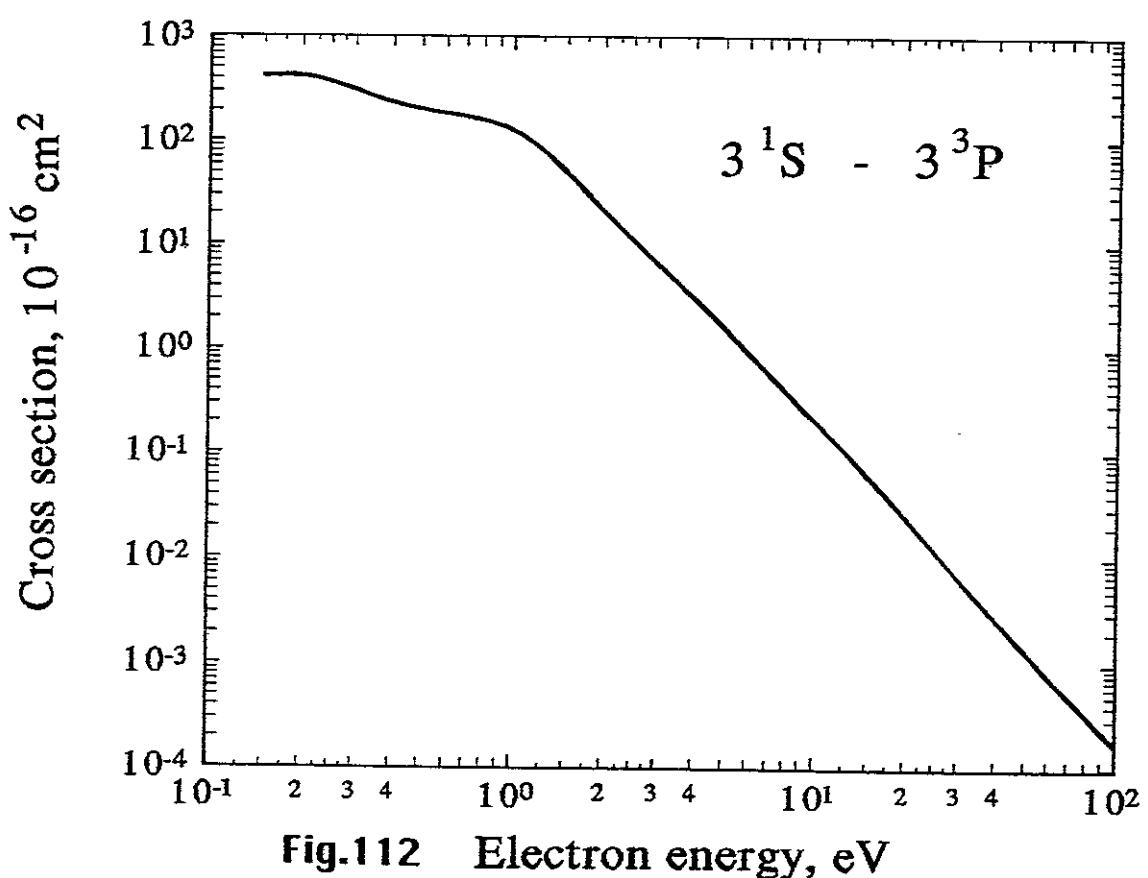


Fig.112 Electron energy, eV

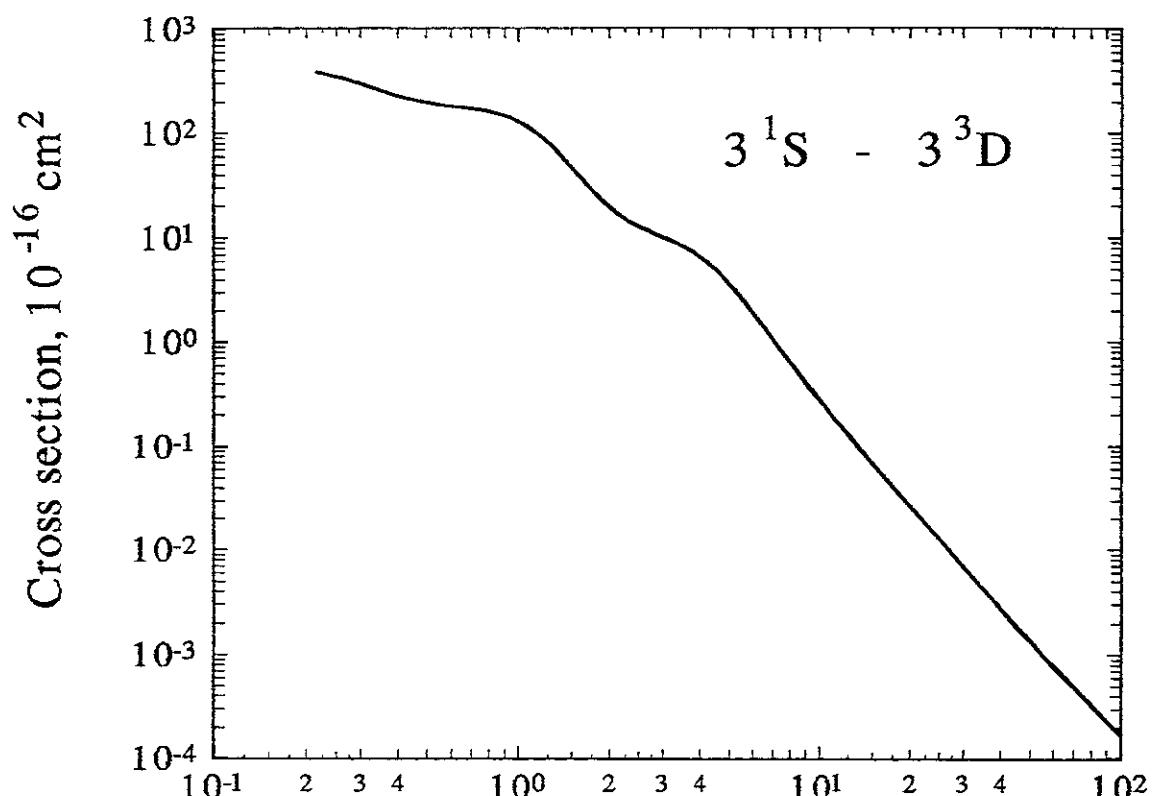


Fig.113 Electron energy, eV

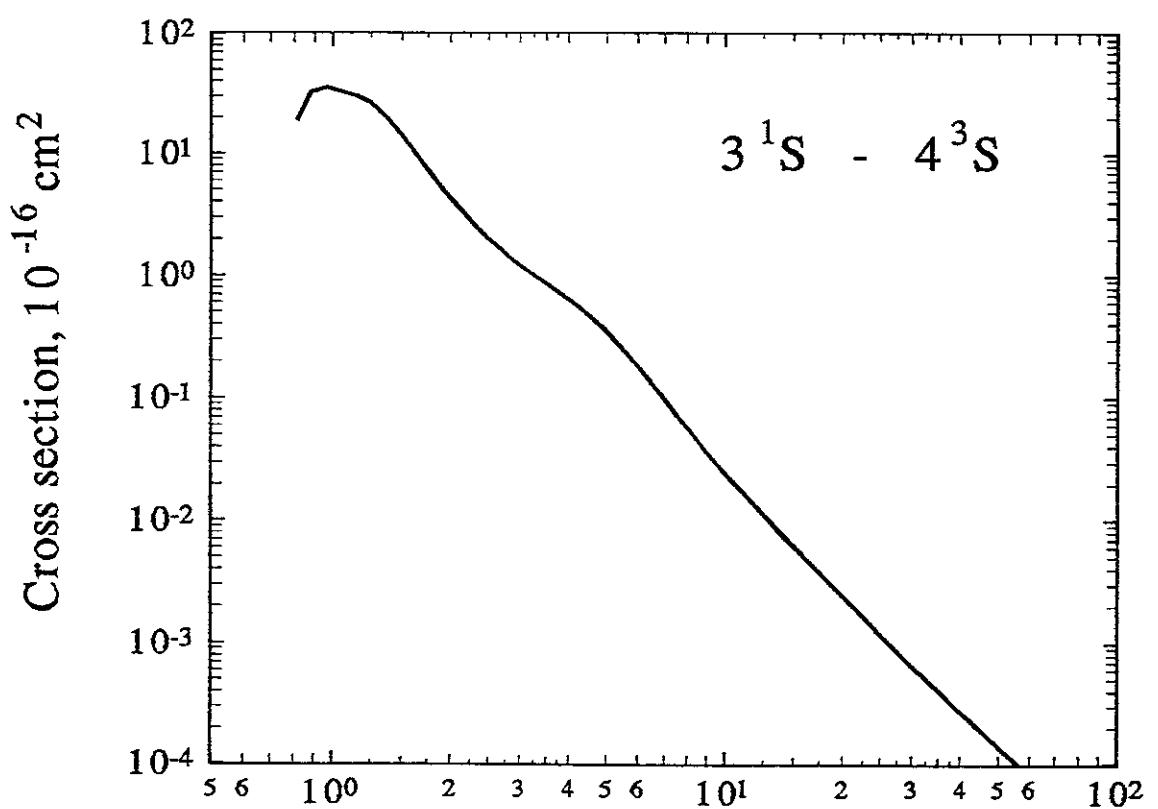


Fig.114 Electron energy, eV

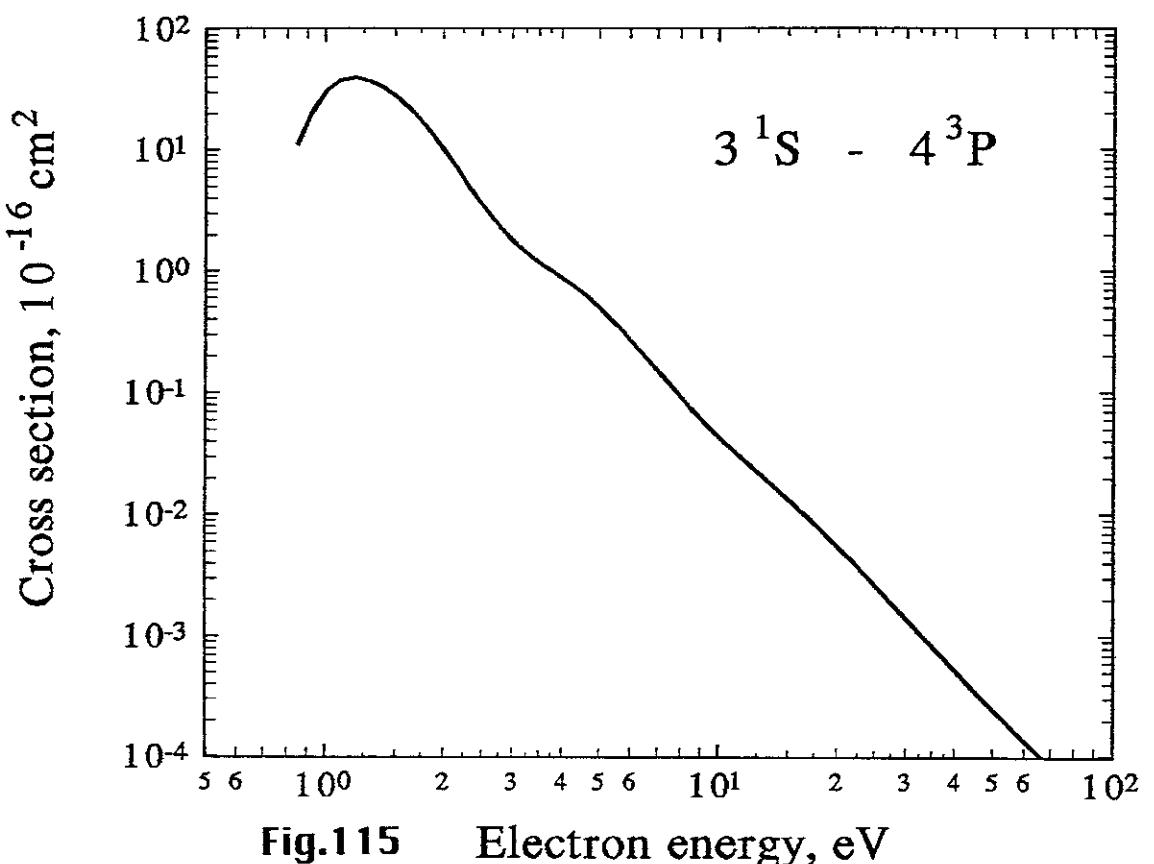


Fig.115 Electron energy, eV

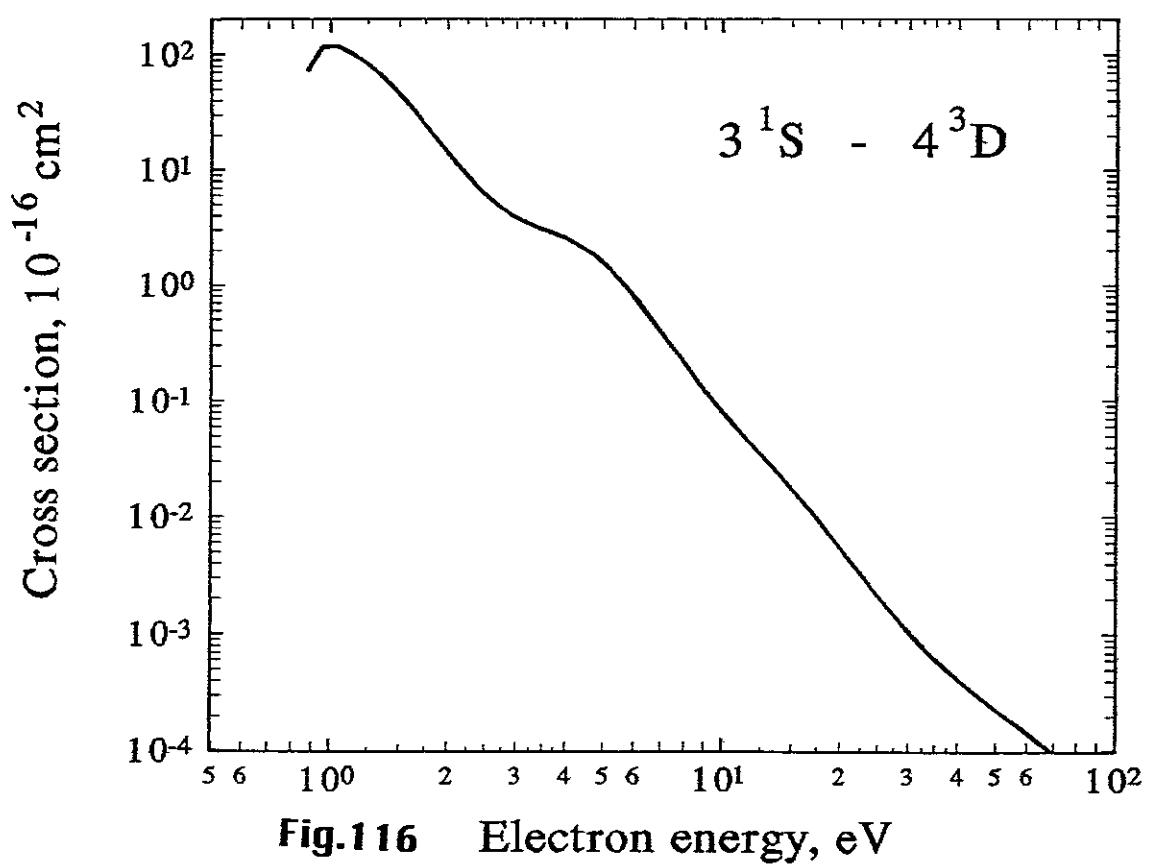


Fig.116 Electron energy, eV

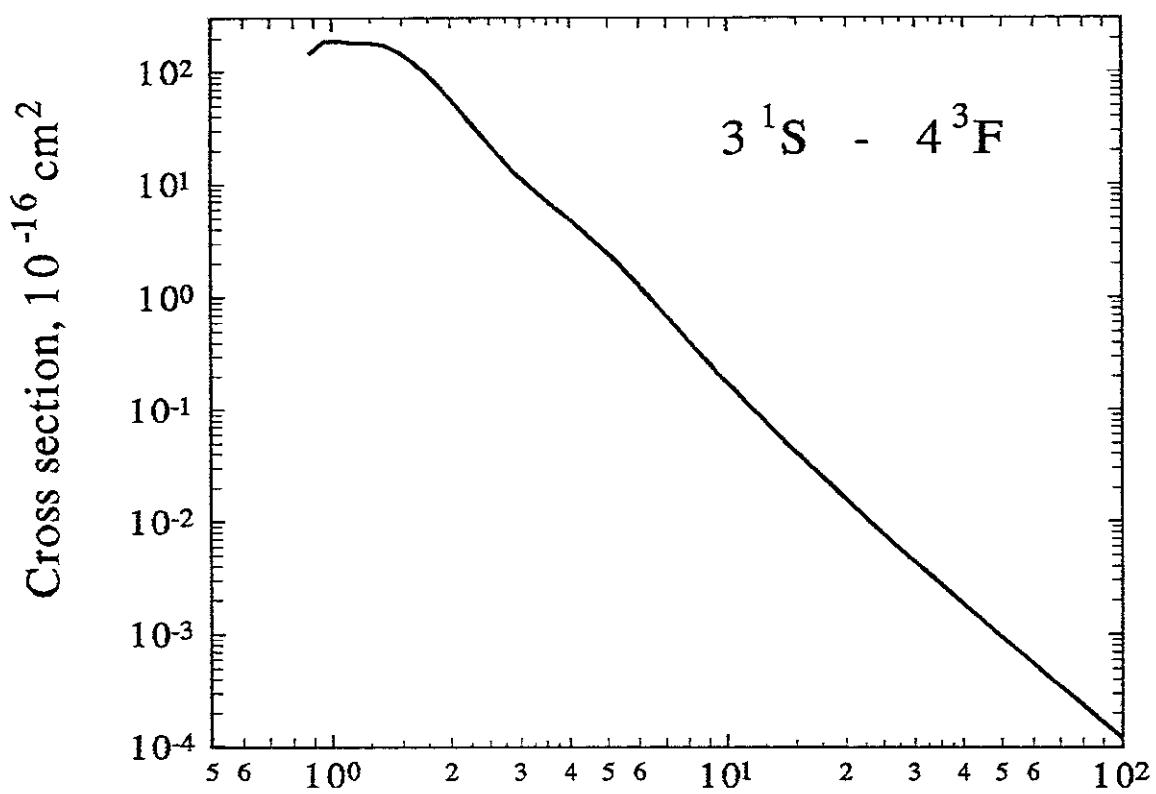


Fig.117 Electron energy, eV

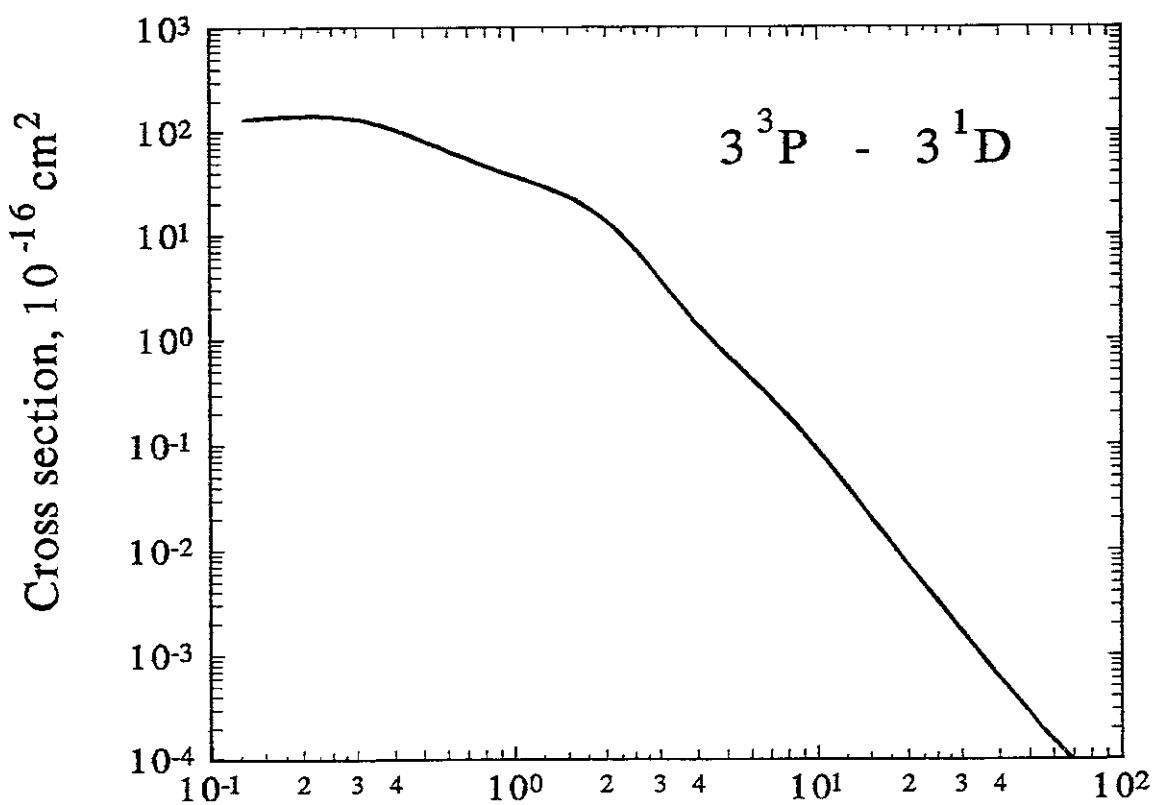


Fig.118 Electron energy, eV

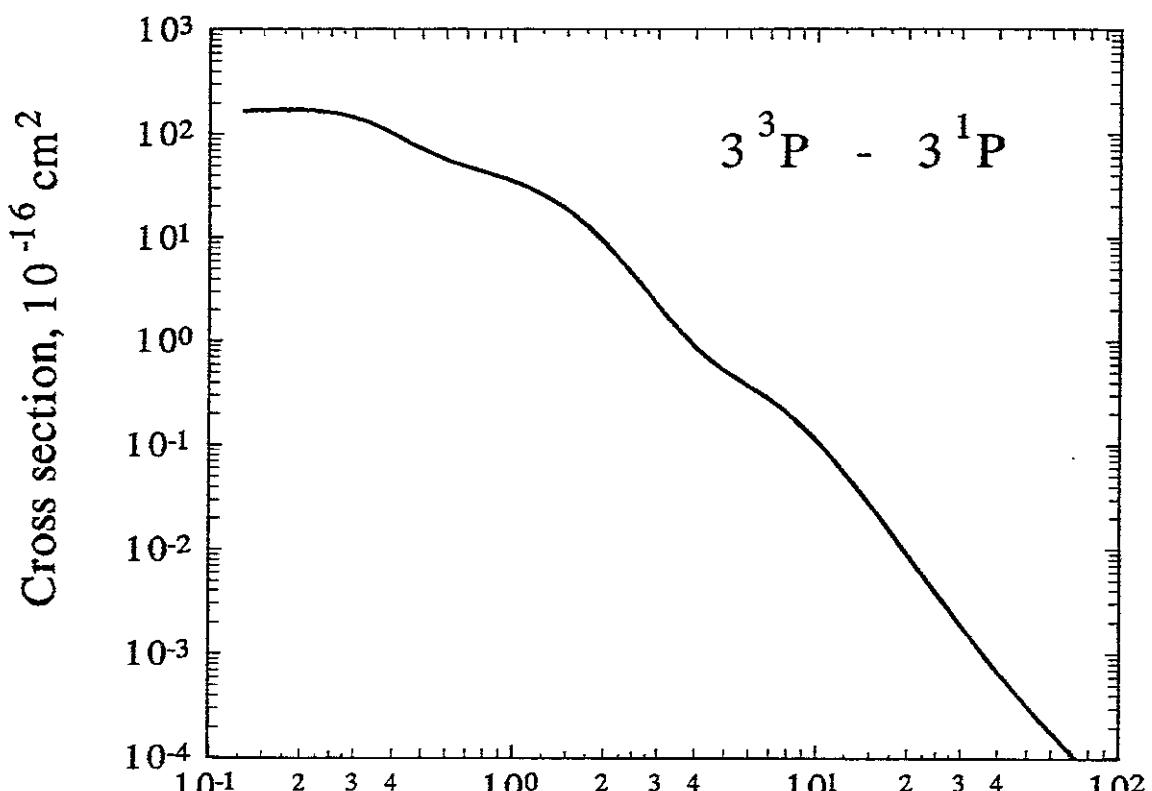


Fig.119 Electron energy, eV

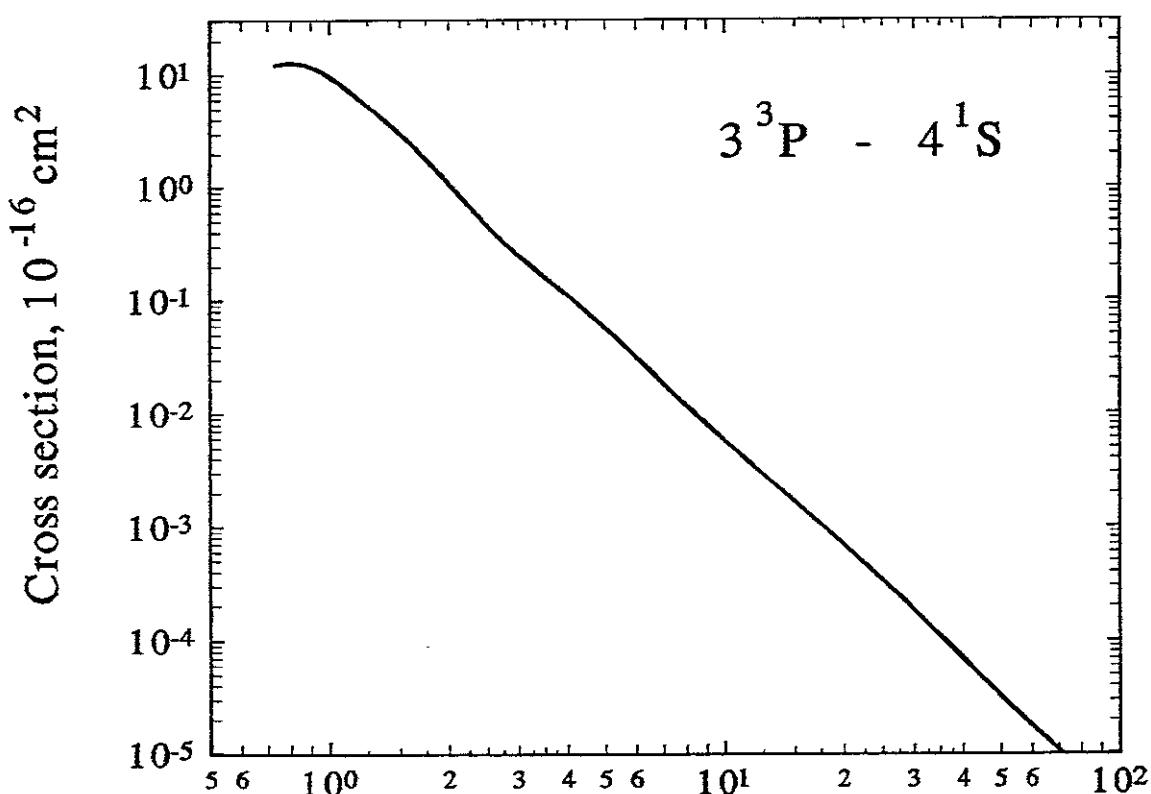


Fig.120 Electron energy, eV

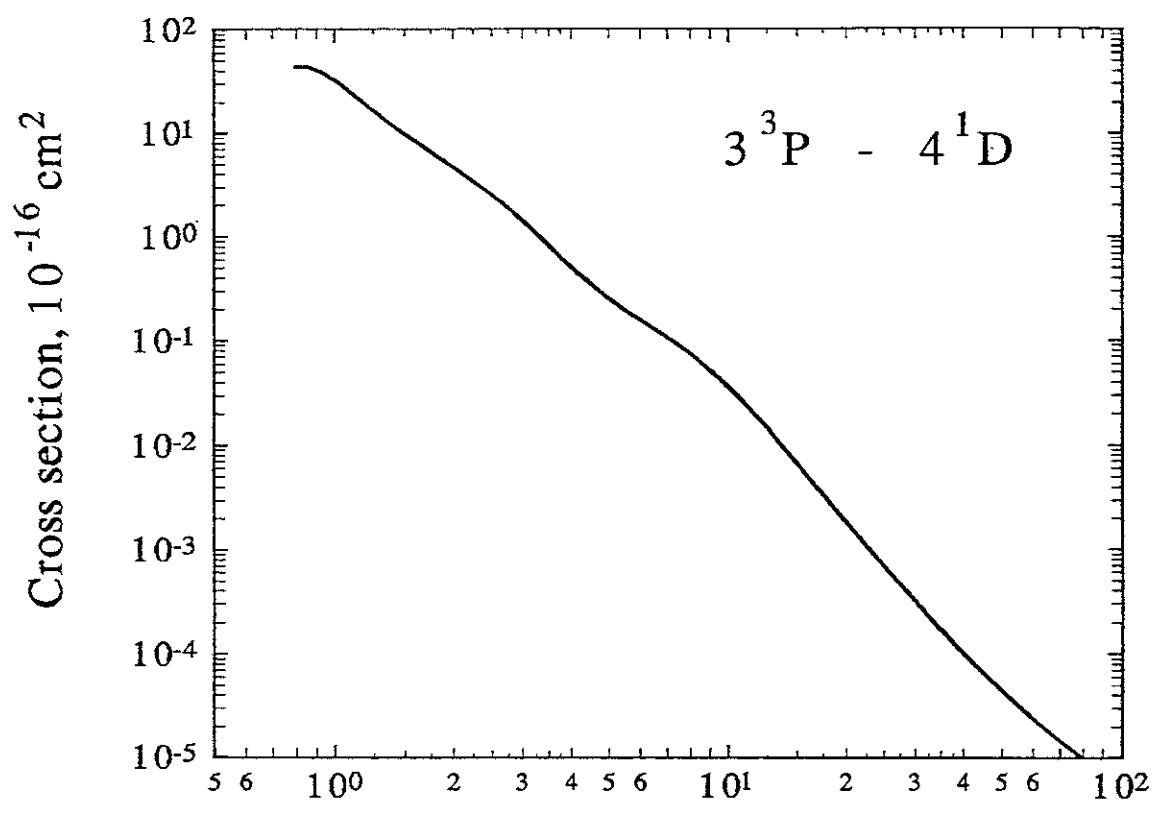


Fig.121 Electron energy, eV

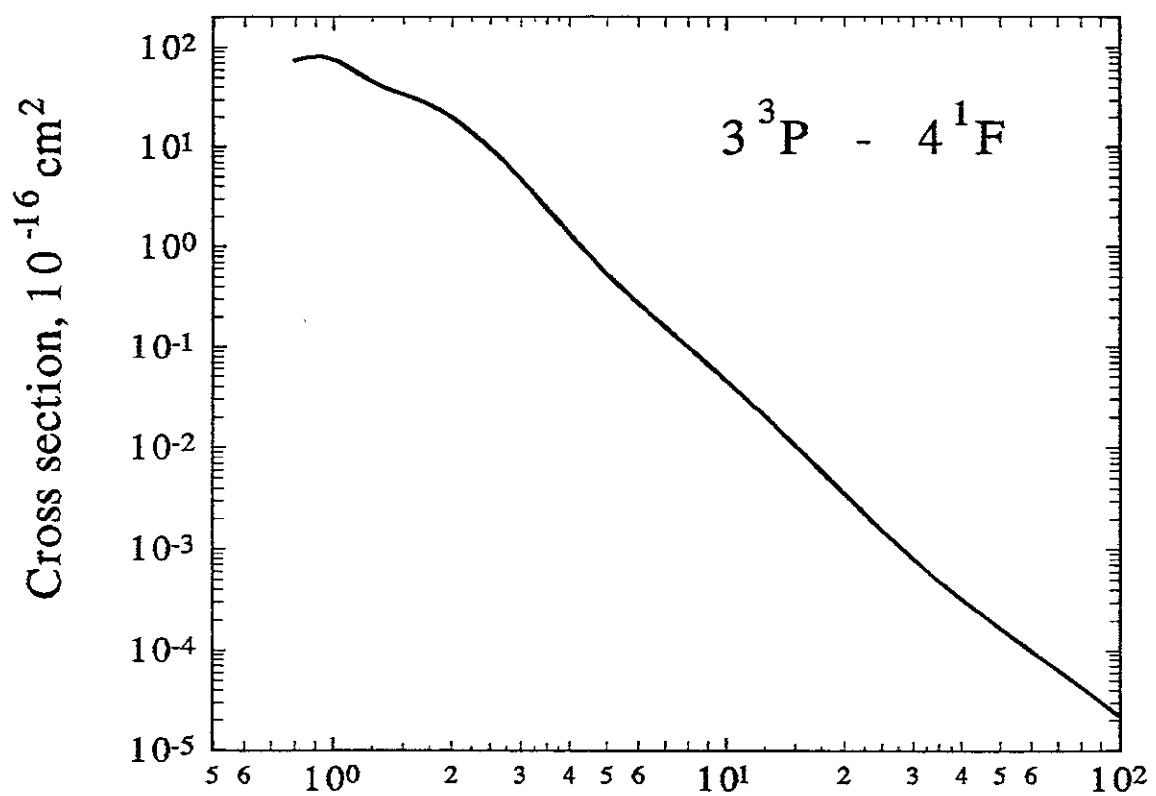


Fig.122 Electron energy, eV

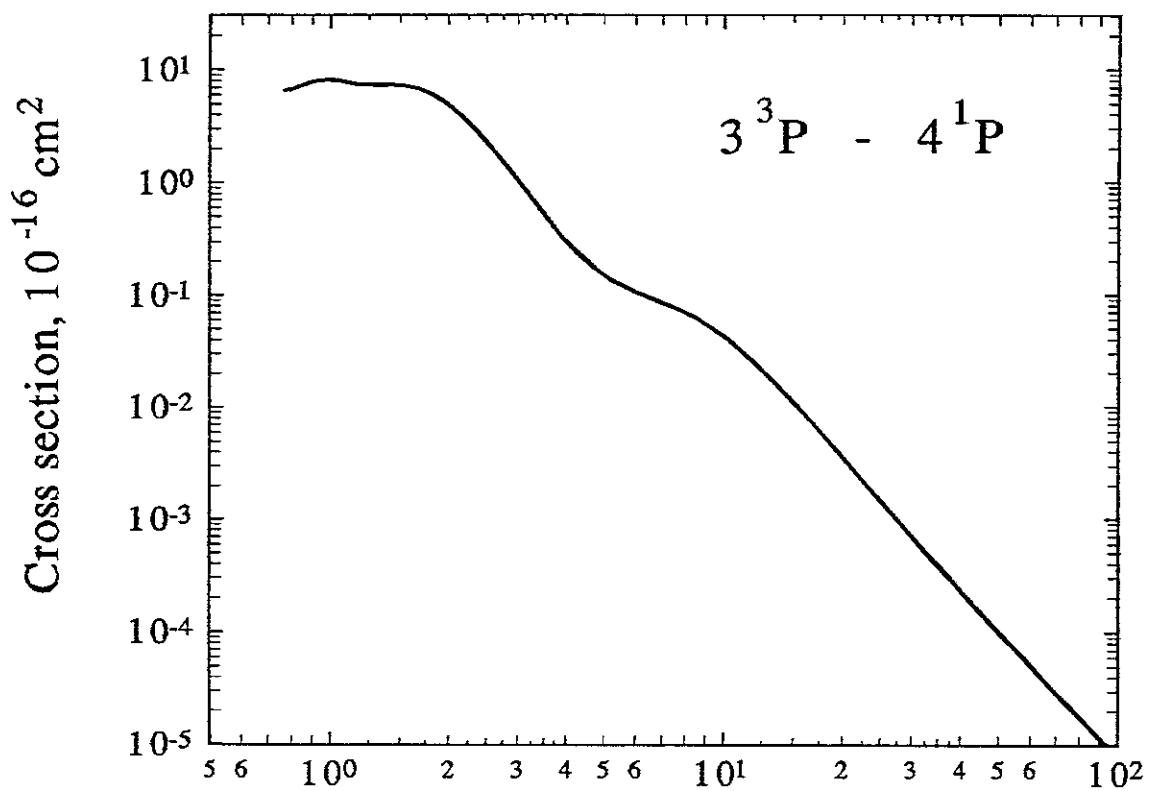


Fig.123 Electron energy, eV

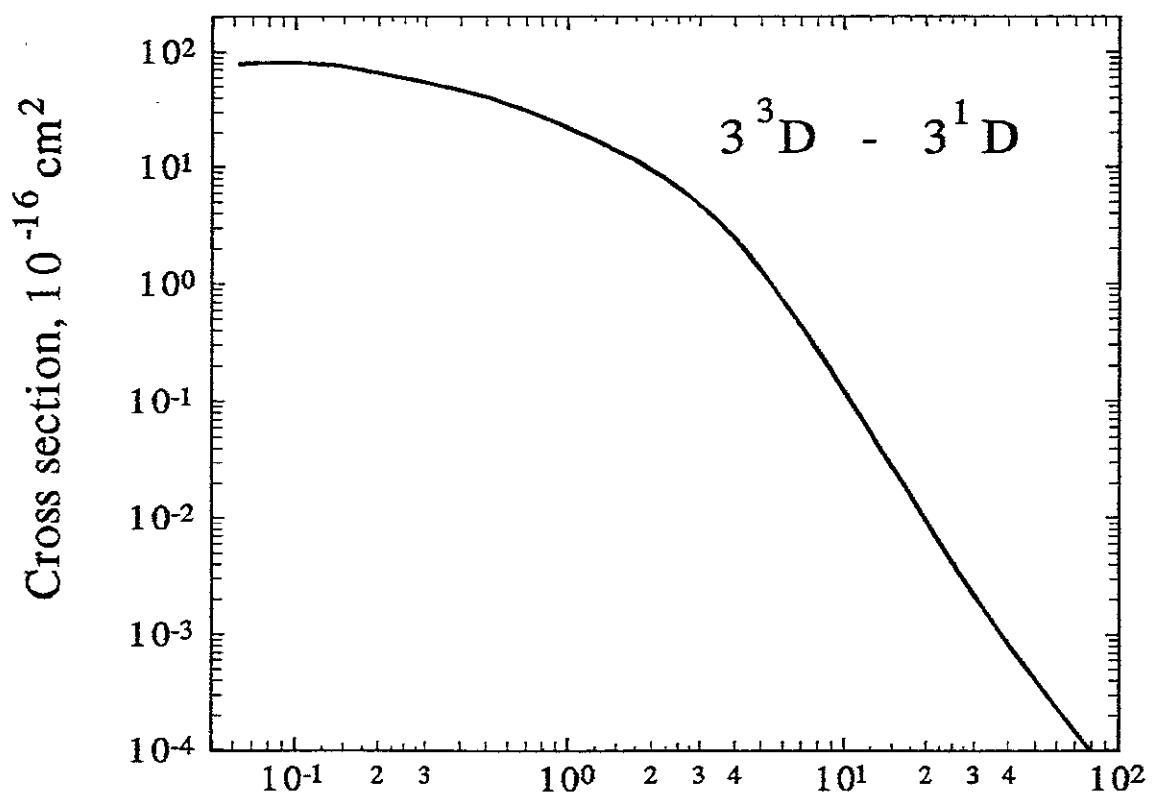
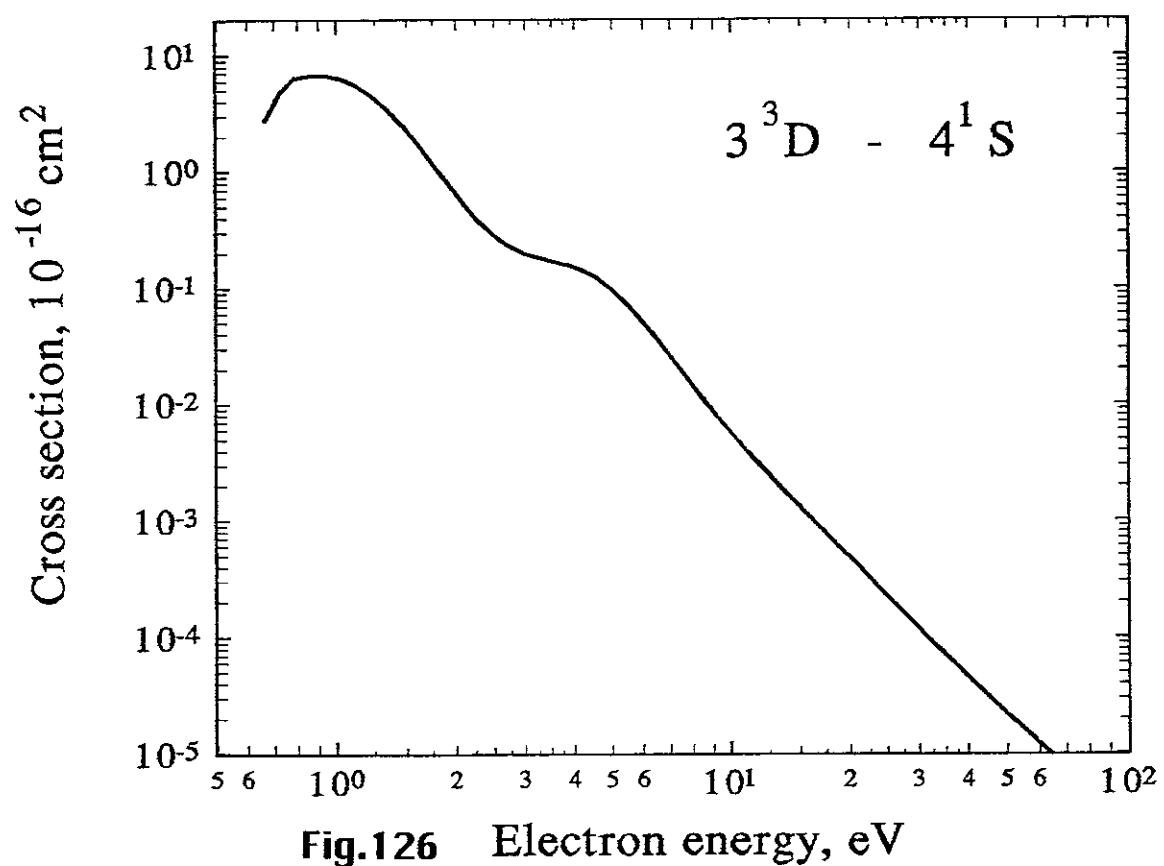
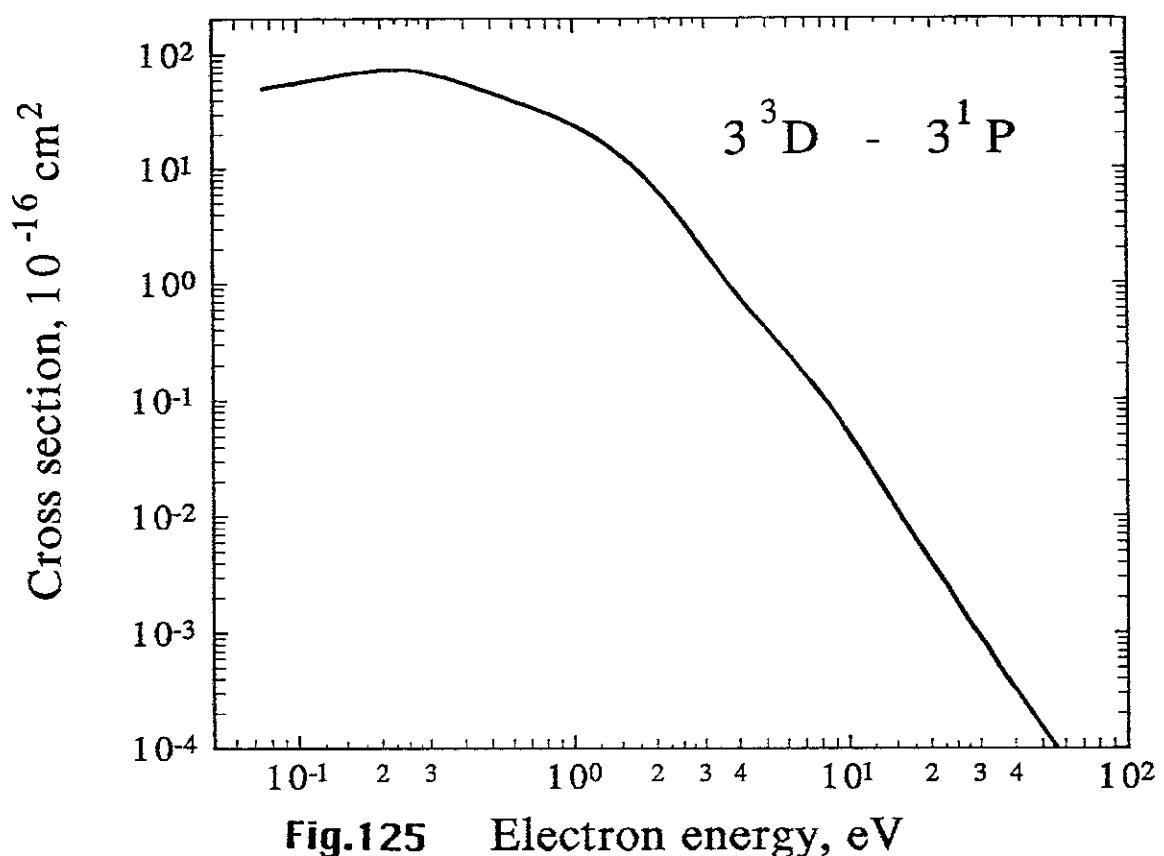


Fig.124 Electron energy, eV



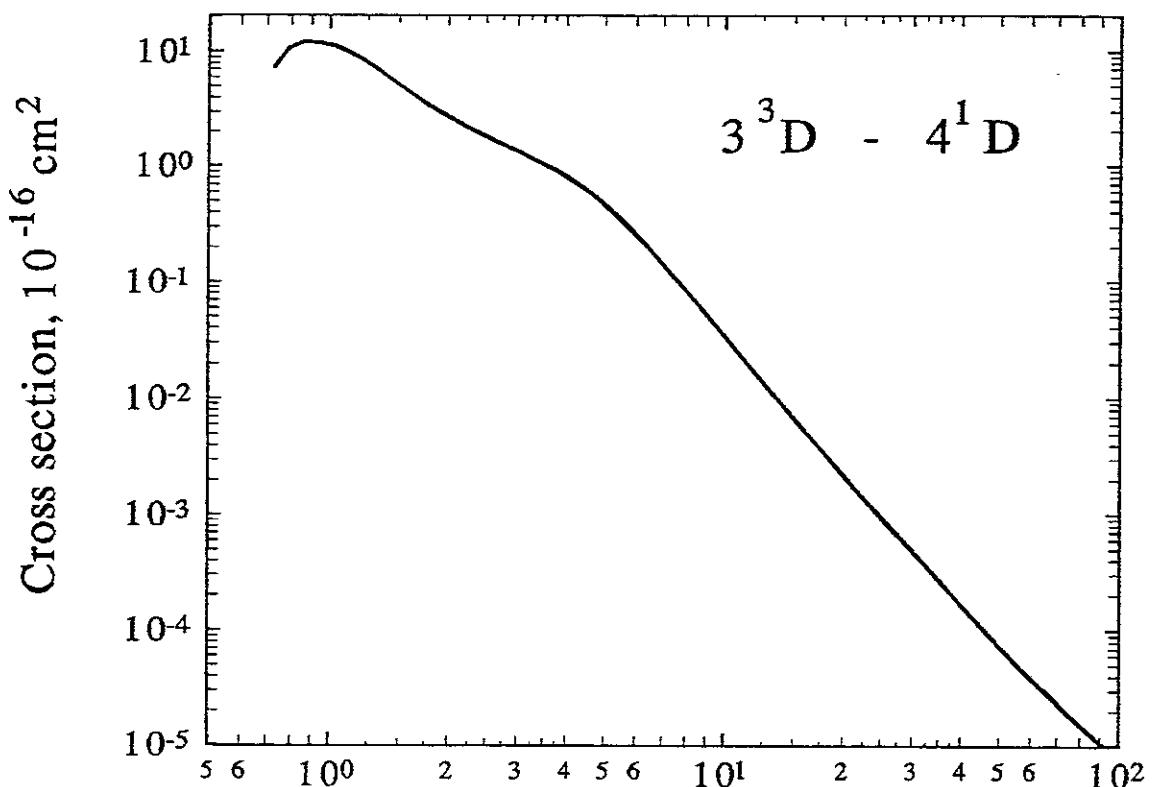


Fig.127 Electron energy, eV

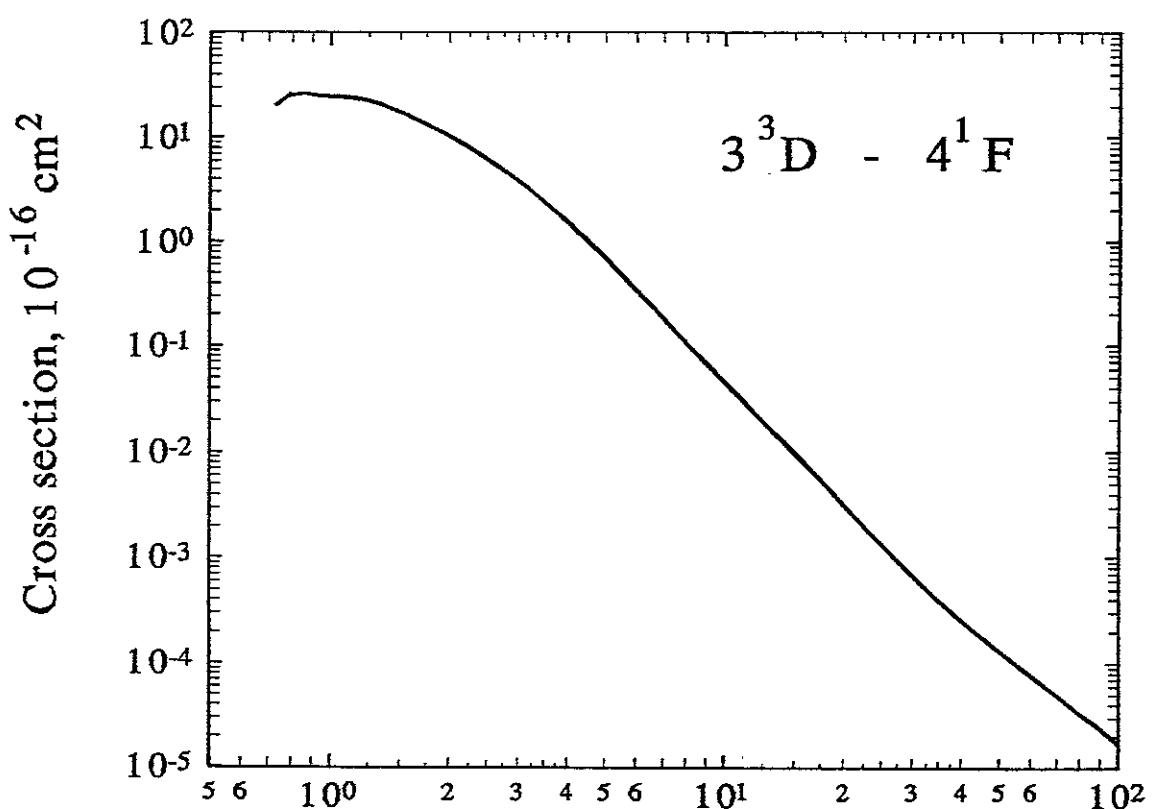


Fig.128 Electron energy, eV

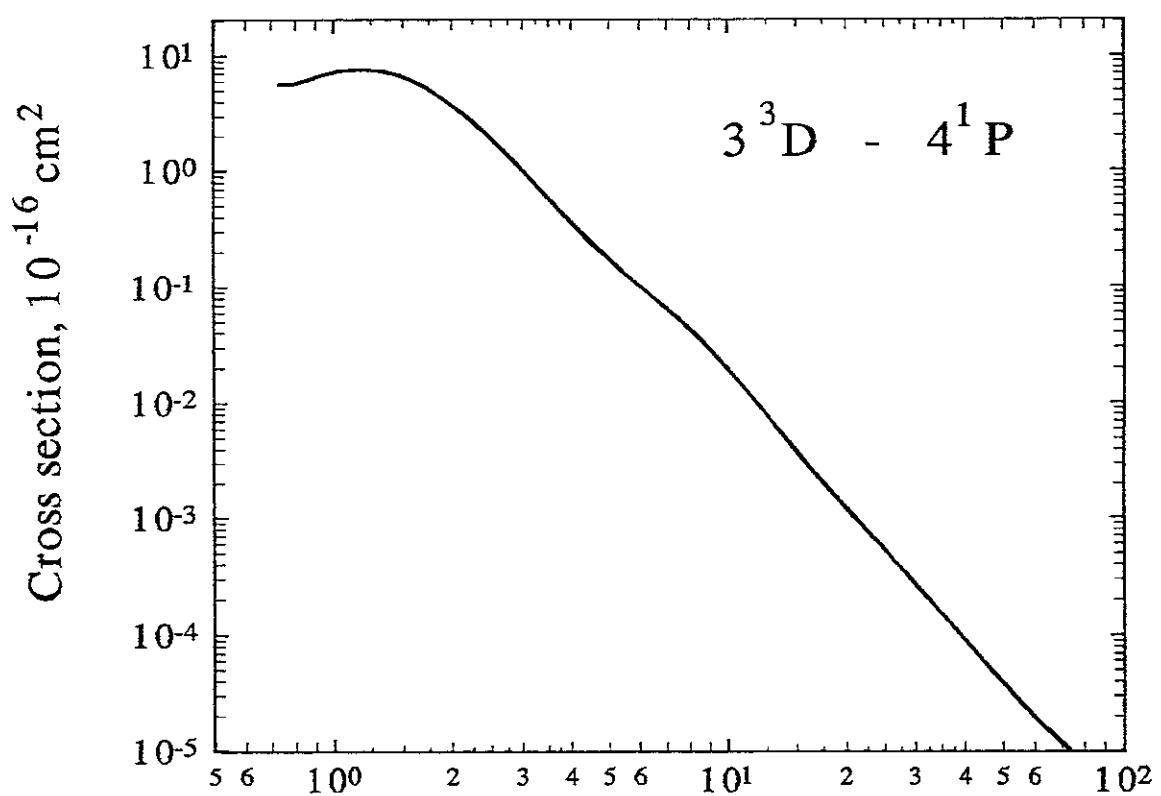


Fig.129 Electron energy, eV

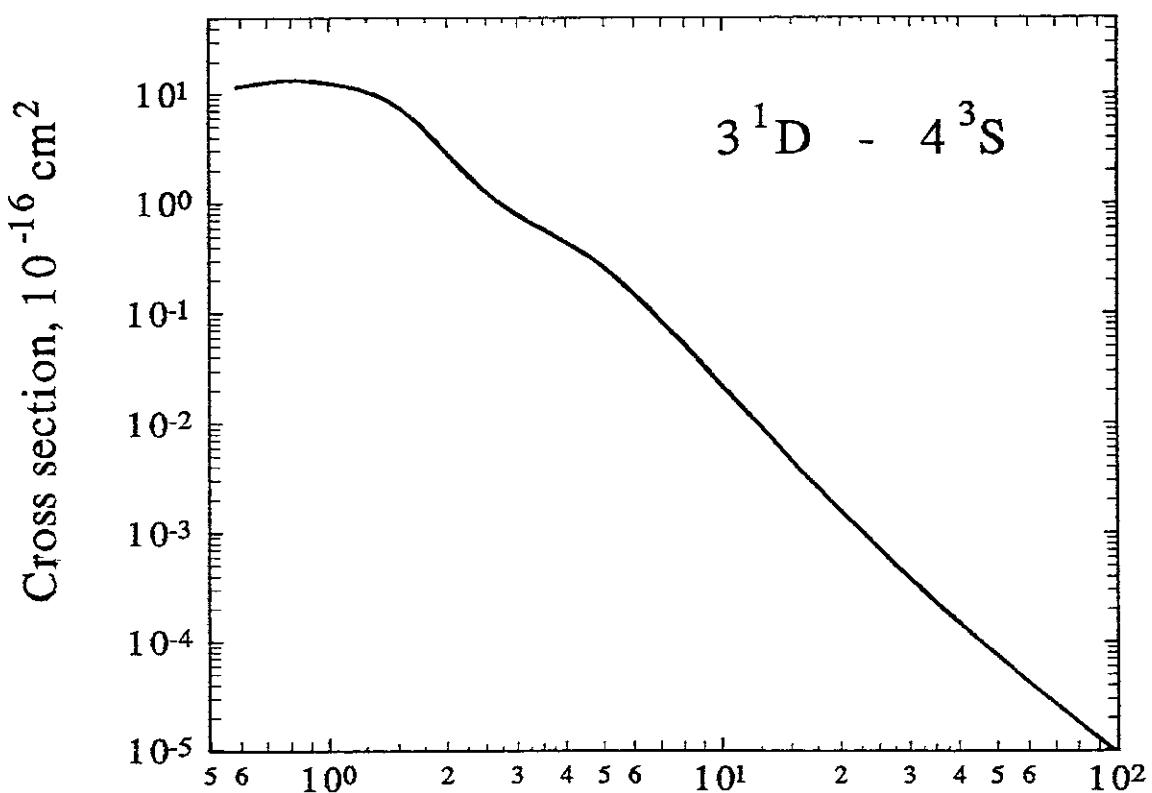


Fig.130 Electron energy, eV

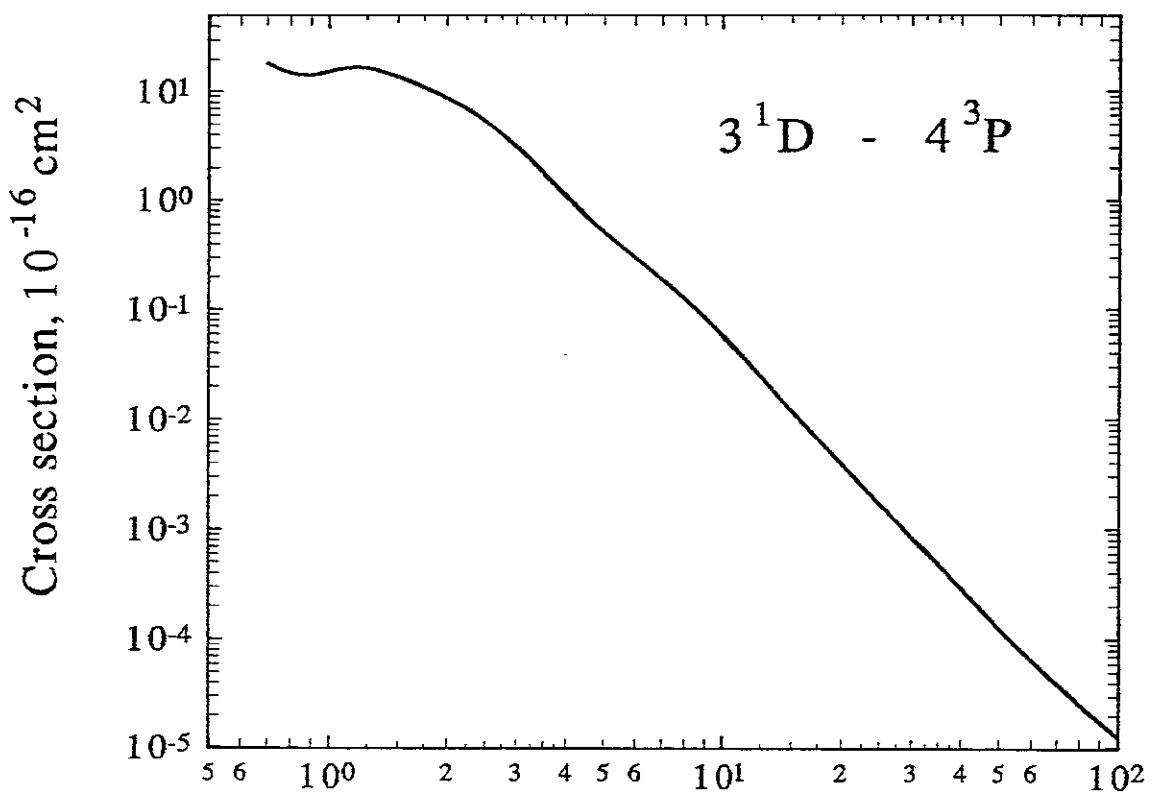


Fig.131 Electron energy, eV

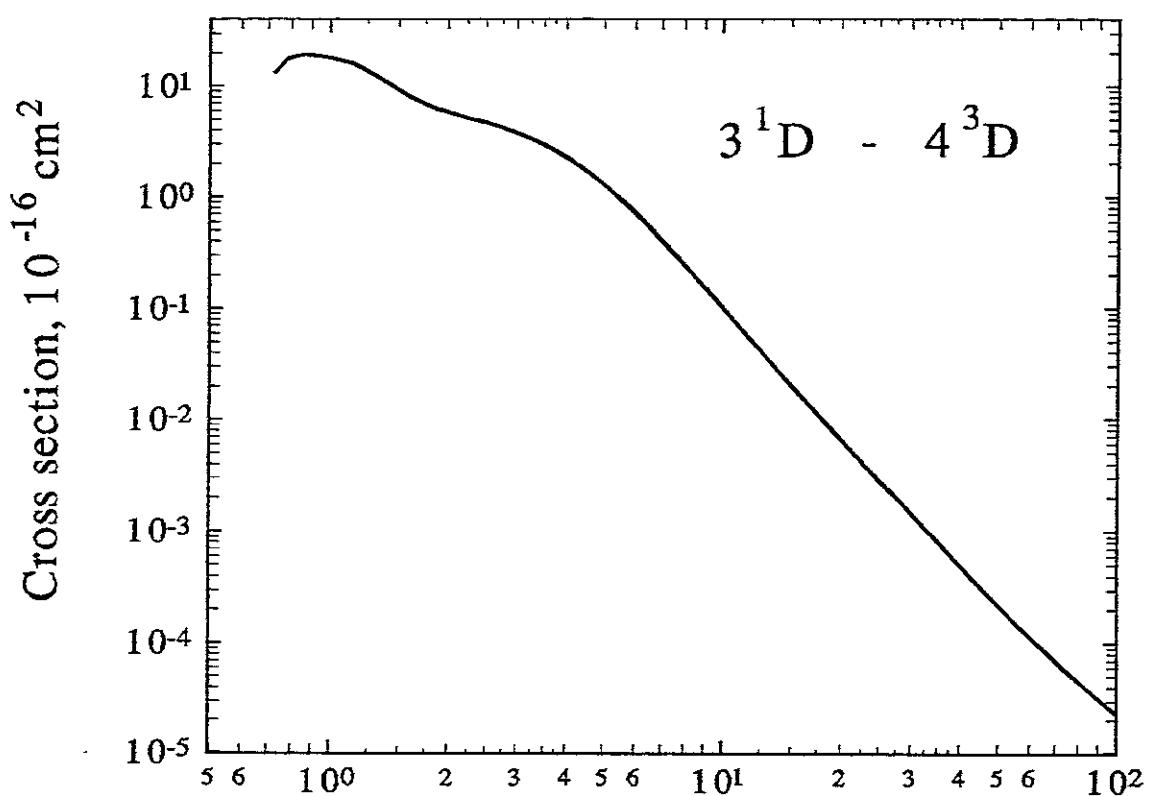


Fig.132 Electron energy, eV

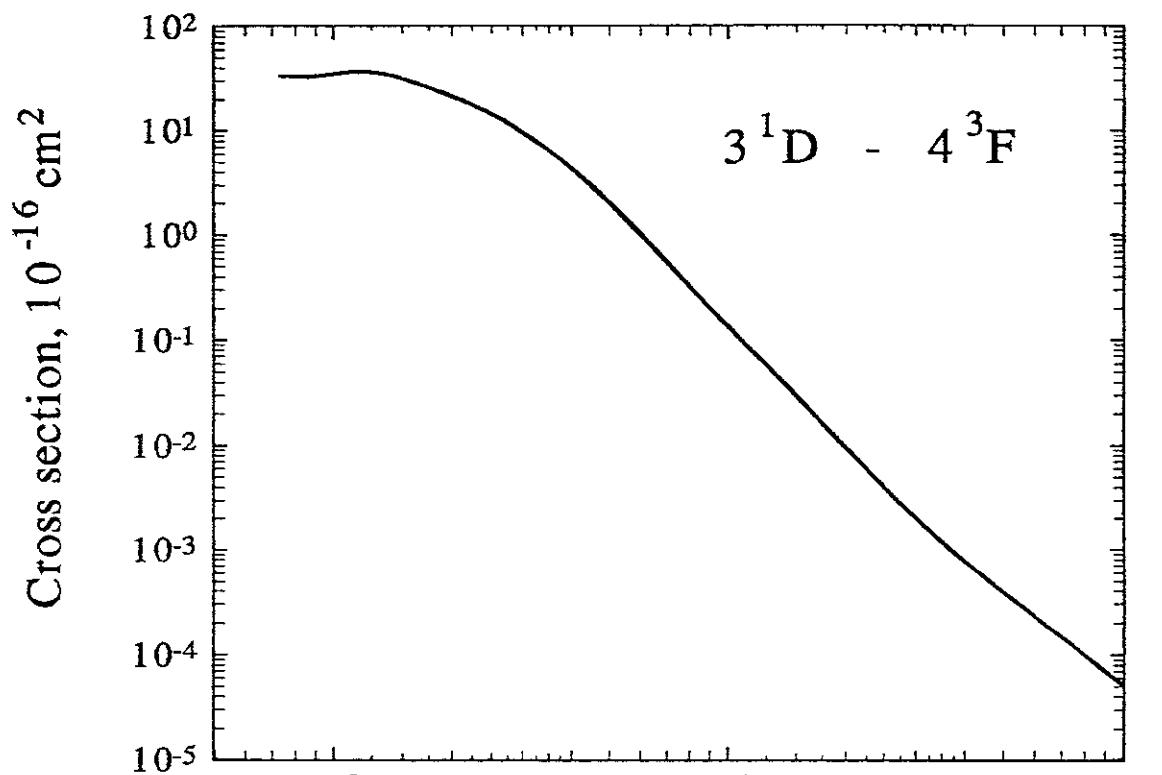


Fig.133 Electron energy, eV

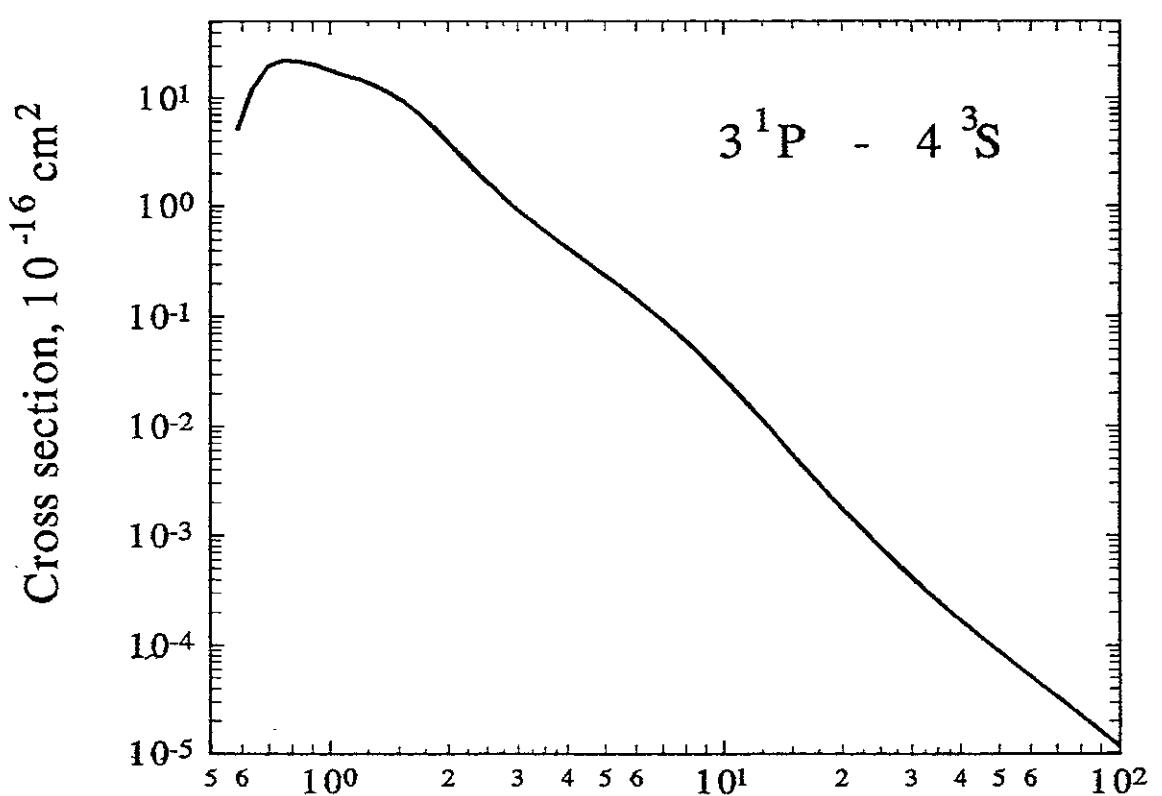


Fig.134 Electron energy, eV

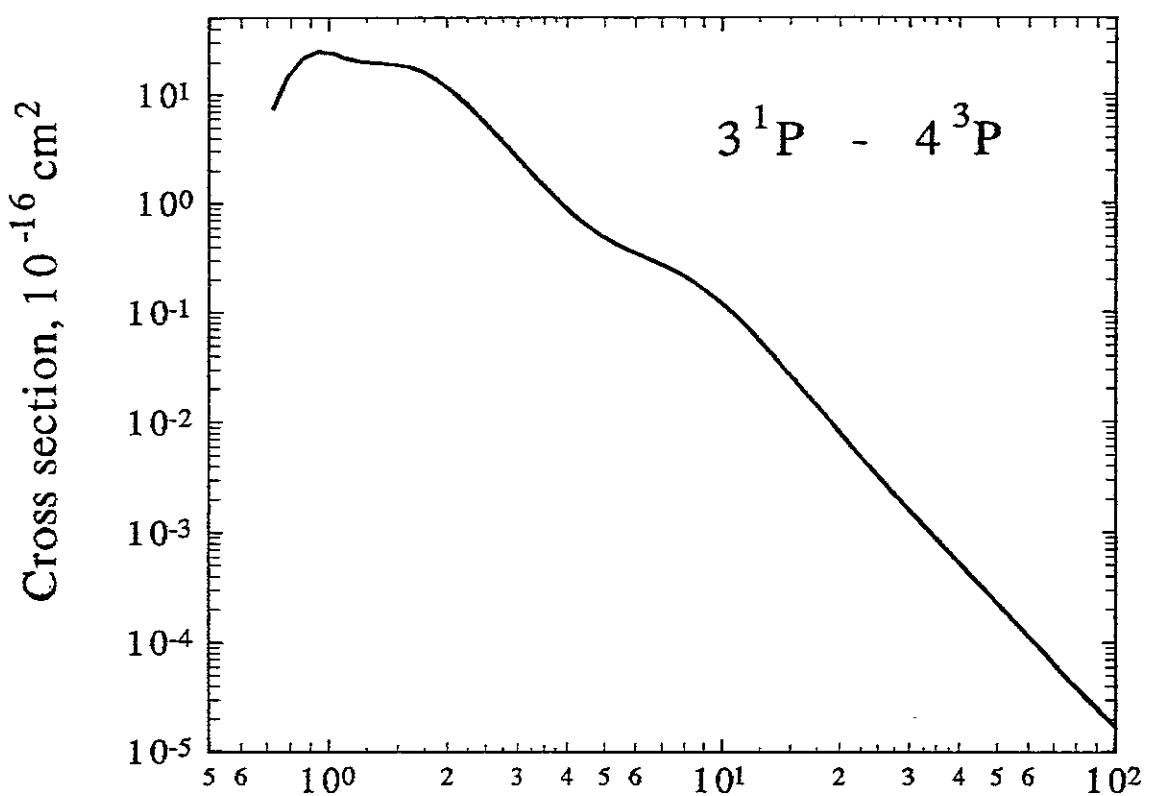


Fig135 Electron energy, eV

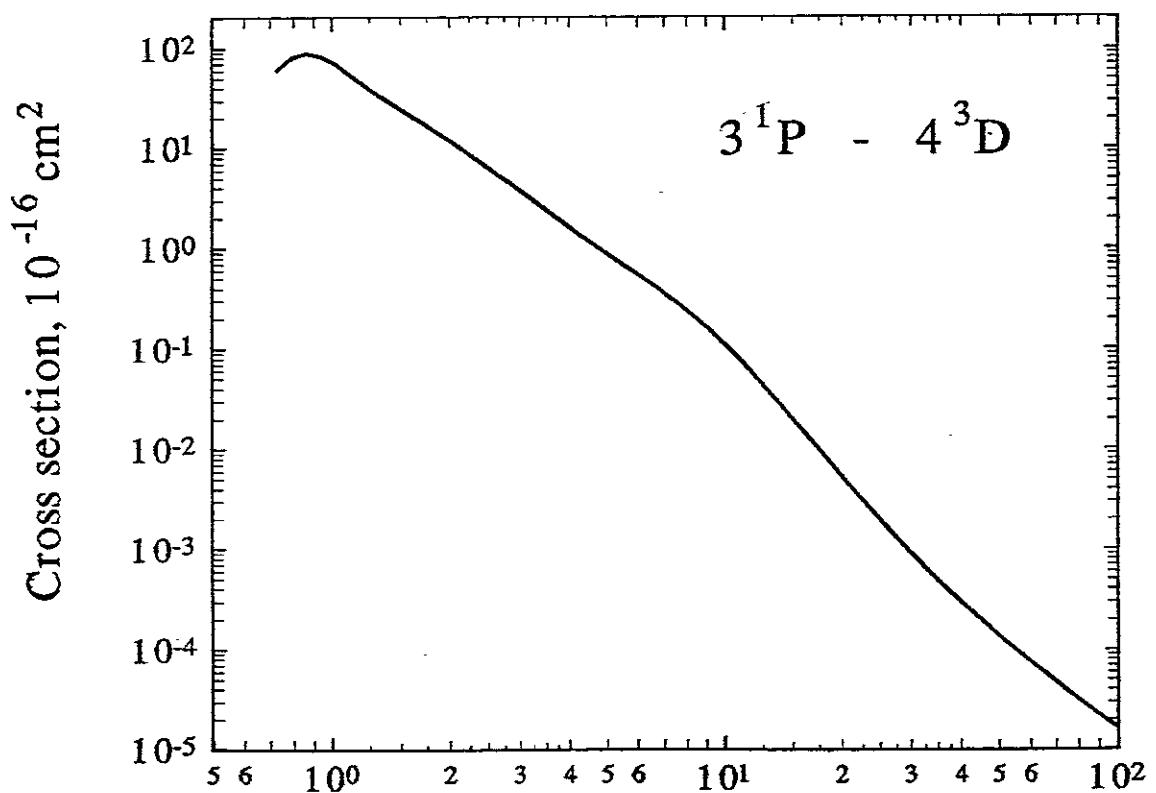


Fig.136 Electron energy, eV

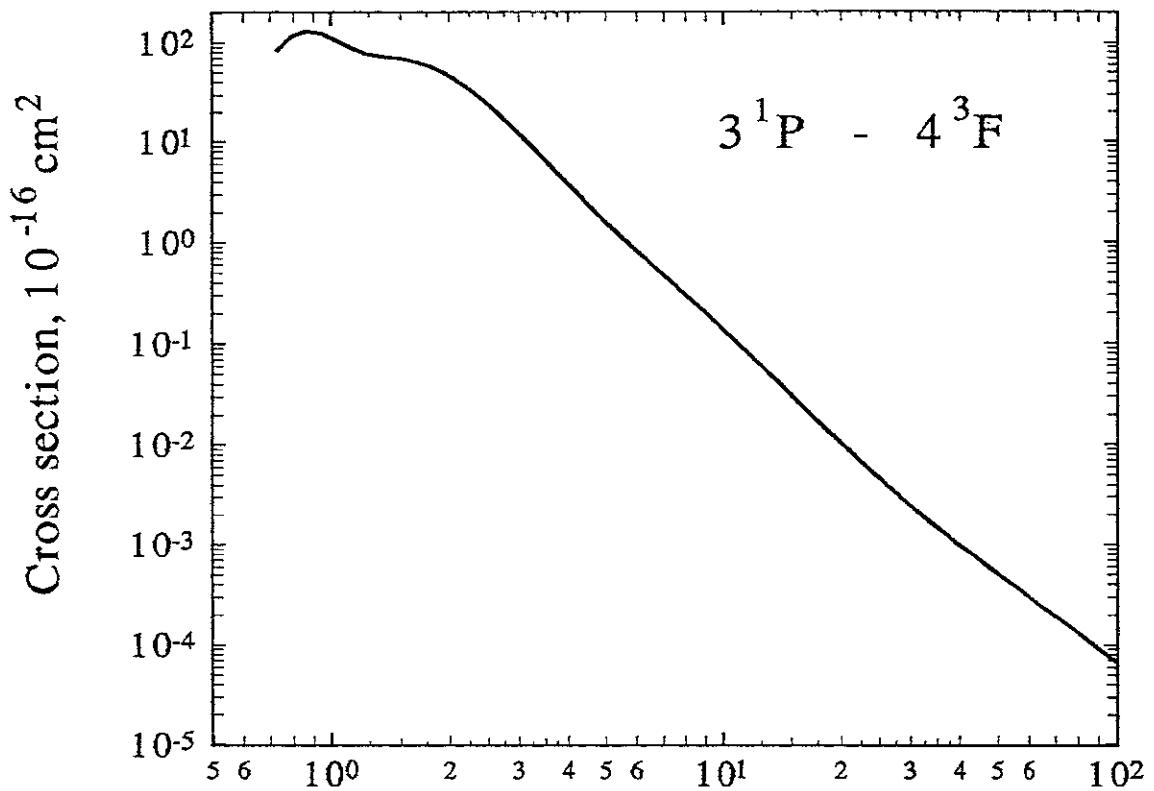


Fig.137 Electron energy, eV

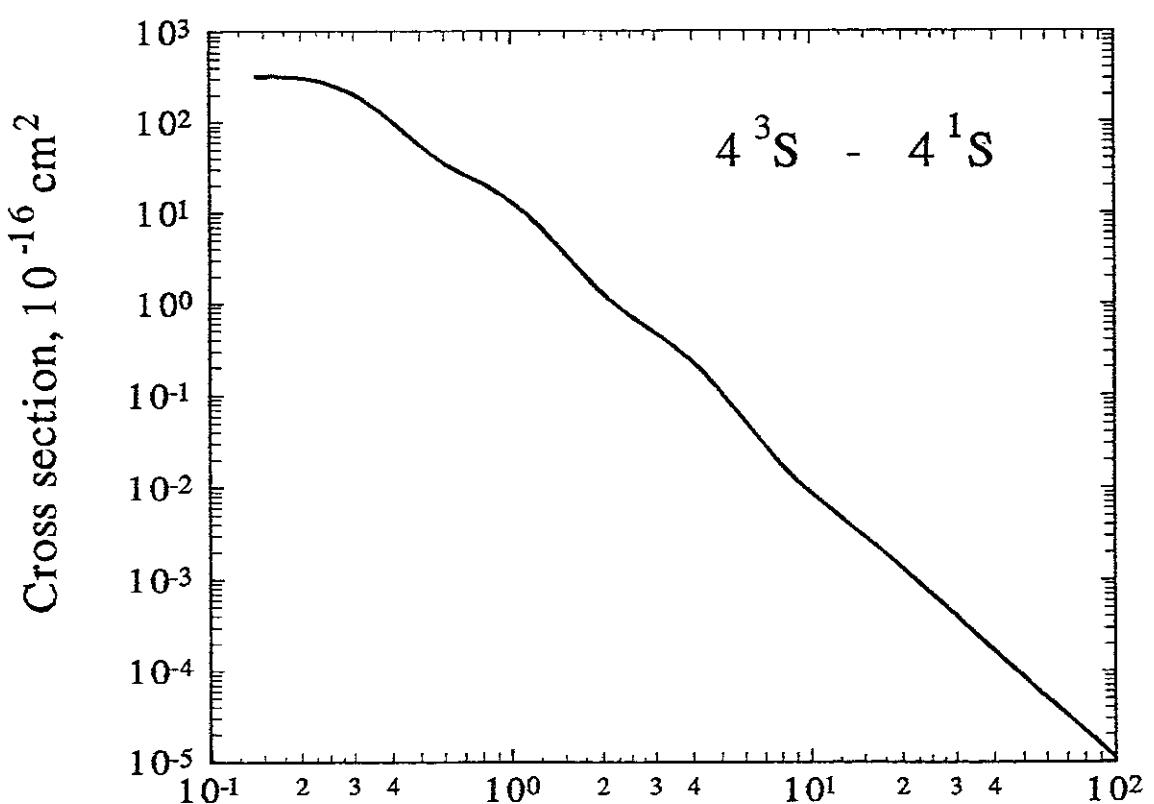


Fig.138 Electron energy, eV

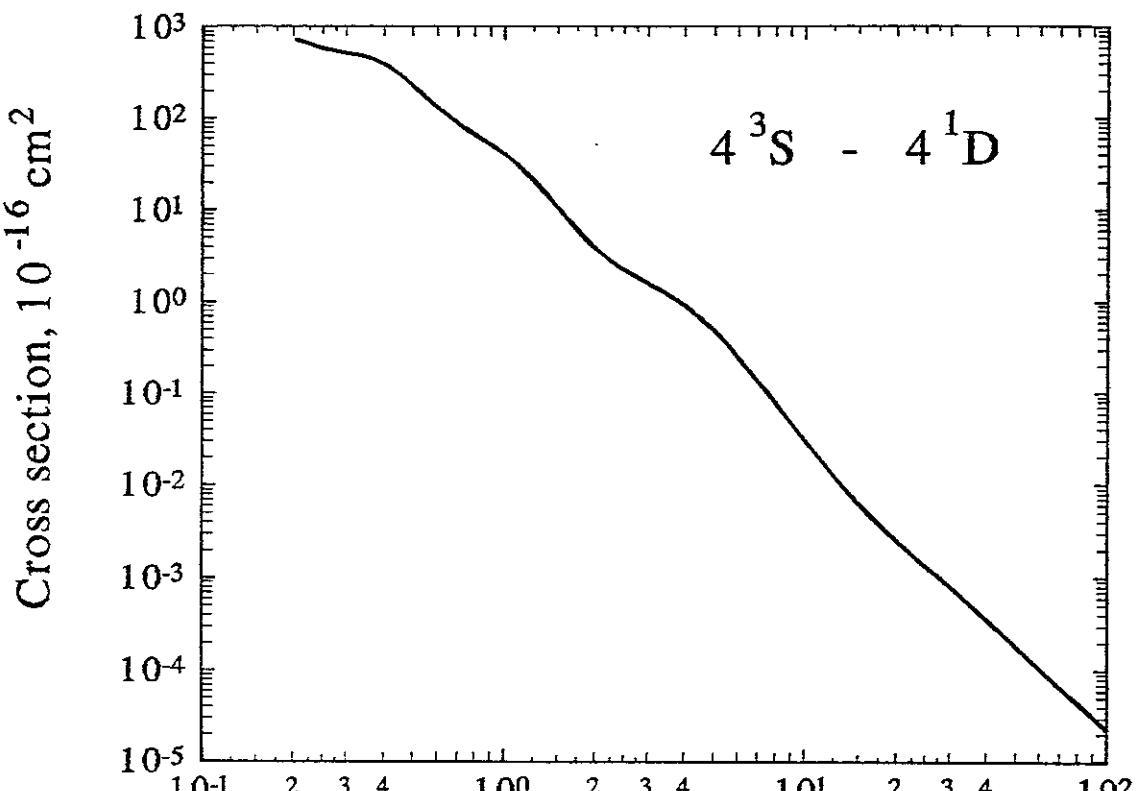


Fig.139 Electron energy, eV

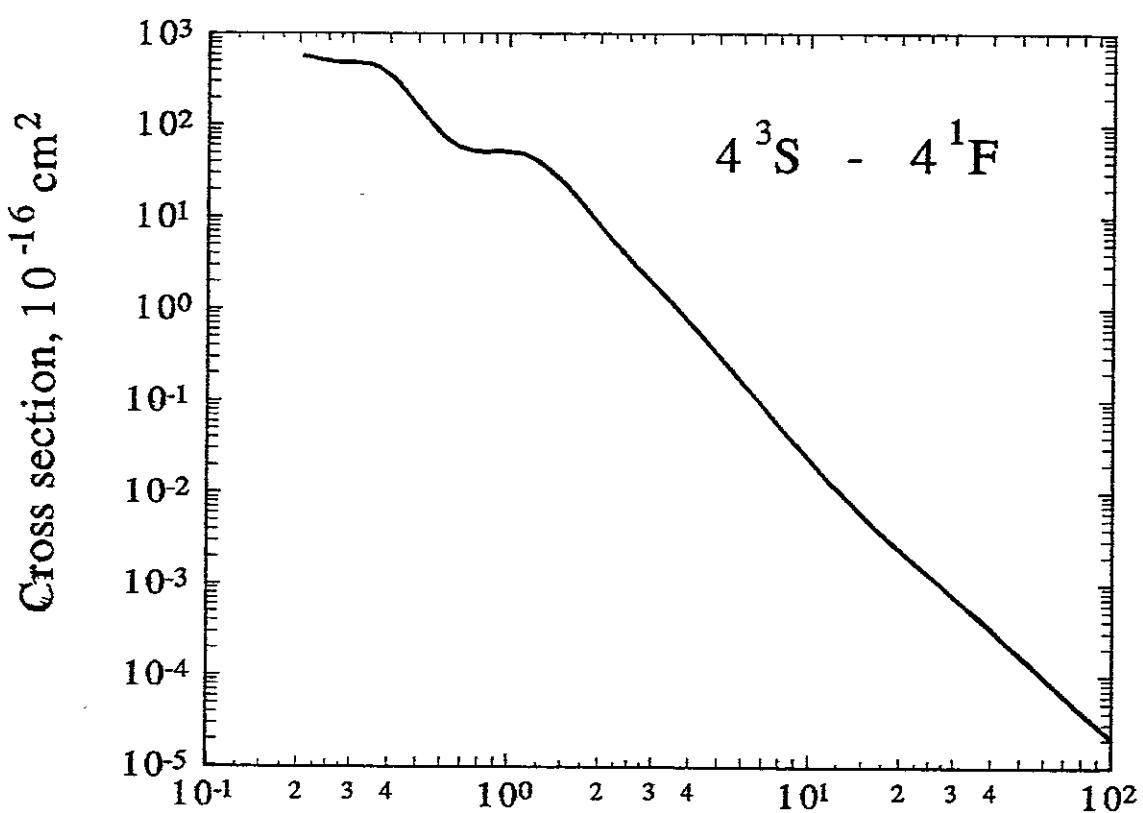


Fig.140 Electron energy, eV

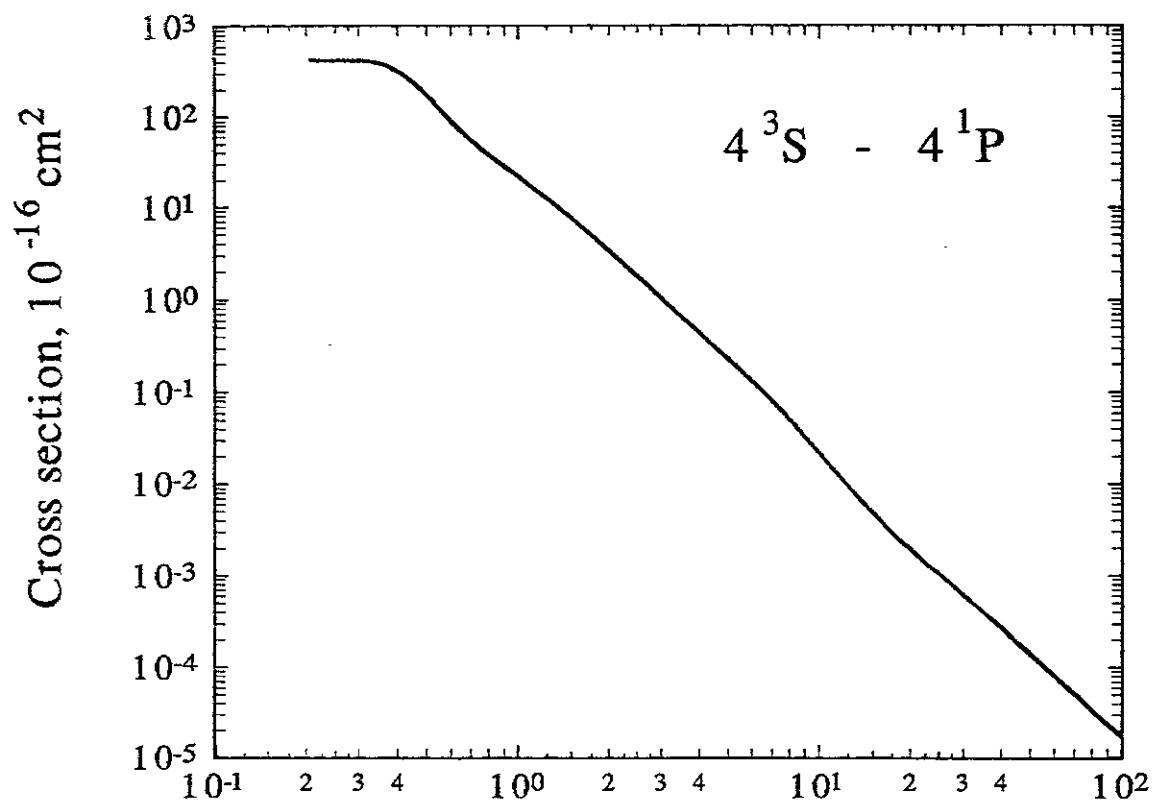


Fig.141 Electron energy, eV

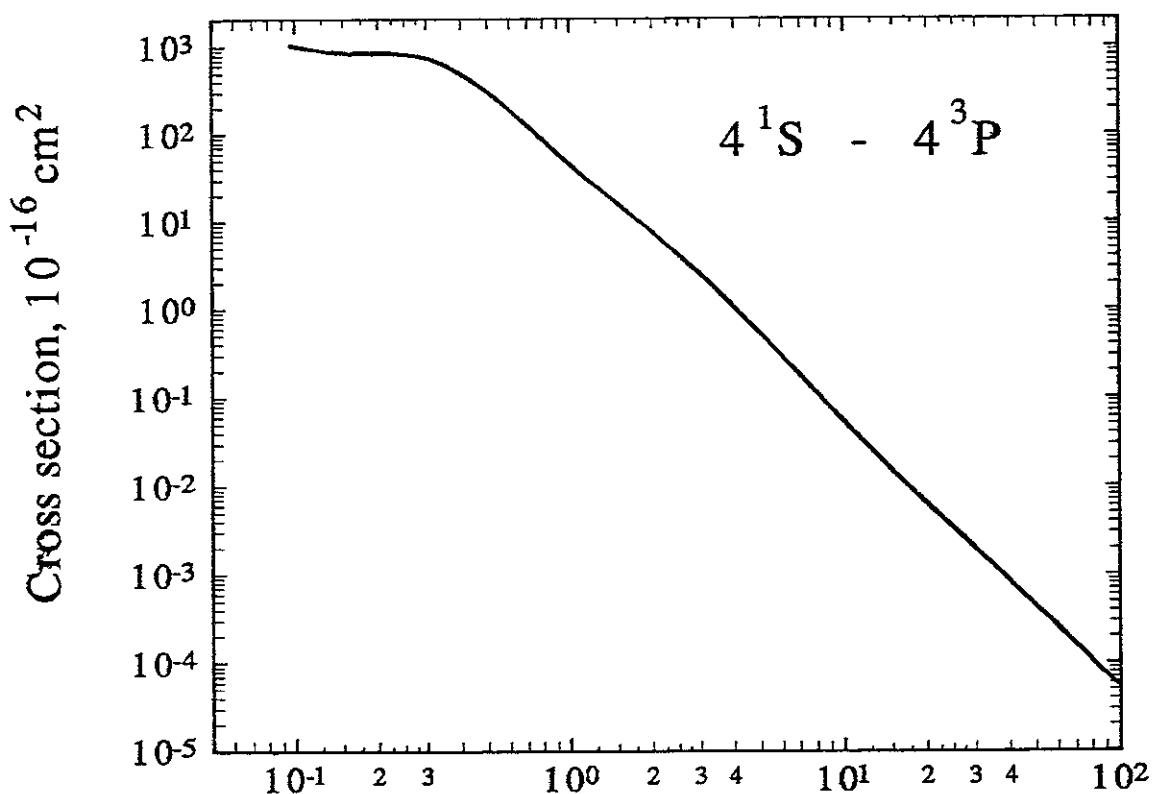


Fig.142 Electron energy, eV

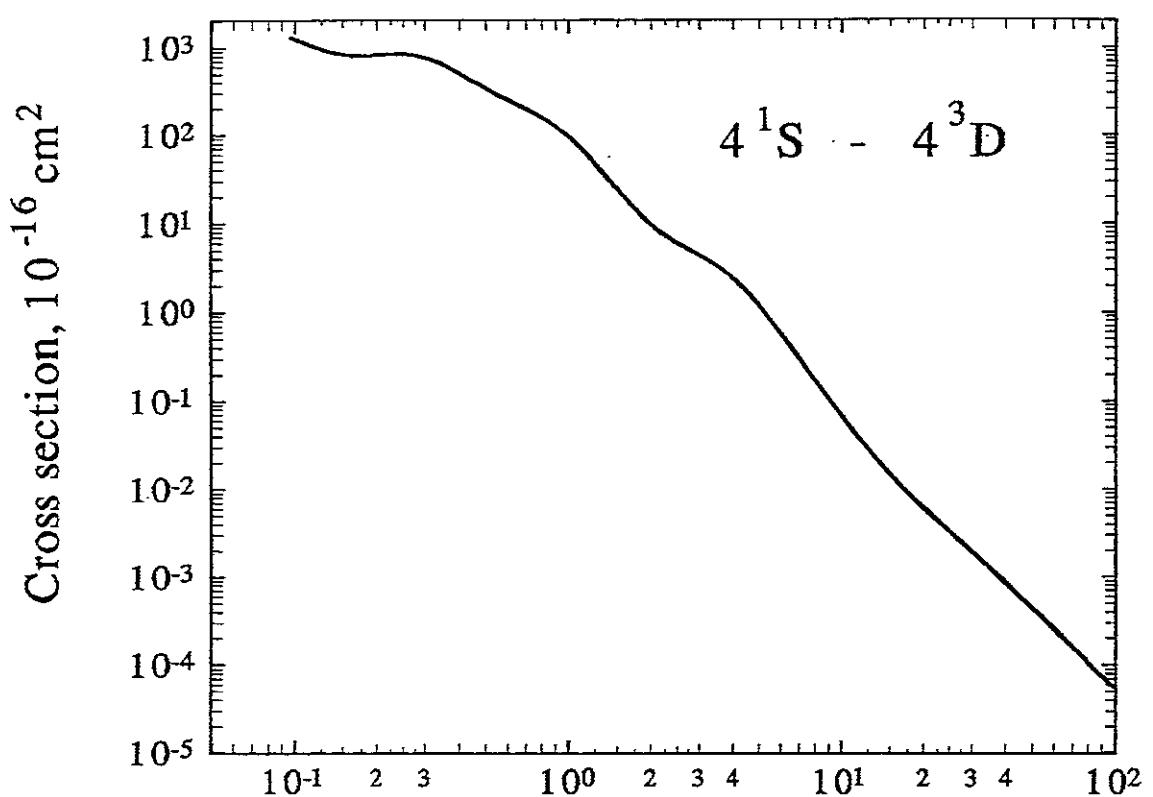


Fig.143 Electron energy, eV

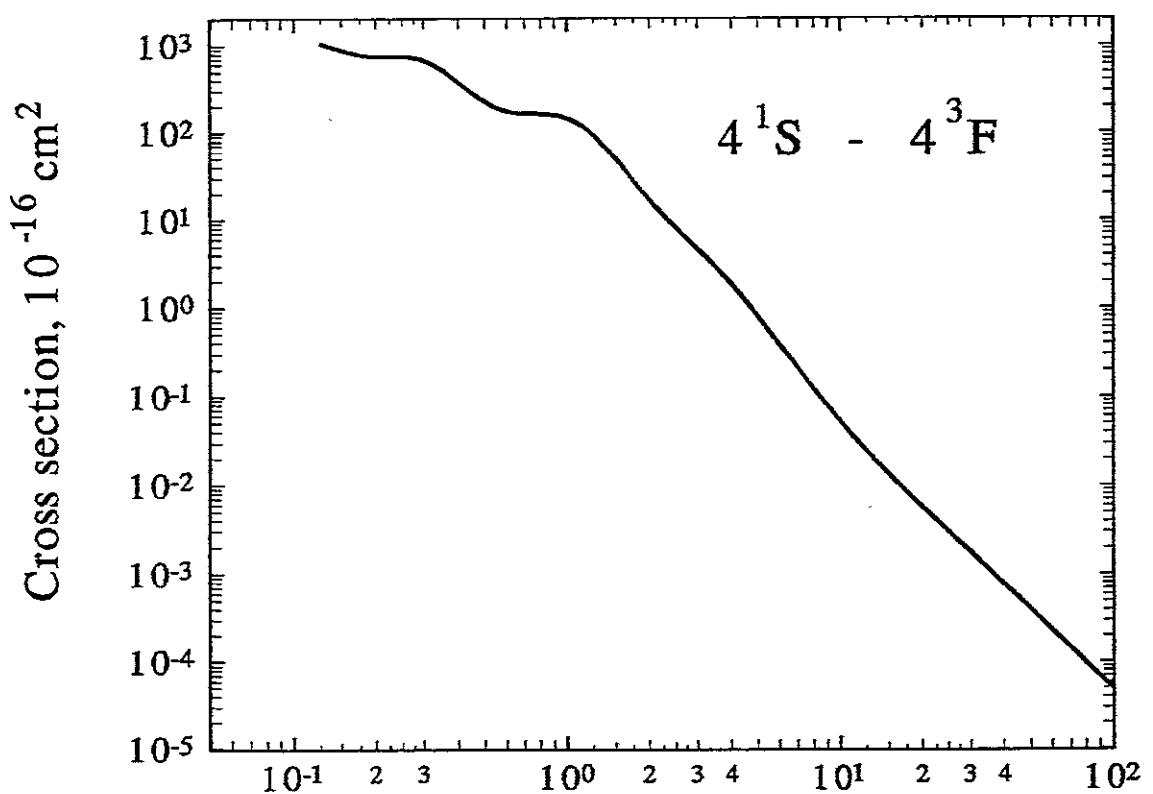


Fig.144 Electron energy, eV

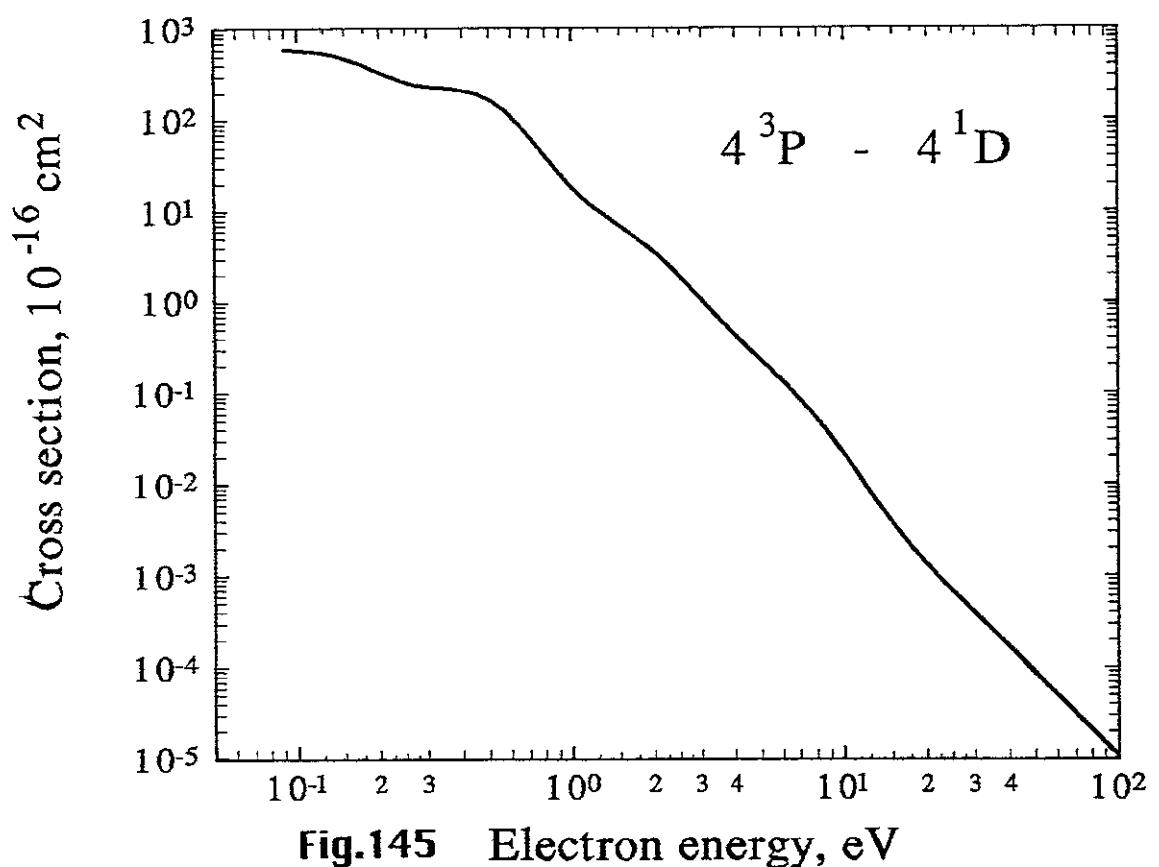


Fig.145 Electron energy, eV

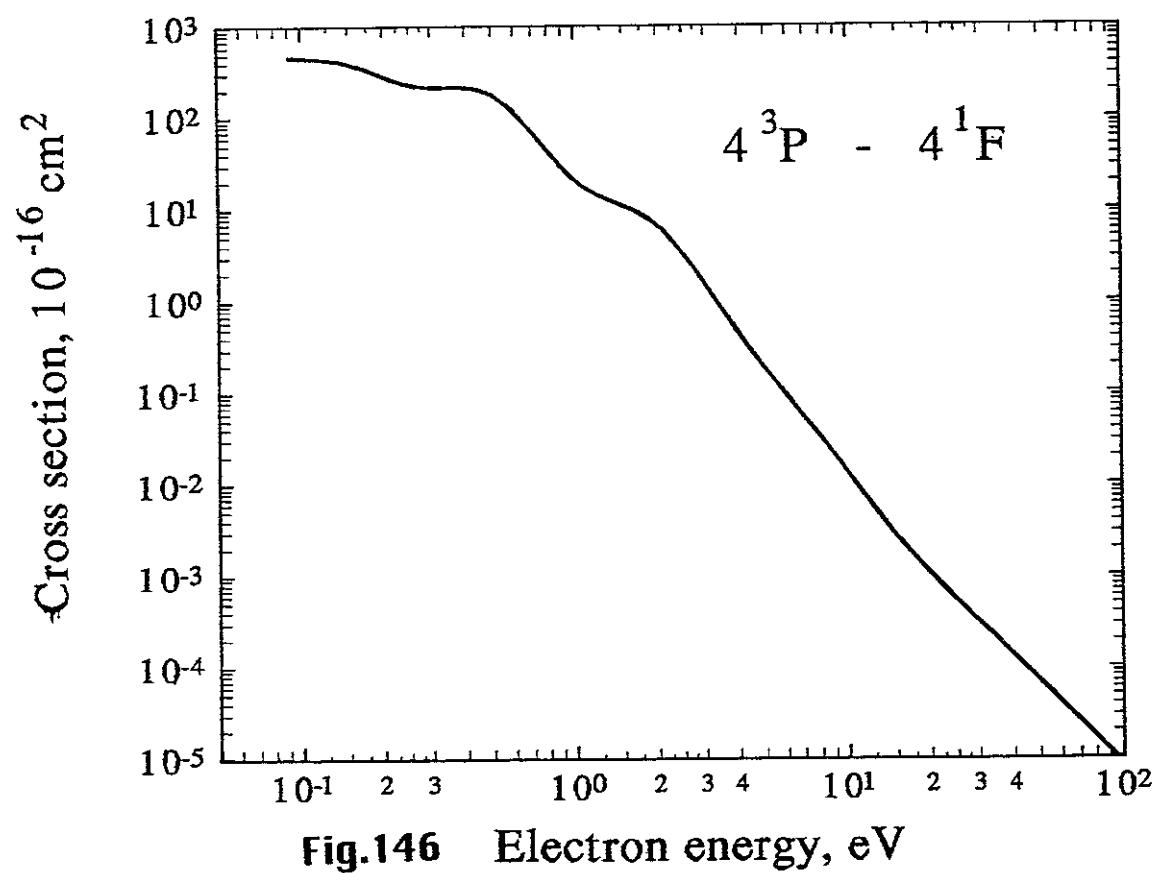


Fig.146 Electron energy, eV

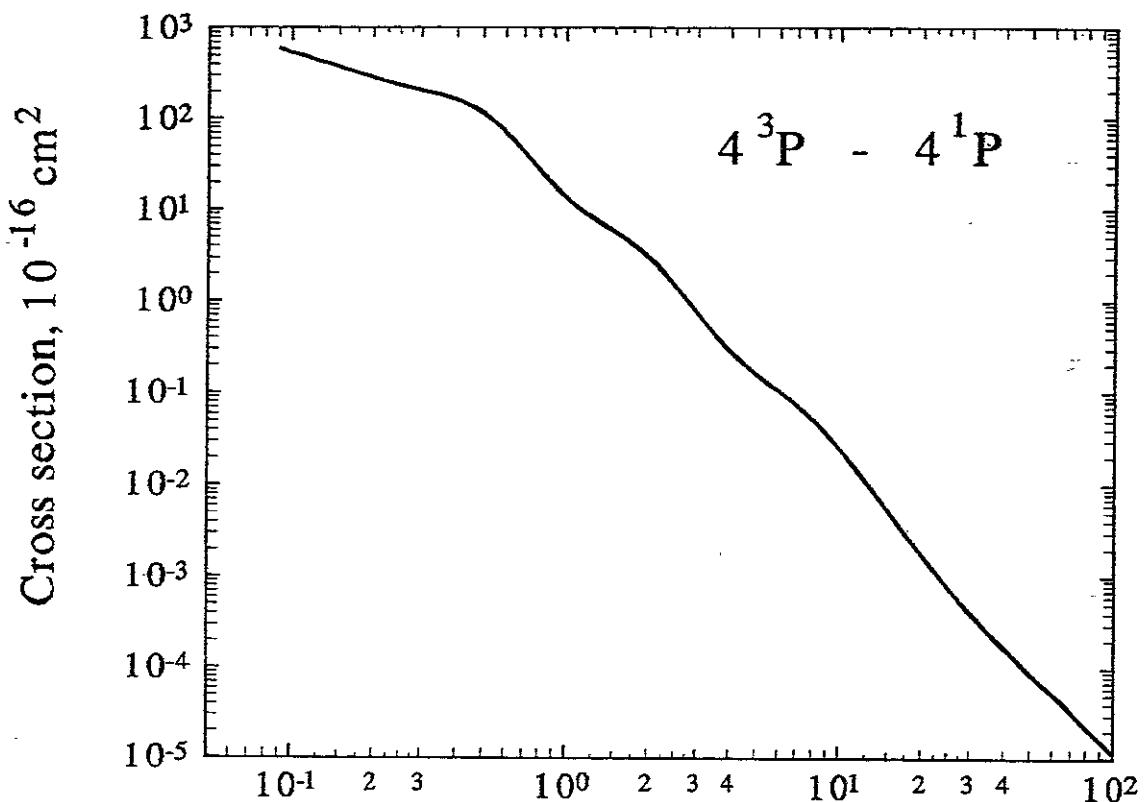


Fig.147 Electron energy, eV

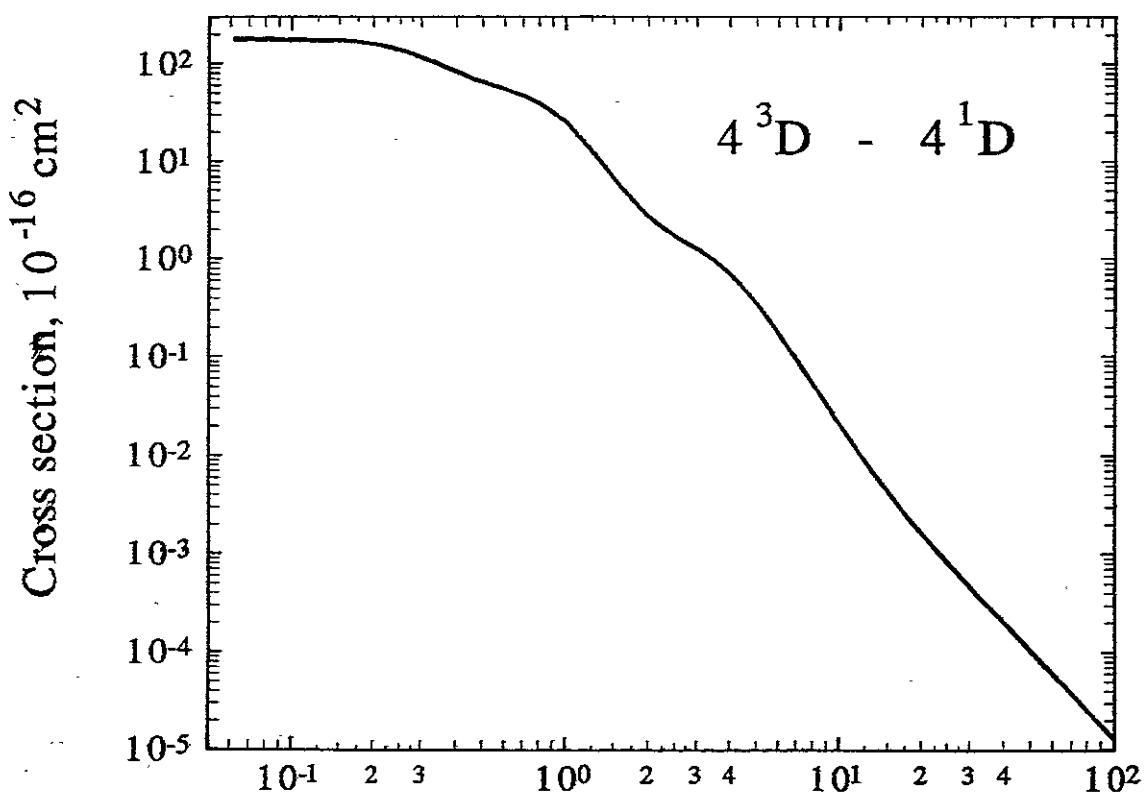


Fig.148 Electron energy, eV

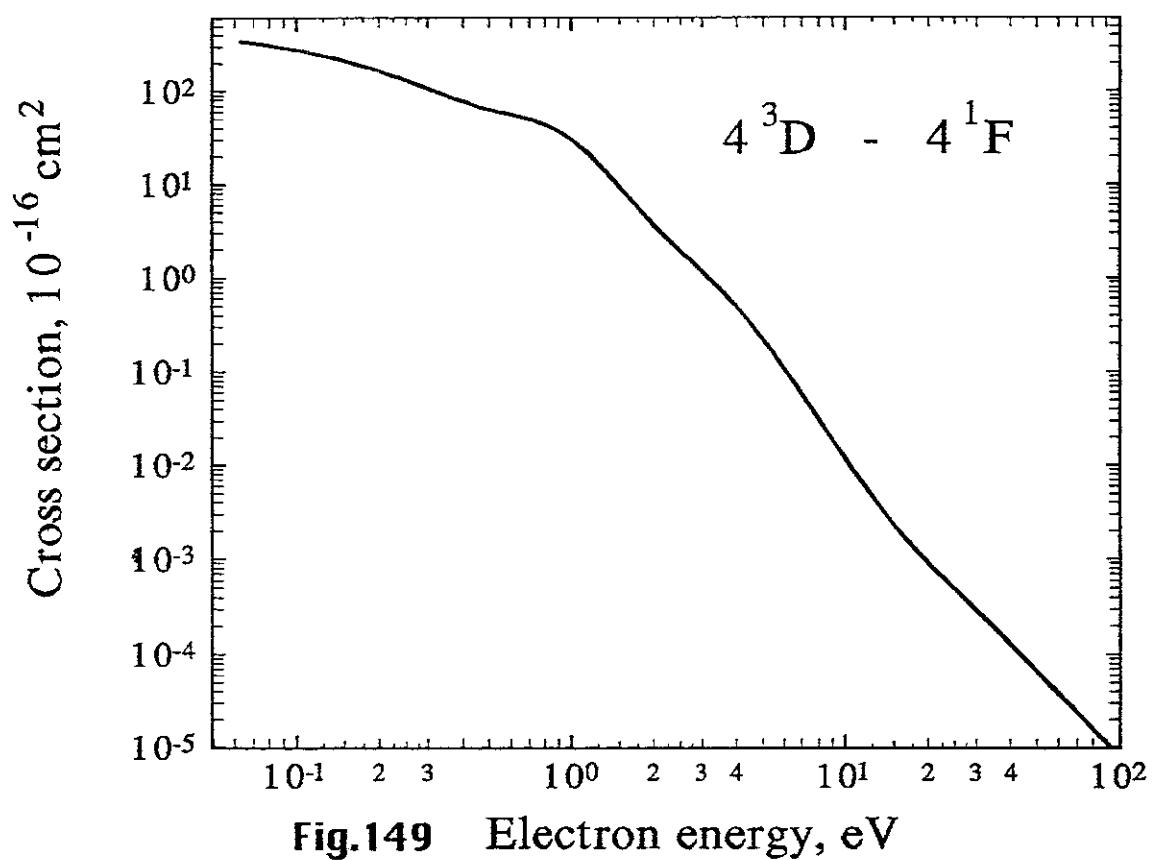


Fig.149 Electron energy, eV

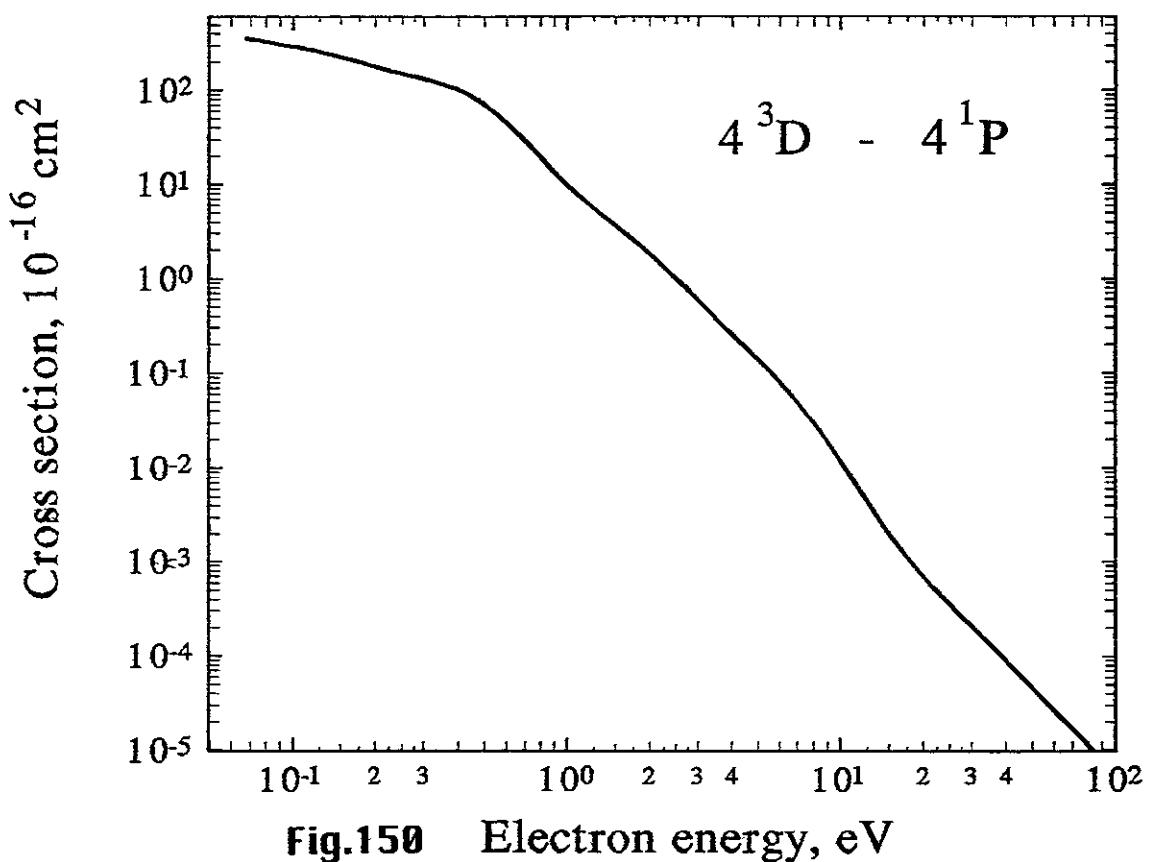


Fig.150 Electron energy, eV

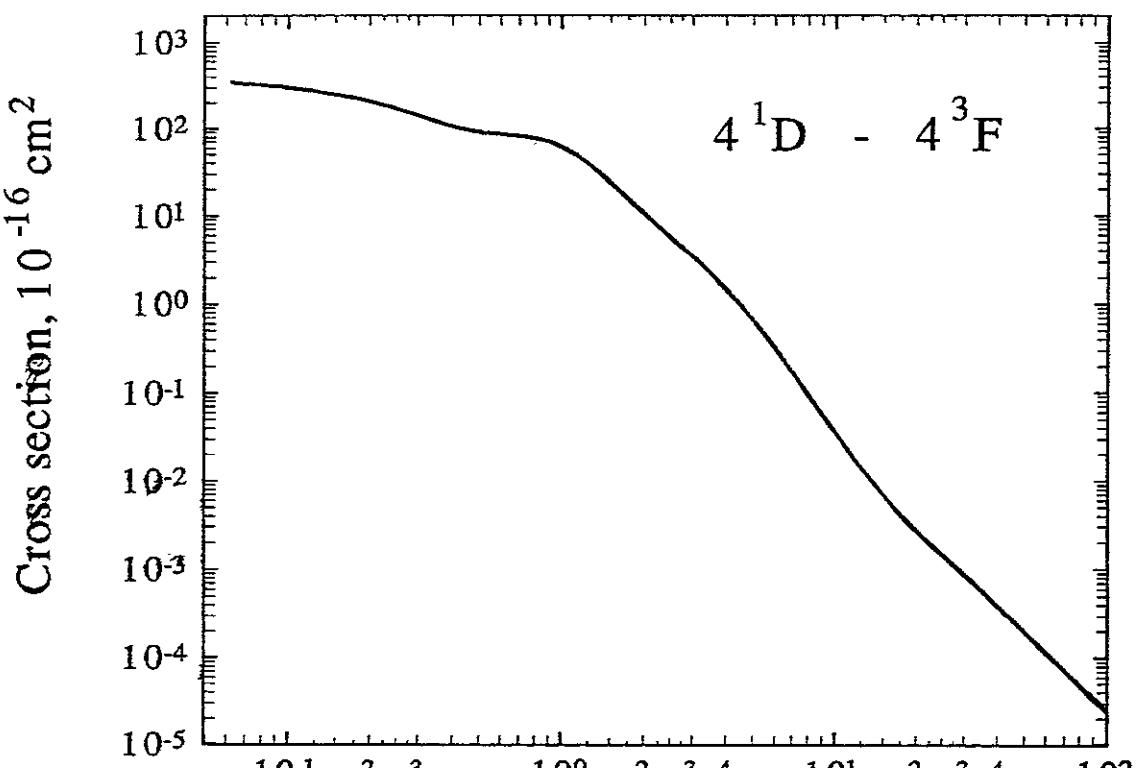


Fig.151 Electron energy, eV

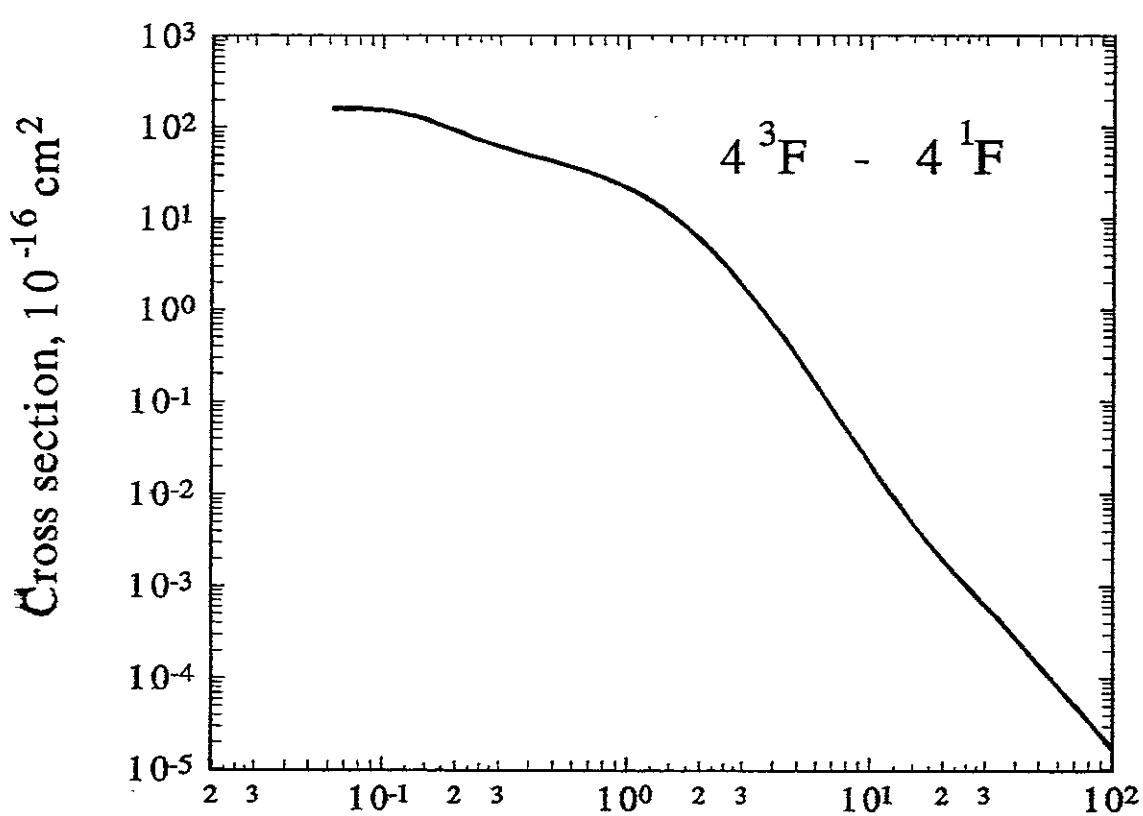


Fig.152 Electron energy, eV

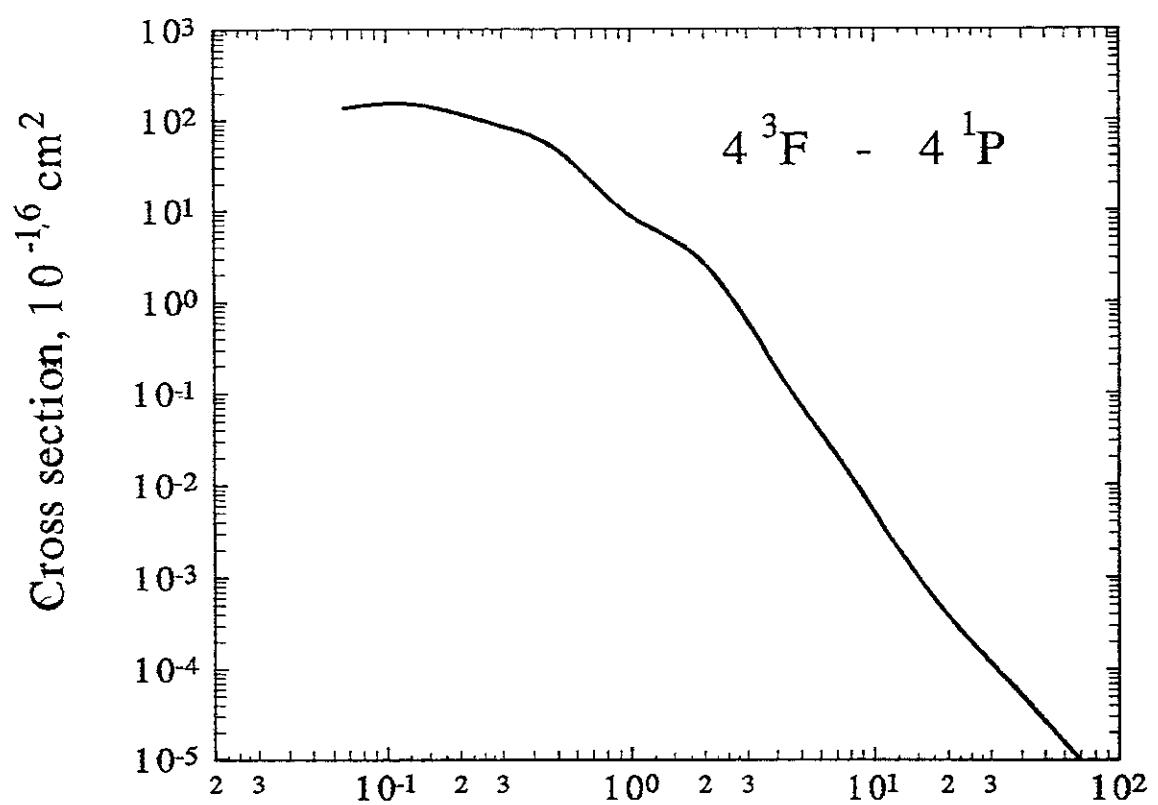


Fig.153 Electron energy, eV

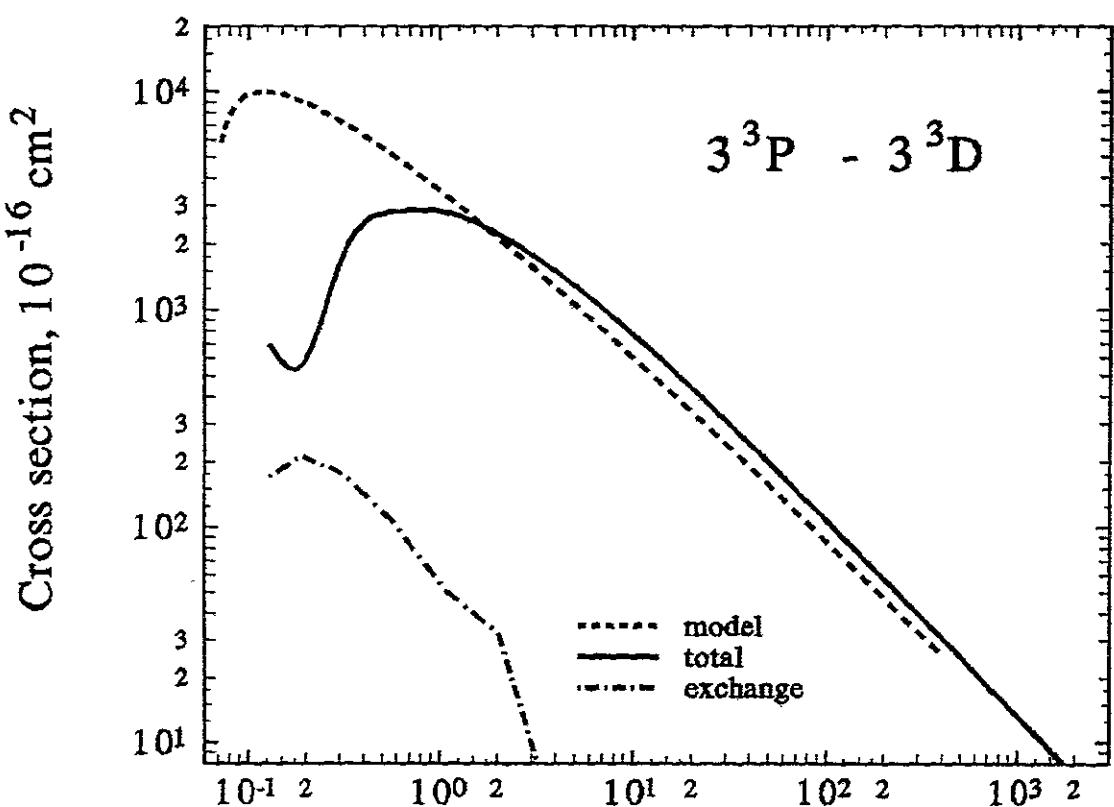


Fig.154 Electron energy, eV

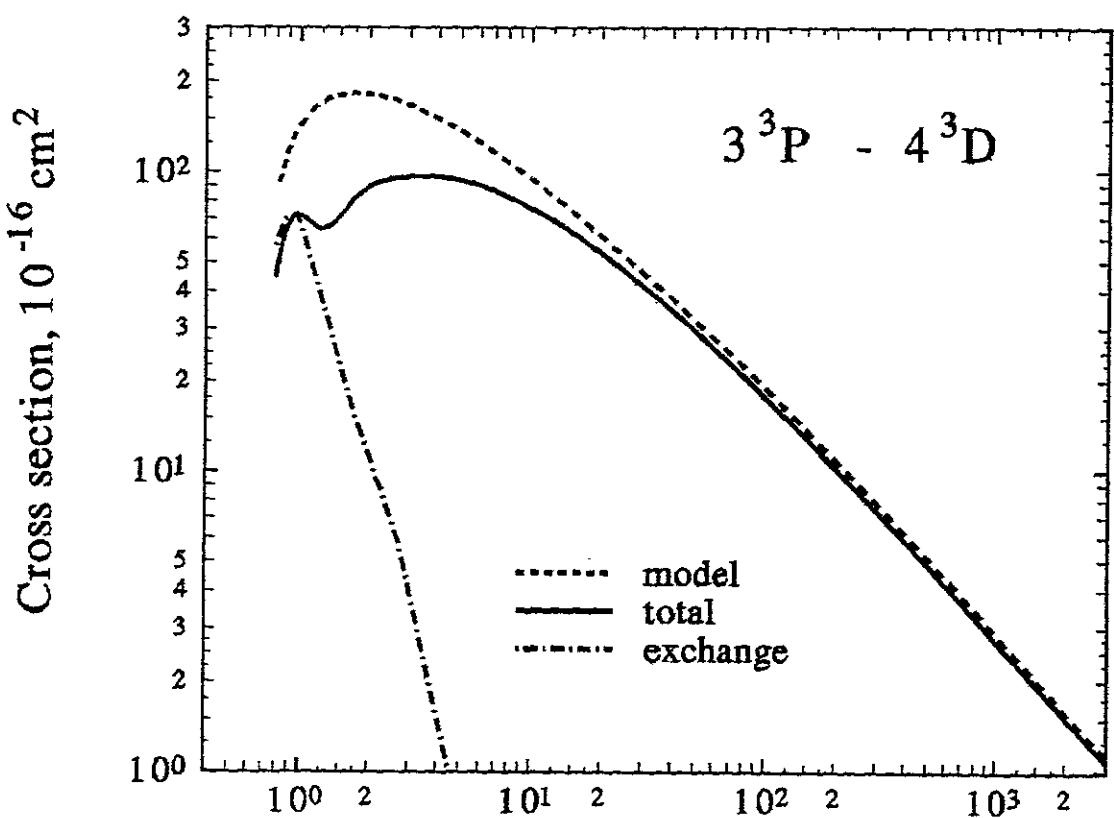


Fig.155 Electron energy, eV

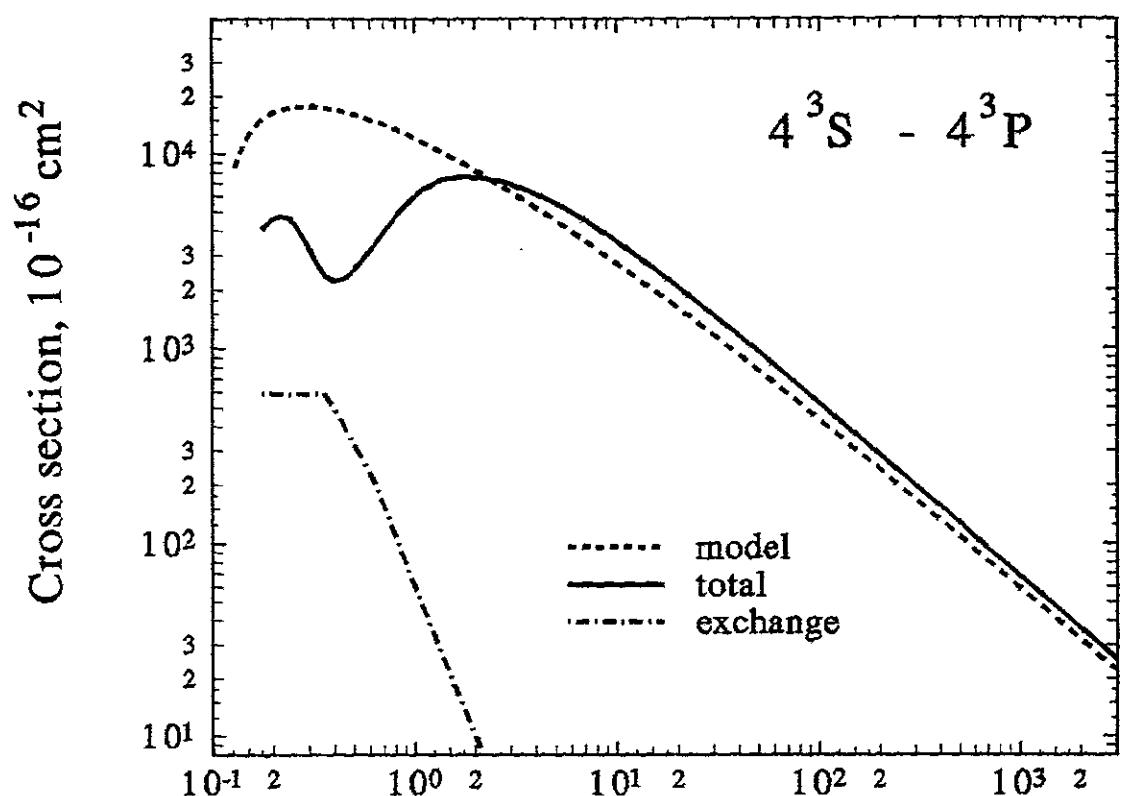


Fig.156 Electron energy, eV

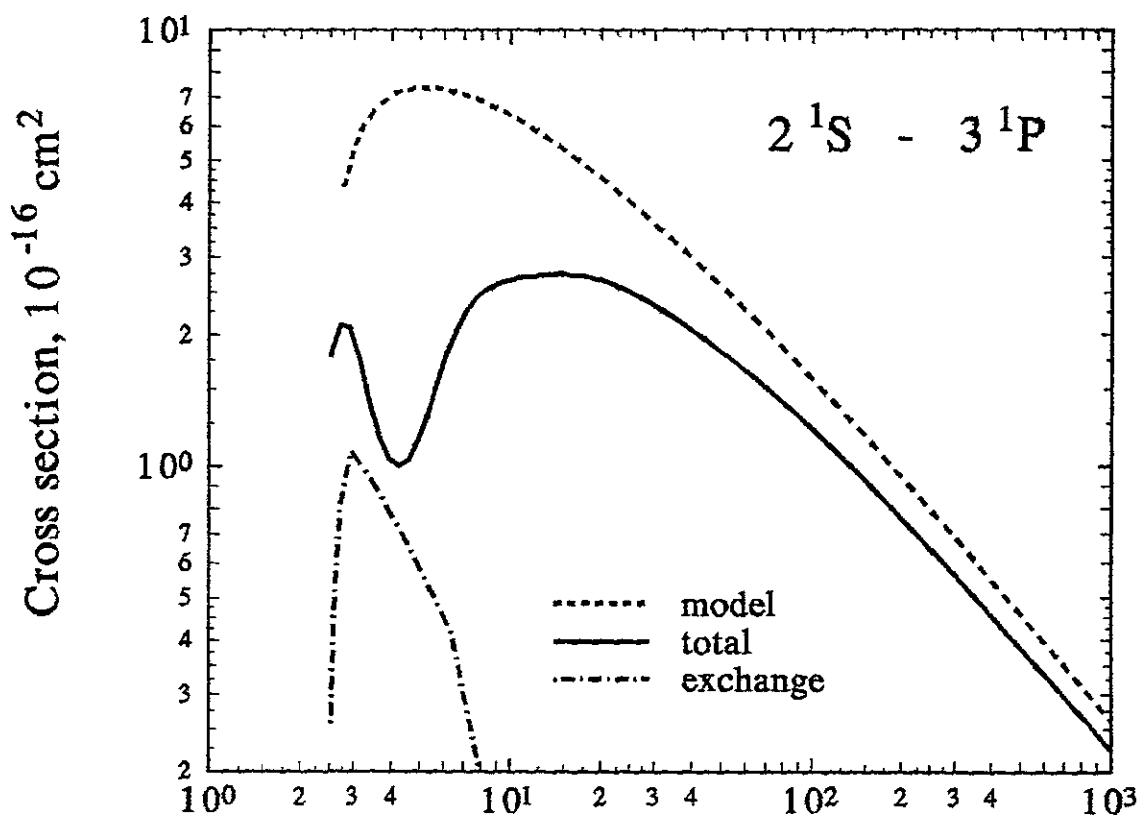


Fig.157 Electron energy, eV

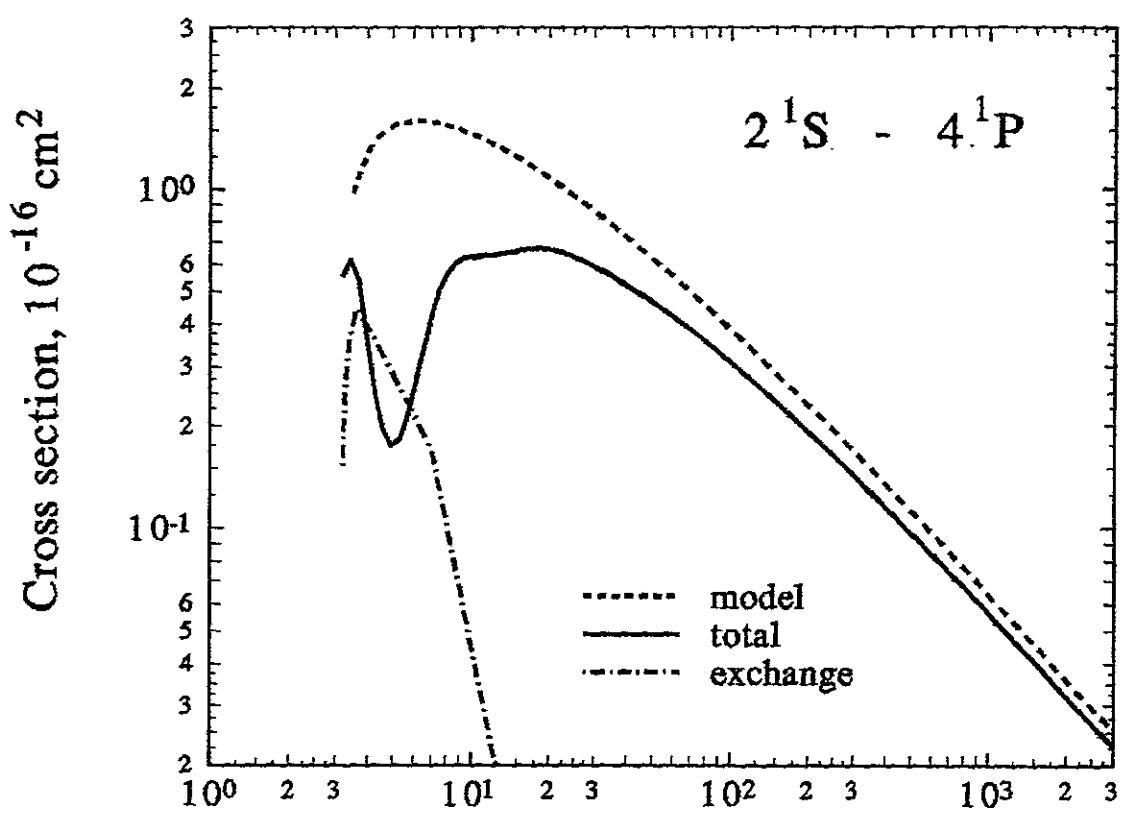


Fig.158 Electron energy, eV

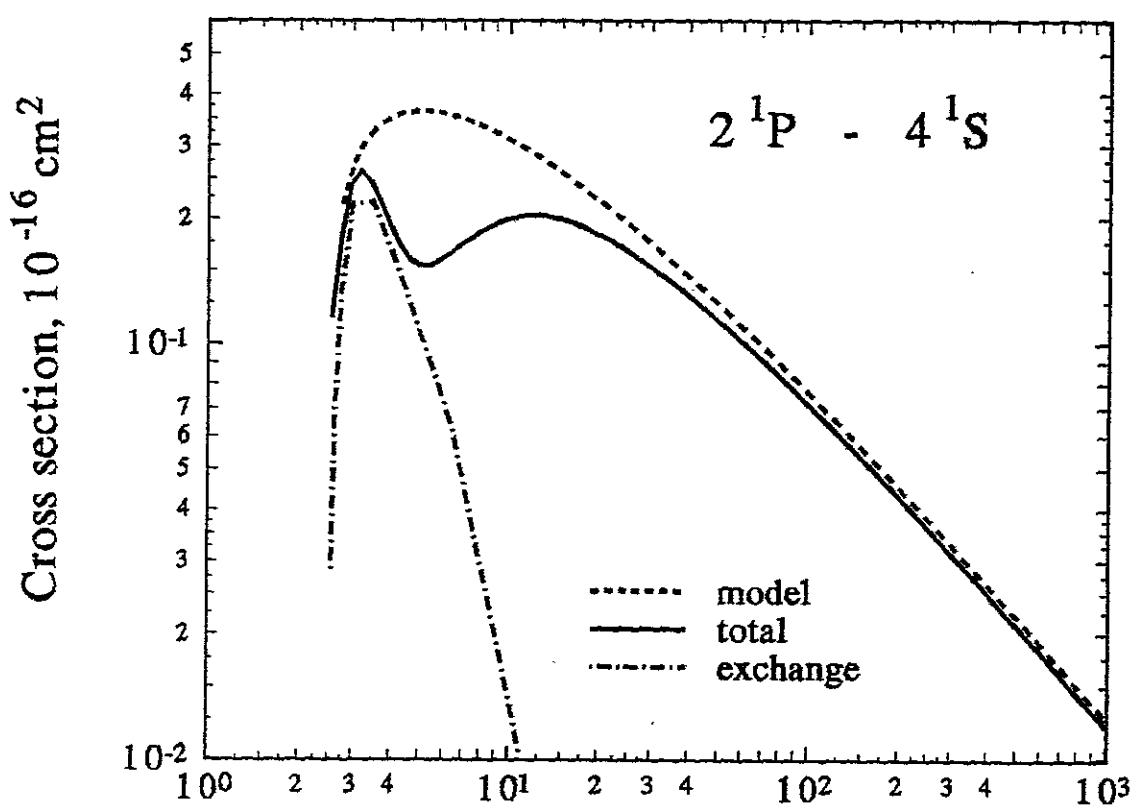


Fig.159 Electron energy, eV

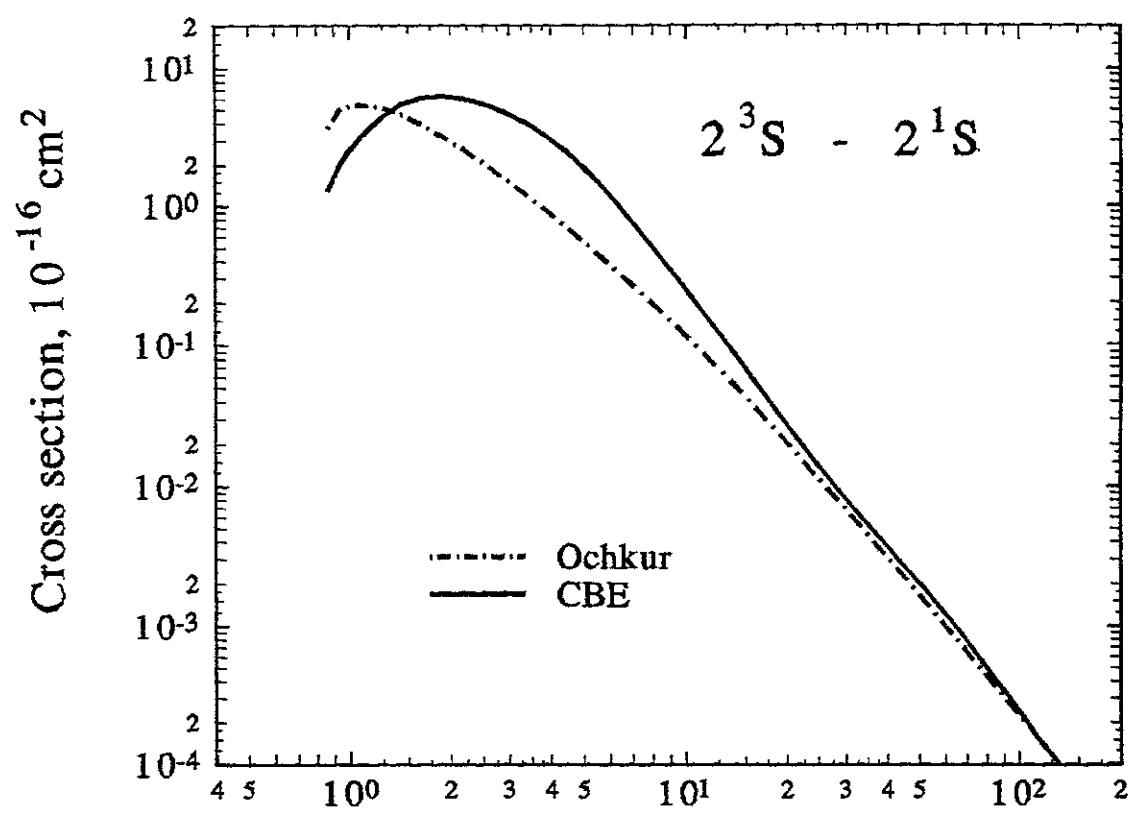


Fig.160 Electron energy, eV

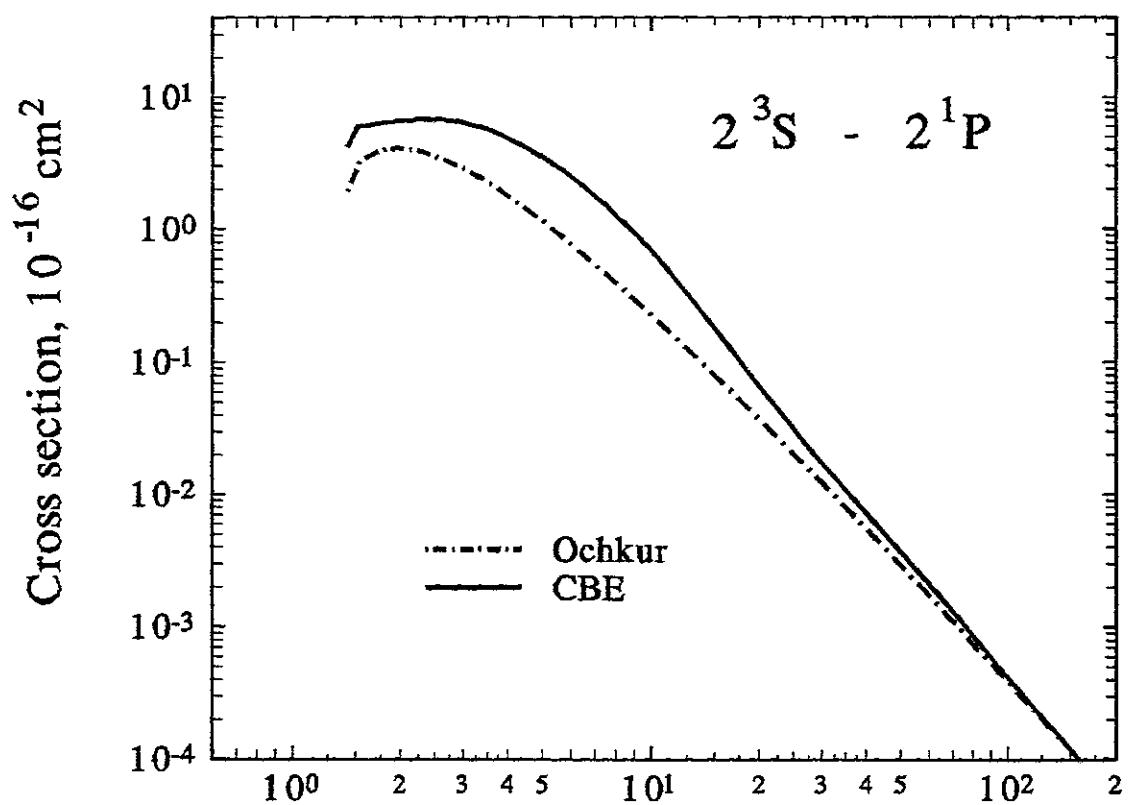


Fig.161 Electron energy, eV

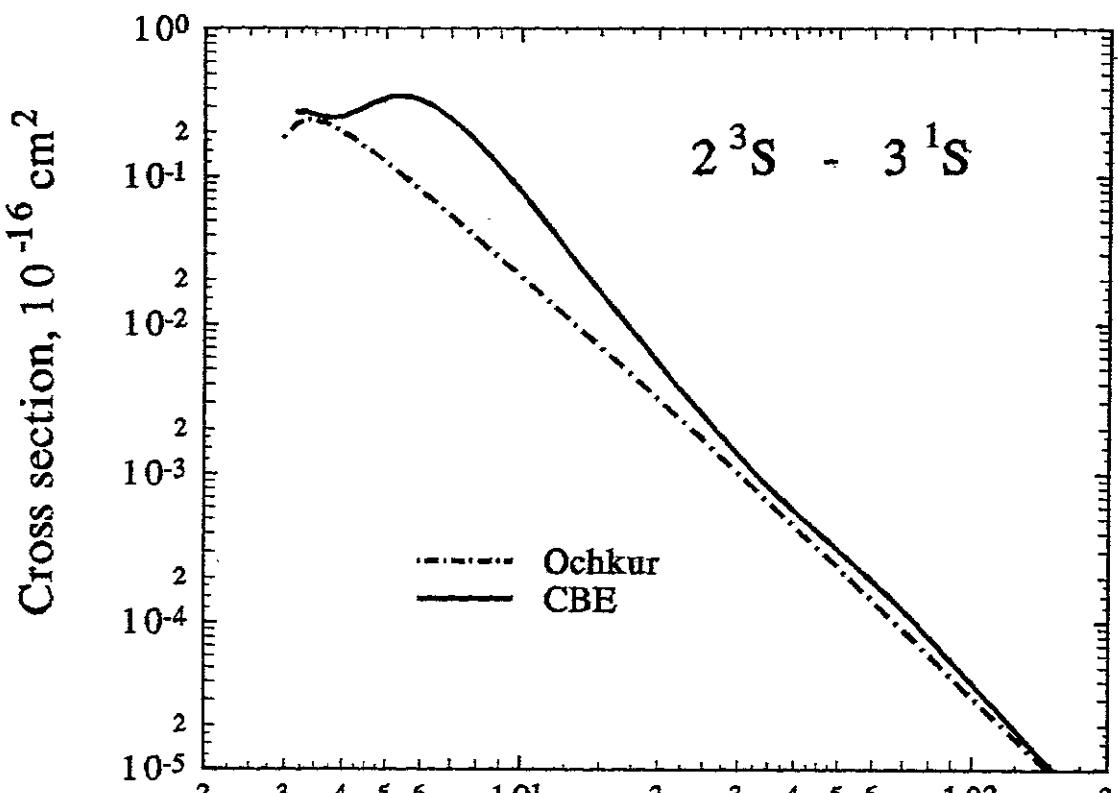


Fig162 Electron energy, eV

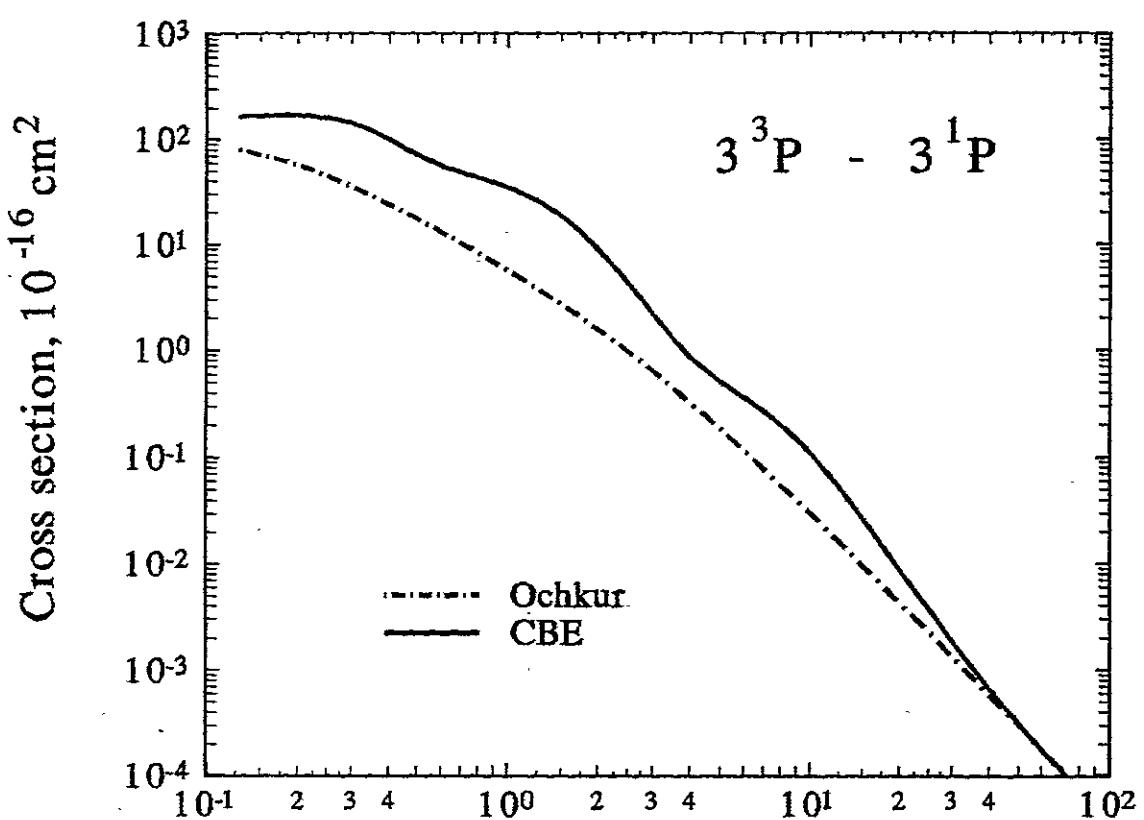
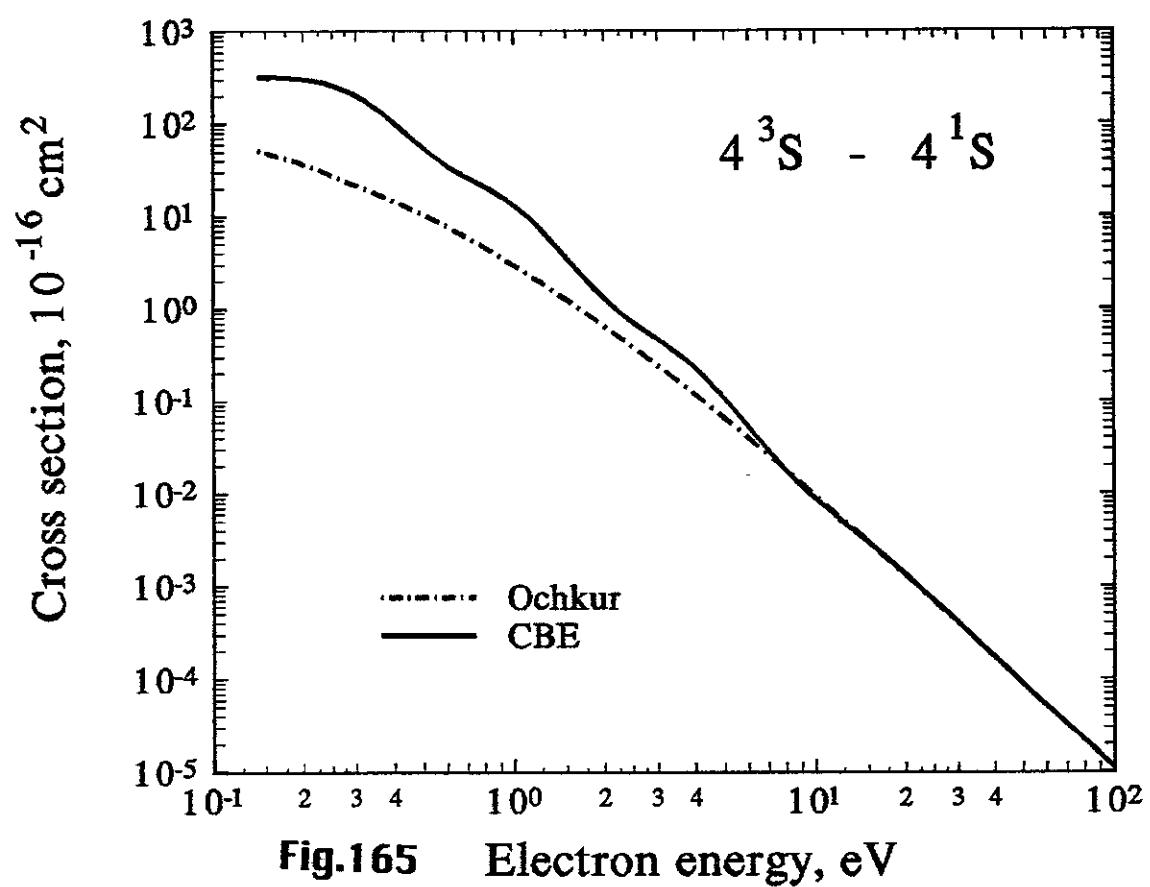
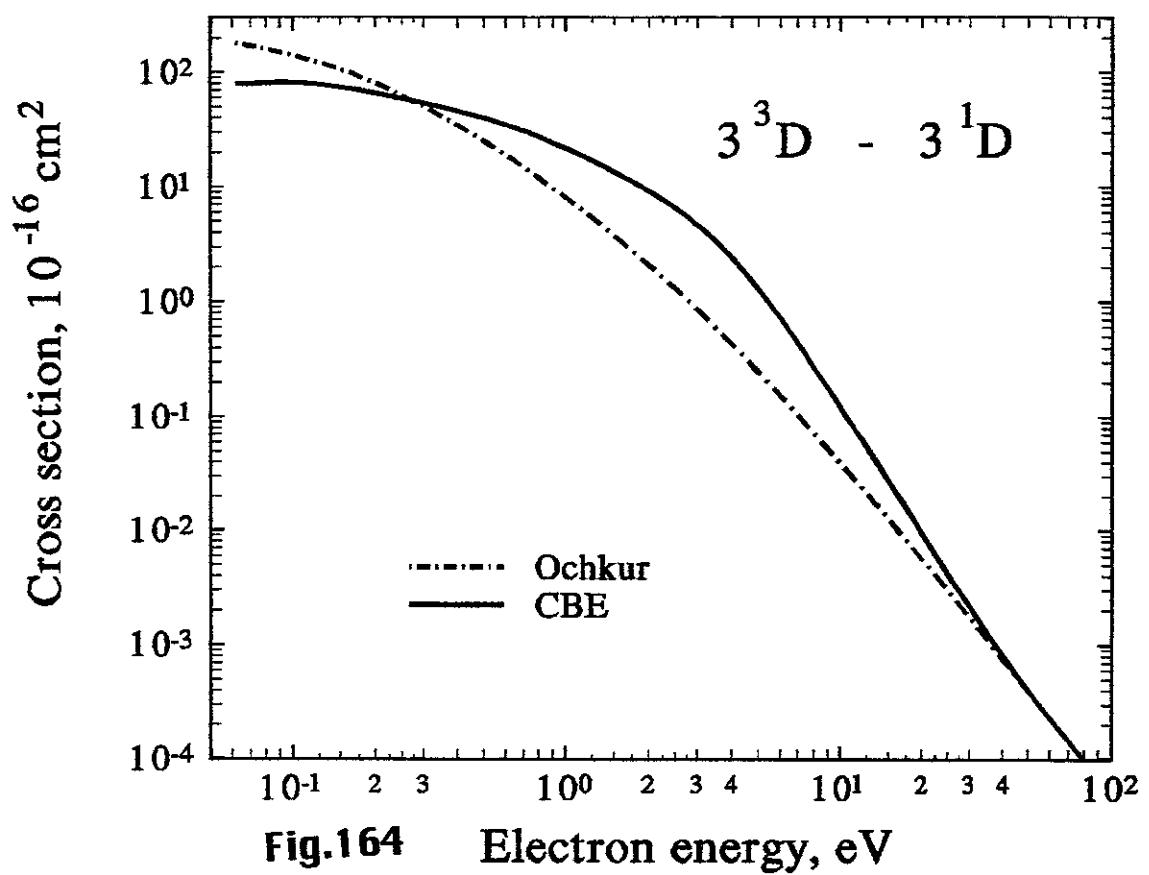
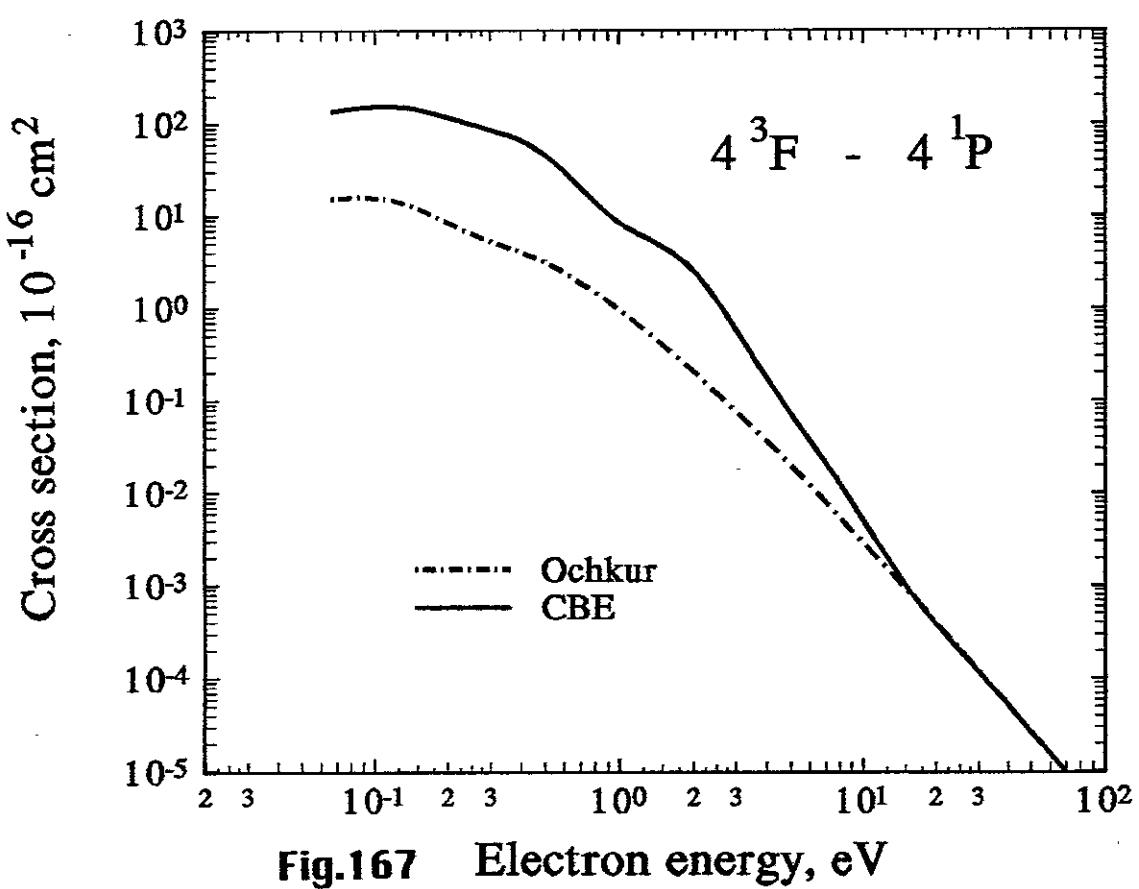
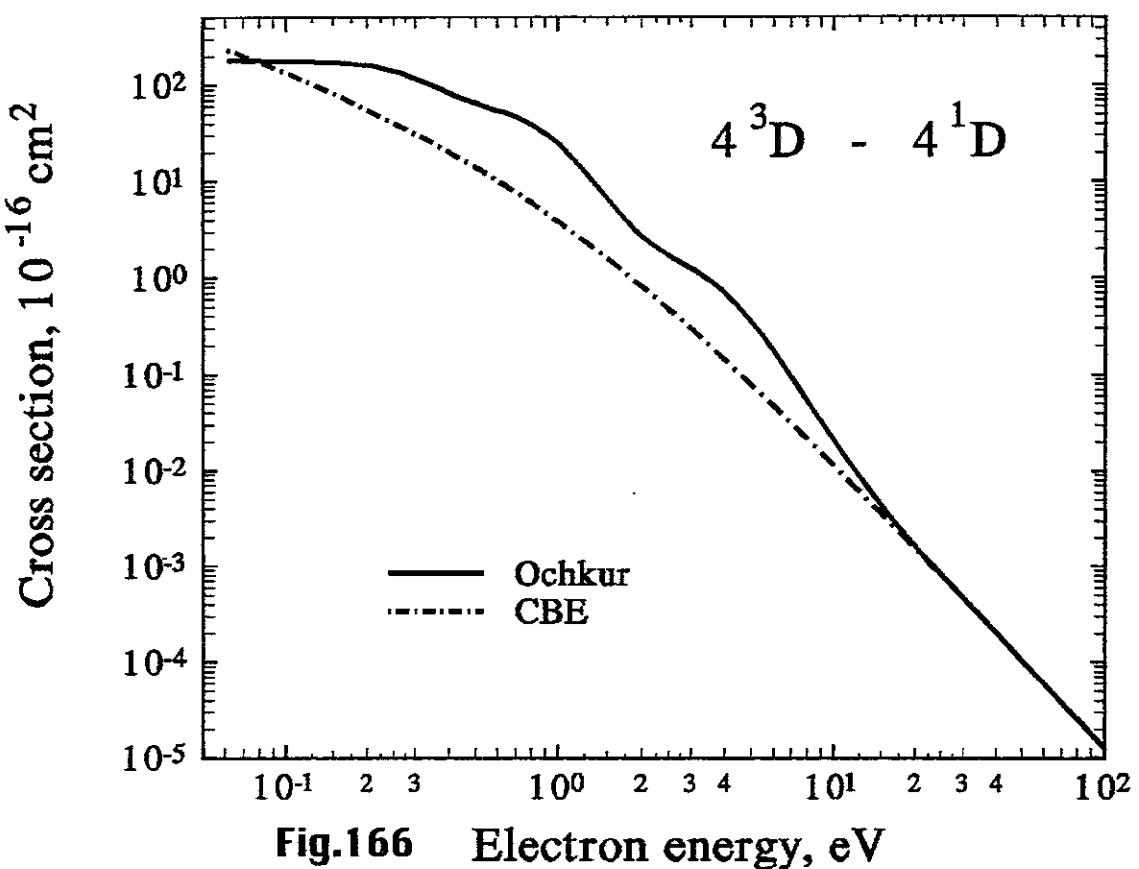


Fig.163 Electron energy, eV





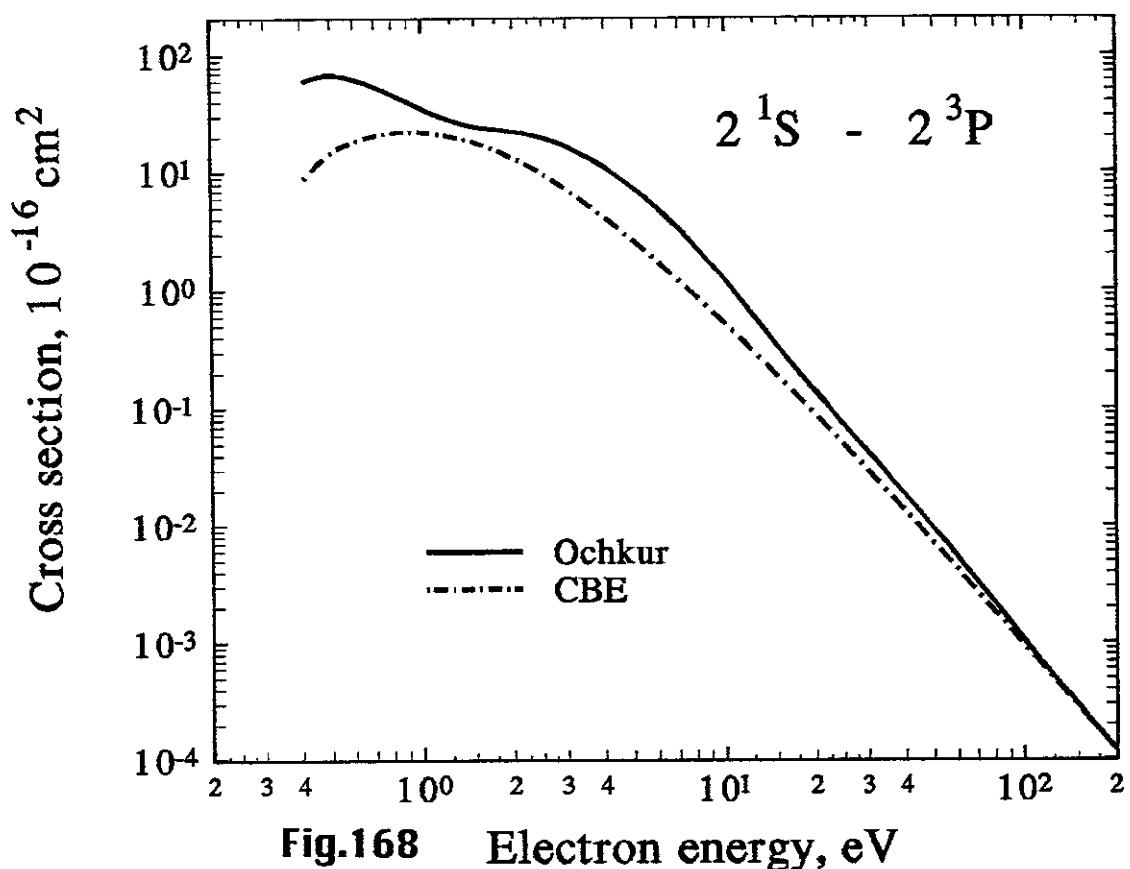


Fig.168 Electron energy, eV

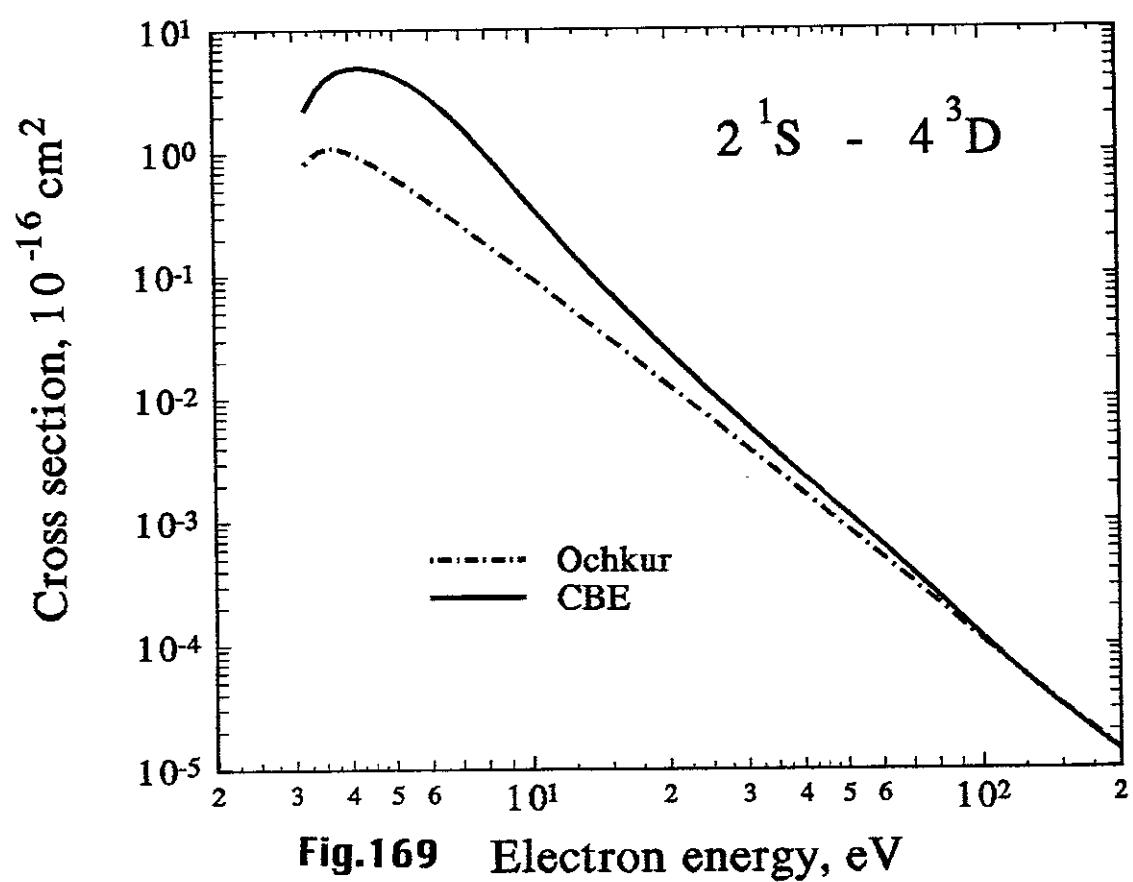


Fig.169 Electron energy, eV

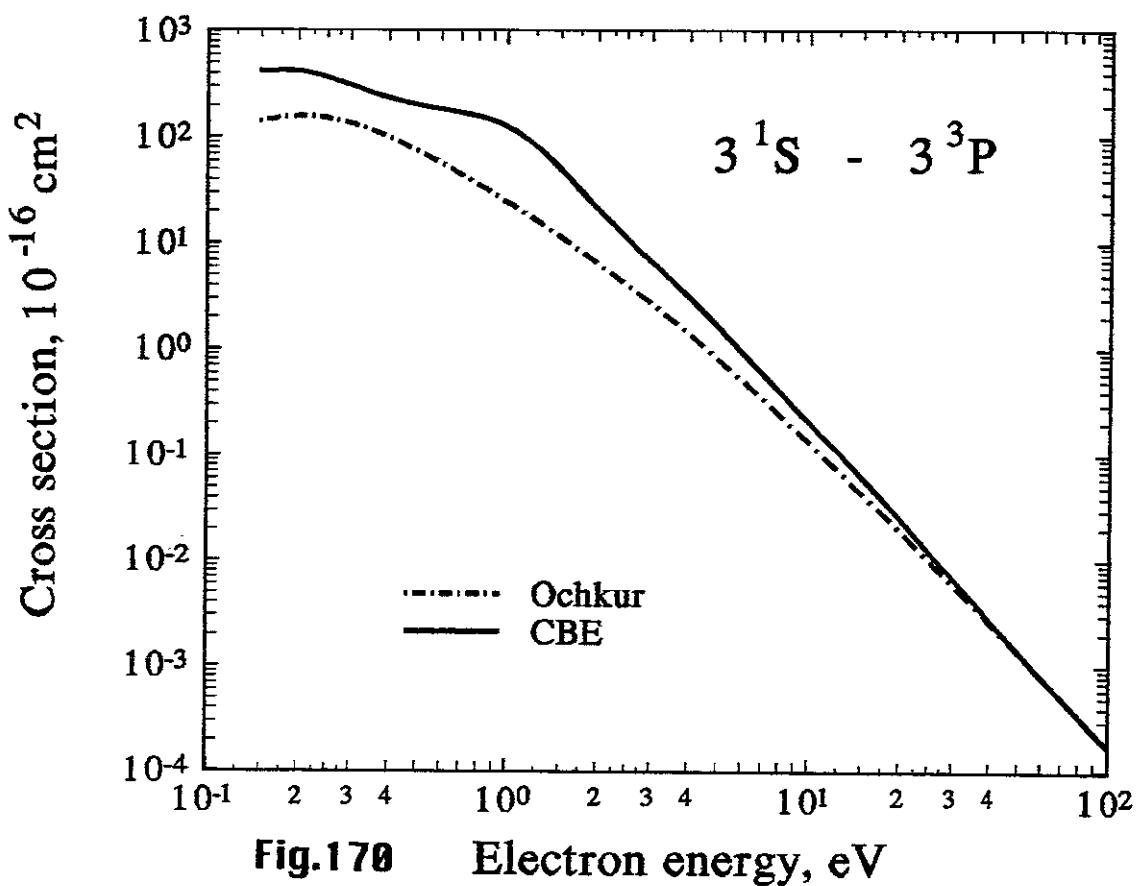


Fig. 170 Electron energy, eV

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